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NAVAL POSTGRADUATE SCHOOL Monterey, California



THESIS

ATTRITION IN THE UNITED STATES ARMY: AN EXPLORATORY DATA ANALYSIS APPROACH

by

David Alan Thomas

June 1984

Thesis Advisor:

Peter A.W. Lewis

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Unclassified

REPORT DOCUMENTATION	PAGE	READ INSTRUCTIONS BEFORE COMPLETING FORM						
1. REPORT NUMBER	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER						
Attrition in the United State An Exploratory Data Analysis	5. TYPE OF REPORT & PERIOD COVERED Master's Thesis June 1984							
		6. PERFORMING ORG. REPORT NUMBER						
David A. Thomas		8. CONTRACT OR GRANT NUMBER(*)						
9. PERFORMING ORGANIZATION NAME AND ADDRESS Naval Postgraduate School Monterey, California 93943		10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS						
Naval Postgraduate School Monterey, California 93943		June 1984 13. NUMBER OF PAGES 193						
14. MONITORING AGENCY NAME & ADDRESS(II different	from Controlling Office)	Unclassified Unclassified SCHEDULE						

16. DISTRIBUTION STATEMENT (of this Report)

Approved for public release; distribution unlimited.

17. DISTRIBUTION STATEMENT (of the obstract entered in Block 20, if different from Report)

18. SUPPLEMENTARY NOTES

19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Attrition, Enlistees, Exploratory data analysis, Graphical analysis, GRAFSTAT, Recruiting, Multivariate data, personal characteristics, Survival analysis, Survivor curves, Length of service, Education level

20. ABSTRACT (Continue on reverse side il necessary and identity by block number)
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Unclassified ECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)
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Attrition in the United States Army: An Exploratory Data Analysis Approach

bу

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Captain, United States Army
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Submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE IN OPERATIONS RESEARCH

from the

NAVAI POSTGRADUATE SCHOOL June 1984



ABSTRACT

71.1

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ACKNOWLEDGMENTS

This thesis is dedicated to the growing number of statisticians and analysts that believe in the use of Exploratory Data Analysis as a necessary part of any data analysis; in particular such people as Dr. John W. Tukey and Dr. Peter A.W. Lewis.

The graphs depicted in this thesis were produced by an experimental API package, GRAFSTAT, which the Naval Postgraduate School is using under a test agreement with the IBM Watson Research Center, Yorktown Heights, New York. The author of this thesis is grateful to Dr. P.D. Welch and Dr. Philip Heidelberger for making GRAFSTAT available for student use.



I. INTRODUCTION

A. BACKGROUND

The inception of the All Volunteer force in 1973 provided Army manpower planners with the challenge of attracting, recruiting and retaining high quality personnel. The ever-increasing technology on the battle-field coupled with budget constraints have forced manpower planners to search for an efficient alternative to sheer numbers. The soldier of today must be able to operate and maintain highly sophisticated equipment. In addition, the Army manpower planner must also cope with a decreasing supply of 18-21 year olds. In fact, this cohort is predicted to shrink by about 15 percent by 1988 when compared to the 1979 cohort, and by about 25 per cent by 1994 [Ref. 1: p. 2].

Cf ccurse, manpower shortages in the army are nothing new. Past shortages have been both quantitative and qualitative; the shortages historically have fluctuated over the years depending on the intricate balance among military requirements, civilian employment and wage alternatives.

[Ref. 1: p.1]

Currently Army recruiters have eliminated shortages. Through an extensive advertising campaign, army planners have taken maximum advantage of current economic conditions: since the inception of the All Volunteer Force, the army has met its objectives in numbers of enlistees in all but two years (FY77,FY79) and has met 100 percent of objective in the last four years [Ref. 2: pp.6-7].

The trends alluded to above, however, indicate that such case in manning the force may be short-lived. Army mannower



planners may be forced to recruit "less-qualified" soldiers just to meet manning requirements. More screening will be necessary to meet these requirements in an adequate fashion. One particular screen that has seen widespread use is education level [Ref. 3: p.342]. Future recruiting may not result in the high percentage of High School Diploma Graduates that is currently enjoyed: from FY79 through FY83 an average of sixty percent of all non-prior-service enlistees have been High-School Diploma Graduates [Ref. 2: pp.6-7].

The FY85 Army Eudget calls for holding active end strength to FY 84 levels [Ref. 4: p.16]. This in turn leads to maintaining an 80.6 per cent level of High School Diploma Graduate content [Ref. 4: p.16]. In order to maintain this level and maintain FY 84 end strength, a maximum of 12 per cent of total enlistees may be non-high-school diploma graduates (NESDG).

In light of increased (due to inflation) or at best constant recruiting costs, army manpower planners must necessarily be concerned with determining exactly what level of education produces the best recruiting risk. In other words, if Non-High-School Diploma Graduates and Graduate Equivalent Degree enlistees are a necessary part of the force structure, what, if any, are the associations between education level and "performance"? This research effort will provide some insight to this question.

Scme commonly accepted measures of performance currently in use by army manpower planners are

- 1. Attrition (various definitions and levels),
- Skill Qualification Tests scores,
- 3. Military judicial and non-judicial actions or lack thereof.

[Ref. 5]



The term attrition itself has taken on many different meanings in recent research. In many studies, attrition has been defined as "failure to complete the first term of service." [Ref. 6: p.24] In this study total length of service obtained will be used as a measure of performance in the initial analysis and the above definition will be used in later more detailed analysis.

Manpower policy makers have been investigating attrition since the early 60's [Ref. 7: p.1]. Such research has attempted to predict attrition through various sorts of models. Across the Army, Navy, and Air Force, level of education, mental ability and age have been determined as the lest "pre-service" predictor variables of attrition [Ref. 7: p.1].

The cost of "assessing, dressing and training" a typical soldier has been estimated at approximately \$15000 [Ref. 8 p.16]. This initial cost resulted in a total cost of \$1,743,200,000 in reaching FY 83 enlistment goals, based on 116,215 accessions [Ref. 9: p. i]. Obviously one means of meeting requirements at minimum cost is to reduce unnecessary losses of money through premature attrition.

Attrition studies have been, for the most part, based on different forms of regression models, particularly linear and logistic models using both individual occupations and occupational groups. [Ref. 10: pp. 1-10]

B. PURPCSE OF RESEARCH EFFORT

The purpose of this thesis will be twofold:

1. To demonstrate the usefulness of Exploratory Data Analysis (EDA) techniques in "preprocessing" large volumes of data generally associated with any manpower analysis. This thesis will use a study of attrition of U.S. Army enlistees as the vehicle for



this demonstration. The dependent variable under investigation is specified as "total active federal service". This phase of the research will provide examples as to how EDA techniques can assist manpower analysts and decision makers in determining problems in the data under analysis and in variable selection. (a discussion of exploratory data analysis techniques is found at Appendix A)

2. Upon selection of suitable predictor variables of attrition, an analysis of survival functions will be utilized to provide more detailed information.



II. DATA AND METHODOLOGY

A. THE DATA

1. DMDC Cohort File Description

As stated, the data used to fulfil the purposes of this thesis was the FY79 COHCRT file, maintained by the Defense Manpower Data Center (EMDC) at Monterey, California. This COHORT file is a longitudinal register of all accessions for a given year, updated at various predetermined times so as to allow for tracking of performance of that cohort in subsequent years. The FY79 cohort under investigation was last updated in September 1983. The file deficts each individual through 69 variables [Ref. 11]. FY79 was arbitrarily selected as a representative sample; it should be noted that the data from any given year may be confounded by political, social, and economic factors which are highly subjective and difficult to measure.

2. Freliminary Investigation and Data Reduction

The data set was reduced based on a request for an investigation into non-high-school-graduate performance from the United States Army Recruiting Command (USAREC), Fort Sheridan, Illinois. This request and subsequent telephonic requests for information suggested investigation into three military occupational skills (MOS): specifically at least one MCS from each of the major subdivisions of the Army, namely Combat Arms, Combat Support, and Combat Service Support. A histogram of the FY79 accessions (with non high school diploma graduate status) by MOS was developed (Appendix B) and subsequently the MOS's rank ordered by numbers accessed. Eased on this ranking, Table I depicts the MCS's chosen for analysis.



TABLE I Military Occupational Skills To Be Analyzed

Major Subgroup of Army	MOS
Combat Arms	11B Infantryman 11X Infantryman 13B Artilleryman
Comhat Support	64C Motor Transport Operator 31M Multichannel Communications Operator
Ccmbat Service Support	76Y Supply Specialist 94B Food Service Specialist

In addition, the data set was further reduced to only non-prior-service male accessions, based again on conversations with USAREC. Of course, all education levels were included so as to be able to ultimately compare the effects of education level. A data request was provided to DMDC for the data described above; the final form of the data was in character form, stored in 5 files on the Mass Storage System of the Naval Postgraduate School computer system.

3. Freparation for Exploratory Data Analysis

Eased on the above reduction of the data, the 69 available variables of interest were reduced to 14 variables to limit the scope of the investigation and to demonstrate the use of the Exploratory Data Analysis techniques. It should be noted that these procedures will be useful on any size data set for any number of variables subject only to the limitations of the storage capacity of the computer system in use. Table II provides a listing of this first selection of variables.



TABLE II
Initial Variables of Interest

Explanatory Variables	<u>Levels</u>
High School Level Cbtained Current Pay Grade Marital Status (current) Number of Dependents (current) Character of Service Reenlistment Code	13 31 29 4
Age at Entry High School Level at Entry Sex Race	15 13 23 20
Ethnic Ccde Marital Status/No.cf Dependents at Entr AFCT Group (Mental Category)	y 20 8

<u>Derendent Variable</u>

<u>Levels</u>

Total Active Federal Service

Number of months

Total active Federal service was chosen as the dependent variable at this stage of the analysis to allow for investigation of possible associations with the above candidate predictor variables over time as opposed to a "go-nc-gc" binary representation of attrition. This dependent variable allows the decision maker to initially see the effects of the candidate predictor variables on different levels of attrition, whether the assessions contracted for three cr four years cf initial service.

These variables having been selected, simple FORTRAN and AFL programs (Appendix C and D) were written to retrieve the data from mass storage into an interactive environment for graphical analysis.



B. HETHCDOLOGY

Exploratory data analysis techniques are to be utilized to analyze the data described above. A draftsman's display [Ref. 12: pp. 136,145] is prepared to initially process the data. Association between variables of interest are determined as well as any possible errors in the data. necessary refinement, further Draftsman's displays utilized to select possible explanatory variables. Boxplot analysis is performed to analyze the distribution of the levels of the candidate explanatory variables and their contribution in determining length of service. A comparison of the statistics of each distribution is utilized to determine relationships among the various levels of each of the candidate explanatory variables. Confirmatory analysis in the fcrm of parametric and nonparametric hypothesis testing is presented to indicate the statistical significance of sample comparisons.

Finally, a survivor function approach is utilized to analyze for probabilistic relationships. Failure times and survival times are identified that lead to calculations of the probability of attrition and reenlistment for both the three year enlistees (3YO) and the four year enlistees (4YO) from the FY79 COHORT data.



III. EXPLORATORY DATA ANALYSIS

A. INITIAL DRAFTSMAN'S DISPLAY

described in Appendix A, the draftsman's display AS [Ref. 12: pp. 136, 145] is an efficient means of taking a "first glance" at a data set. In addition, the use of APL as a programming language for this analysis allows for rapid manipulation of large arrays in a user friendly fashion. ten percent sample of the data set consisting of the variables listed in Table II above was run through the "draftsman" program [Ref. 13]. Sampling was performed by reading every tenth record of the data set provided by DMIC. file was prepared in Social Security Account Number order so 10 percent sampling ensured that a country-wide sample was created. Also, the file being longitudinal, any length-tiased sampling problems were avoided [Ref. 14: The output produced was a 14 by 14 matrix of two dimensional scatter plots. A segmented copy of the display is found at Appendix E. Refer to this Appendix for the following discussion. Note that the data has been "jittered" to reduce cverlap of the data or data points with the same discrete values [Ref. 12: p.21]. (note:ccding of the variables is defined in [Ref. 11])

First an overall view of the entire display is very useful to an analyst in several ways:

1. Categorical data is rapidly identified by the "blocking effect" seen in most of the displayed variables, e.g., "Marital Status" vs. "MOS." This aspect of the display is critical in allowing the analyst to "see" the data and immediately determine where dummy variables, for example, may be necessary.



- Also coding of the variables is displayed as in "Hs 2. at entry " vs. "Total Service" One observes that the scale of education ranges from 0 to 13, with the majority of the data grouped at 4 and 13, which ccrresponds to 2 years of high school and a Graduate Diploma (GED), respectively. Fortunately, in this analysis, the file description containing the coding schedule was available; one can envision the usefulness of the graphical technique in "uncoding" data sets that may not have an accompanying description. The analyst could then recode as necessary with many of the commonly-used file maragement systems available.
- Errors in the data may be identified in a rapid and 3. efficient manner. Again referring to "HS at entry" vs. "Total Service". the majority of the data is shown to be 2 year high school level (4) and GED Now the official request for data to DMDC was for all education levels. Because of a simple misunderstanding and a misplaced operand in the code that extracted the data from the master cohort file, only NHSG data were provided. The use of the display, then allowed for the prevention of the costly mistake the unsuspecting analyst may have made in developing a model with erroneous data. This error-preventing aspect of this procedure manifested itself in subsequent displays as will be discussed later.
- 4. Although further analysis was not performed, the display allows the analyst to determine multicollinearity/interaction effects of the concomitant variables. For example, "Age at entry" vs. "Number of dependents" plot may provide the impetus for further study, if either of the variables had a visual effect on, say, total service.



The use of the entire display is simple and "intuitive". It allows an analyst to bridge the gap, at least in some fashion, between the quantitative world of the analyst and the "real" world of the decision maker through the power of the brain's visual correlation abilities.

In the problem at hand, that is, the effect of various personal characteristics on performance (in the form of attrition or more generally, total service), analysis of the first column of the display is most revealing. Again, this data set has been discovered to only contain NHSG and GED; the entire spectrum of education levels will be analyzed in a subsequent draftsman's display. The first column of the display depicts scatter plots of all independent variables versus total Federal service. To aid in the discussion, seven of the plots have been reproduced in Figure 3.1 and the remaining seven in Figure 3.2 below.

Viewing both figures, no rapidly discernible or "glaring" associations are evident. This is largely a result of the sheer size of the data set.

However, much useful information is available:

1. Figure 3.1, MCS Versus Total Service:

• This figure indicates that the largest number of assesions were MOS 11B (a "1" in the DMDC coding) followed by 13B(2 cn coding scale). No 11X's are discernible because this entry level "basic foot soldier" MOS was not created until 1980. MOS 64C seems to have a distinct break in length of service: this break indicated that perhaps further analysis is needed. One possible explanation may be that a portion of the accessions entered this MOS only for the training, and subsequently left the service at first opportunity through an administrative discharge. MOS 76Y (6 on DMDC scale) seems to be the most successful in terms of



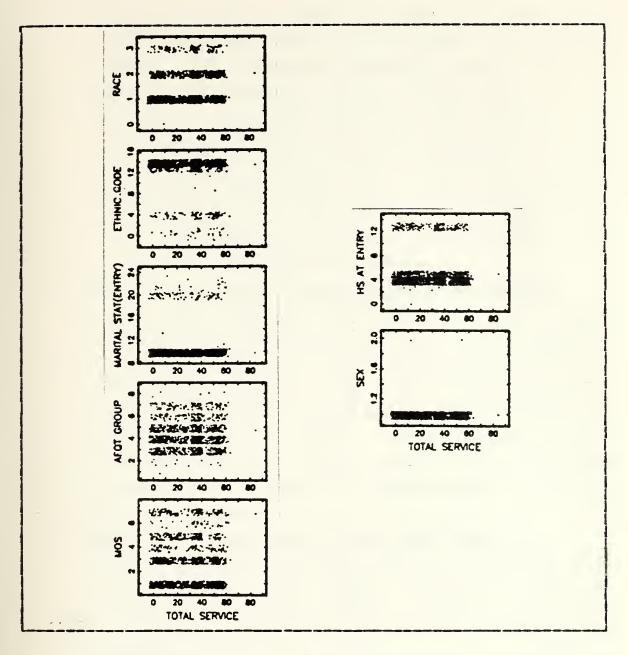


Figure 3.1 First Column of Draftsman's Display

performance (i.e., completion of at least 36 months of service).

2. Figure 3.1, AFCT Group Versus Total Service:

• This variable combination is coded from 1 through 8, with 1 being a Category V. This lowest category corresponds to an AFQT total score of 9 or less. A



slight trend is evident: as AFQT increases, more data points are found in the higher total service range. This graphical analysis agrees with the literature presented in the introduction of this thesis. This also indicates that most of the accessions considered here (NHSG and GED) are found in categories 3,4,5,6, which corresponds to mental categories IVB,IVA,IIIB, and IIIA, respectively. This leads to the conclusion, as expected, that NHSDG accession performance on the AFQT is in consonance with education level.

3. Figure 3.1, Marital Status Versus Total Service:

• This plot indicates that most NHSDG were single with no dependents (10 on the DMDC coding scheme).

Again the mass of data points requires further subsequent analysis. The upper grouping depicts a slight increasing trend as accessions differ by number of dependents (20=married/no deps., 21=married/1 dep., etc.). This, along with other aspects will be analyzed in more detail in section B, this chapter.

4. Figure 3.1, Ethnic Code Versus Total Service:

• This plot indicates that a great preponderance of the accessions were "other" which corresponds to Caucasian in the DMDC coding. Puerto Ricans (code 4) indicate increased total service, leading to the conclusion that race is an important predictor of service and attrition.

5. Figure 3.1, Race Versus Total Service:

• This plot reinforces that of the ethnic code plct.

Most assesions were white, as indicated by the mass of data at code 1. There is a slight increase of service indicated in the category 2 corresponding to blacks, and perhaps even a greater massing in



the 50-60 mcnth area of category 3, which corresponds to race "other". Again race seems to be a predictor of service or attrition.

6. Figure 3.1, Sex Versus Total Service:

- Although the data requested from DMDC was for male accessions (coded 1), at least a few data points are evident in the category coded "2", corresponding to sex "female". Subsequent analysis through an AFL program written to "scan" the data and count the frequency of certain data elements (Appendix D) indicated that in excess of 200 female NHSDG persons were accessed and recorded in this file. Again the draftsman's display and more generally the exploratory data analysis approach indicated erroneous data, perhaps preventing faulty analysis.
- 7. Figure 3.1. High School at Entry Versus Total Service:
 - Previously discussed above. This variable has seen widespread use as as a screening device in recruiting [Ref. 7: p.1].
- 8. Figure 3.2, Ace at Entry Versus Total Service:
 - This variable combination indicates a wide range of values because of the more "continuous" nature of the age variable. Although most NHSDG accessions were in the 18-20 year category, this plot indicates a slight increase in total service as age increases to about 25. Then the plot may indicate that older accessions do not fare as well in the measure of performance chosen. This agrees with the literature; further investigation is deemed necessary by the display.



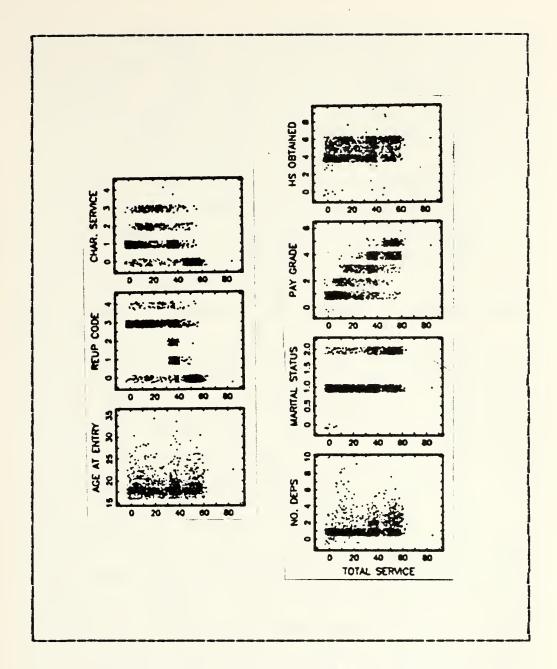


Figure 3.2 First Column Continued

9. Figure 3.2, Reenlistment Code Versus Total Service:

• This plot provides information that premature attritors and successful first- tour completers may receive the same reenlistment code. A "O" indicates unknown or no code, a "1" eligibility to reenlist, a "2" that a local bar to reenlistment



has been applied, a "3" that a DA-level BAR has been applied, and a "4" that the soldier is totally ineligible. The DMDC file description only provided 2 codes: again the display has indicated erroneous data or perhaps changed codes subsequent to latest file update. This display prompted a telephonic clarification to DMDC that may not have been made in the absence of exploratory data analysis. Since both "failures" and "successes" can receive a code of "eligible", this variable is not useful as a predictor of attrition.

- 10. Figure 3.2. Character of Service Versus Total Service:
 - This variable combination, like reenlistment ccde above, is ar indicator of "after the fact" rerformance, either premature attrition or successful first-term completion. Again, a "0" indicates unknown or uncoded data, a "1" an honorable discharge, "2" under honorable conditions, a "3" other than honorable conditions, and a "4" a dishonorable discharge. A massing of the data in the 0-20 month area of honorable discharges indicates that premature attritors were granted such a discharge through perhaps the Trainee Discharge Program or Expeditious Discharge Program. this variable combination is not a good predictor of performance since discharge award in some cases is based on the local commander's decision. often the honorable discharge may have been granted to speed the discharge of a substandard soldier: Under Honorable Conditions discharges, Other Honorable discharges and Dishonorable discharges require more "red tape" and administrative delays.



11. Figure 3.2. Number of Dependents Versus Total Service:

• This plot is an updated data entry that allows for the tracking of the addition of dependents through the serviceman's tenure. The plot indicates a majority of the service people considered through September 1983 still had zero dependents (coded "1"). As number of dependents increase, total service seems to increase, although there is a proportion of data points with more dependents that failed to complete 36 months of service. This plot indicates that with further analysis, number of dependents may be a predictor of total service and attrition.

12. Figure 3.2, Marital Status Versus Total Service:

• This variable is an updated variable indicating current marital status of the service member, a "2" for married and a "1" for other [Ref. 11]. The plot indicates a majority of the service members are still single. Married service members seem to demonstrate an increase in total service, indicating that this variable is a candidate predictor variable requiring further analysis. Again, this agrees with the literature.

13. Figure 3.2, Pay Grade Versus Total Service:

• Although pay grade is not really a relevant means of predicting performance of accessions, this plot gives a good indication of the "intuitiveness" of the graphical depiction of the data. This plot indicates an "ideal" upward trend: as months of total service increase, the mass of data moves upward and to the right. High performers are those that receive promotions earlier than the mass in that particular pay grade, for example, grade E5



indicated by a 5 on the vertical axis of the plot shows that the majority of the service members were promoted in the 48-60 month time frame, which is the norm. However, observe the points in the 38-40 month area, indicating waiver or early promotion. From this plot, one can ascertain some idea of the number of achievers in this cohort. Along the same lines, the poor performers are evident in, for example, the E1 grade in the 50 month time frame. The entire plot seems to indicate that there is the expected upward mobility of the average soldier.

- 14. Figure 3.2. High School Obtained Versus Total Service:
 - Although massive data size obscures the plot, this plot does indicate the some of the NHSG accessions have completed their GED requirements (a"6" on the scale) during this time frame. Of these that have completed, a slightly increasing trend is evident, again reinforcing the literature that education level is a suitable independent or predictor variable on attrition.

In summary this first draftsman's display has demonstrated that the graphical (EDA) procedures are critical in identifying erroneous data, determining variables of interest, and identifying multicollinearity/interaction effects. Now a more refined version, with an even further reduced list of candidate variables and in some cases, with variables that have been recoded so as to be more intuitively appealing was produced. This display is in segmented form at Appendix F. This version of the display was developed from the more general data set of FY79 accessions, this time including all education levels.



B. REVISED DRAFTSMAN'S DISPLAY

The initial exploratory analysis above revealed that

- 1. the data on hand was not suitable in that it did not contain High School Diploma Graduates (HSDG) for use in comparing any effects of education on performance;
- 2. the list of variables under investigation could be further reduced.

The purpose of this second iteration of draftsman's analysis was to serve as a final check on the data and to determine any other relevant information from the data prior to a more detailed investigation utilizing other methods.

TABLE III

Reduced Variable List for Further Analysis

<u>Dependent Variable</u>

Total Service

Explanatory Variable

Military Occupational Skill (MOS)
Marital Status/Number of Dependents
Race
Sex
Level of Education at Entry
Age at Entry
Mental Category

General Performance Indicators

Reenlistment Code Character of Service

The data shortfall in education level alluded to above was sclved in the submission of a request to DMDC for a more complete data set. This second data set was received and



again stored in 5 files in the Mass Storage System of the NPS Computer System. The FY79 COHORT file consisted of 30778 records of data. FIles for the FY80-FY83 COHORTS were also acquired for later model validation and subsequent research. It should be noted that the target data requested was to be non-prior-service (NPS) male enlistees. The variables under investigation for this phase are listed in Table III. The last two variables in the table were, as previously stated, not to be considered as predictors but as a means of assessing general performance of the enlistees.

Again, FORTRAN and APL programs (Appendices C,D) were utilized to retrieve the data from mass storage and to manipulate it into form for interactive analysis. A ten percent sample of the data was taken for analysis (3078 records). The data was again jittered to reduce overlap.

An overall view of the draftsman's display (Appendix F) demonstrated the following:

- 1. The new data set is mostly categorical as expected.
- 2. All levels of education have been included as demonstrated by the "HS at Entry vs. Total Active Service" plot.
- 3. The total service scale on all plots extends to 160 mcnths, indicating that at least some prior service enlistees have been erroneously included in the data.
- 4. Some female erlistees have been included as indicated by the "sex vs. Total Service" plot, again demonstrating erroneous data.

Most of the discussion below centers on the first column of the display; hence this column has been reproduced in Figure 3.3 and Figure 3.4 Viewing both figures simultaneously, the massing of the data points in heavily concentrated "blocks" demonstrates the large number of data points in the sample. The dimensionality of the problem is graphically evident. Some specific information that can be gleaned from this display follows.



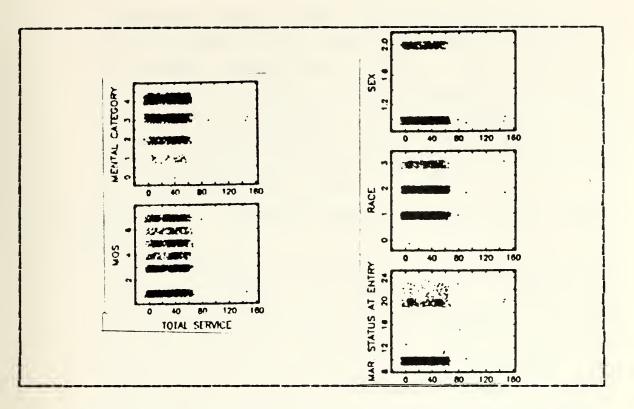


Figure 3.3 First Column of Revised Draftsman's Display

- 1. Figure 3.3, Military Occupational Skill vs. Total Service:
 - The 11B and 13B occupational skills (1 and 3 in the DMDC coding) appear to have attracted the most enlistees. No discernible trend or association is apparent in the length of service for these two combat arms occupational skills. Skill 64C (coded 4) demonstrates the "break" in length of service just as in the non-high-school-graduate data in the previous section. Occupational skill 76Y, (6 on the DMDC scale) as before, appeared most successful with less soldiers attriting within 36 months of service, or the normal first tour length.
- 2. Figure 3.3, Mental Category vs. Length of Service:
 - This variable corresponds to "AFQT group" in the original display, and has been renamed based on the



information seen in the first draftsman's display. This variable has also been recoded to reflect a 1 for mental categories 5 and 4c, a 2 for mental categories 4k and 4a, a 3 for categories 3k and 3a, and a 4 for categories 2 and 1. This plot demonstrates the recruiting policy of targeting the higher mental categories by the massing of the data in those respective areas.

3. Figure 3.3, Marital Status at Entry vs. Total Service:

• This variable is coded with a 10 for single with no dependents through 19 for single with 8 dependents, and then a 20 for married, no dependents, through 29, for married 8 dependents. Most enlistees in this data file were single with no dependents. The married enlistees (20 and higher on the DMDC scale) indicated a slightly increased total service, particularly as number of dependents increased (21,22 and 23 on the scale)

4. Figure 3.3, Race vs. Total Service:

• The addition of the high-school-diploma graduates has not affected the pattern that was evident in the original draftsman's display: a preponderance of whites (ccded 1) followed by blacks (ccded 2), and others (coded 3) is still evident. The "cther" category still demonstrates increasing length of service.

5. Figure 3.3, Sex vs. Service:

• As previously stated, this plot demonstrates that the supposed all male non-prior-service file has included in it a number of female enlistees. Also note that the massing of the data indicates that a large proportion of these females attrite with less than twenty menths service.



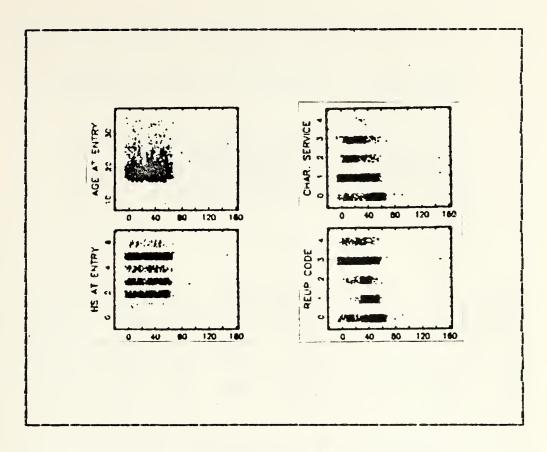


Figure 3.4 First Column, Continued

6. Figure 3.4, High School at Entry vs. Total Service:

 The inclusion of all levels of education can now be verified. The plot has been recoded utilizing an API program (See Appendix D) as shown in Table IV below: The massing of the data at position 5 indicates that most enlistees in this sample were high school diploma graduates. Also, enlistees with two tc four years high school outnumber those with equivalency status. No discernible differences can be observed in the equivalency certificate holders over the other levels of education due to massing of the data. Note the distinct in the GED length of service. A grouping though, is evident for zero to twenty months of service,



TABLE IV

Recoding of Education Levels for Draftsman's Display

```
1.... Up to 1 year of high school
2.... 2 years high school
3.... 3-4 years high school, no diploma
4.... Graduate Equivalency Diploma
5.... High School Diploma Graduate
6.... At least 1 year college and higher
```

and another for approximately thirty to forty months. This may be partially explained by viewing age at entry versus high school at entry along the same row as high school versus total service in Figure 3.5. This same break is evident: the

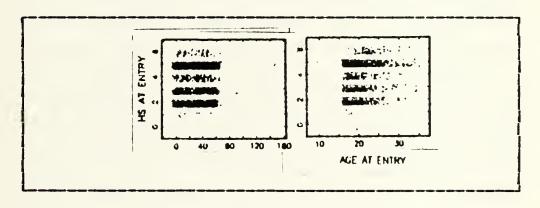


Figure 3.5 Row of Display for Cross Comparison

majority of the enlistees with the equivalency certificate (GED) are 20 years old and below with a break below 20. Perhaps this break in age when viewed with the break in service indicate that the GED enlistee is not successful younger as in ccmpleting service, just as he was in not completing high school.



- 7. Figure 3.4, Ace at Entry vs. Total Service:
 - The massing of the data indicates that most enlistees fall in the 17-21 category. As age increases, total service again seems to be divided into distinct branches. These branches could possibly be related to marital status, number of dependents, or education level, where breaks of this nature were also evident. See the entire display to compare each of the above mentioned variable combinations versus length of service and against other possible combinations of other variables for possible insights.
- 8. Figure 3.4, Reenlistment Code ("Reup" code) vs. Total Service:
 - This plot shows that a surprising number of enlistees, both premature "leavers" and successful (i.e., with more than 36 months service) "stayers", have an uncoded 0 reenlistment code. This probably indicates that the record has not been posted with this information. Code 1, corresponding to "eligible fcr reenlistment", is massed after 36 months, indicating that completion of at least the first term is a requirement for reenlistment eligibility. Ccde 2, a local bar to reenlistment, is also massed around 36 to 40 months of service, indicating that the decision to allow reenlistment is often reserved for the end of a soldier's term of service. It should be noted that the bar to reenlistment can be issued by the local commander at any time deemed necessary, yet it appears that exercising of this powerful option is not being Code 3, the Department of the Army bar to reenlistment, indicates a uniform massing of the data. This agrees with Department of the Army



policy to automatically bar soldiers that have received certain recognition as substandard through judicial, non-judicial, and administrative actions. Cross comparison with the next column of the display (see Figure 3.6) reinforces this idea: This plot is reenlistment code versus character of

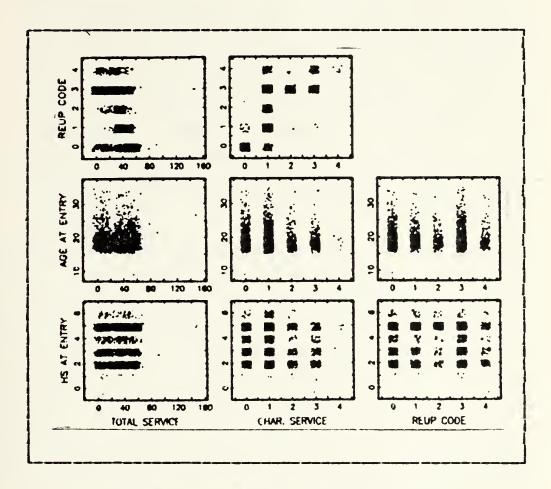


Figure 3.6 Segment for Cross-Comparison

service awarded. Reenlistment code 3 has the majority of the character of service codes 2 and 3 corresponding to "under honorable conditions" and "other than honorable "discharges respectively, both of which are considered substandard. Similarly, code 4 in reenlistment signifies



ineligibility for reenlistment, which is noticeably less of the data, contains the worst character of service code, a dishonorable discharge indicated by a 4 on the character of service axis.

- 9. Figure 3.4, Character of Service vs. Length of Service:
 - This plot indicates that as length of service increases to 38-40 months, character of service code decreases. The DMDC coding [Ref. 11] lists the coding as 1 for an honorable discharge, so one can infer that "stayers" generally receive honorable discharges. Those unsuccessful soldiers with less than 36 months service receive the majority of the "under honorable conditions", "other than honorable" and "dishonorable" discharges, coded 2,3, and 4 respectively.

This revised draftsman's display analysis has provided some insights into those personal characteristics affecting length of service and hence attrition. All seven possible explanatory variables under consideration have demonstrated at least some effects on length of service. The effects of education level, mental category, marital status and number of dependents, and age have at least initially seen to be most profound.

These displays have served to provide an initial graphical view of the data that is both intuitively pleasing and simple. In addition to identifying possible erroneous data entries and any peculiar coding of the variables, a major result of the analysis has been a reduction in the dimensionality of the data itself. The displays also aid in a general familiarization with the data under investigation.



C. ECXPLOT ANALYSIS

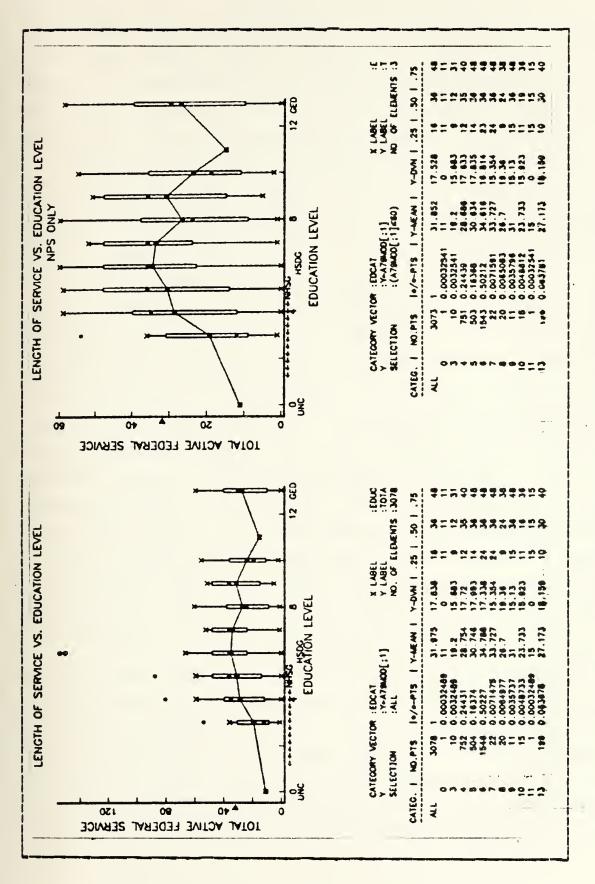
The boxplot will be utilized to demonstrate another Exploratory Data Analysis technique that provides a powerful means of obtaining more information about a data set. (See Appendix A for a discussion of boxplots in general.)

1. Education Level Versus Length of Service

In order to demonstrate the effectiveness and power of boxplots, one of the six candidate explanatory variables, high school education level at entry, will be investigated in detail. As stated in the introduction, the literature has pointed out that education level at time of entry has been a generally accepted predictor variable in attrition analyses during the last ten years. Therefore a boxplot analysis utilizing the category subpopulation analysis program in the IBM experimental GRAFSTAT package is presented in the following discussion. Length of service, the chosen dependent variable for this portion of the study, is plotted versus education level at entry.

The left panel of Figure 3.7 is a depiction of a ten per cent sample of FY79 enlistees as of September 1983. As previously stated, this data set is a smaller subset consisting of seven military occupational skills from the entire FY79 COHORT file from DMDC. The GRAFSTAT input screen for this program allows the analyst to subdivide this batch of data into its seven component occupational skills through the input of a simple "category" vector. (See Appendix G for a depiction of this input screen.) The y axis is length of total active service in months, while the x axis indicates education level at time of entry into the army. The non high school diploma graduate level is indicated by "NESDG" and indicates three to four years of high school without a diploma. Education level decreases toward





Length of Service, I Education Level vs. Figure



the origin, with a 4 indicating 2 years of high school, a 3 indicating 1 year of high school, a 2 indicating 2 years of junior high school, and a 1 indicating 1 year of junior high school. It the right of the position marked "NHSDG", education level increases until the position marked "GED" which indicates a graduate equivalency "diploma" or certificate. A 6 indicates high school diploma graduate, a 7 indicates 1 year of college, 8 for 2 years of college, 9 indicates 3 to 4 years college but no degree, and a 10 indicates a college degree. Fleven and 12 indicate a masters and doctorate degree, respectively.

Viewing the entire display in the left panel, the toxplct provides a graphical statistical summary of the distribution of each of the subcategories (i.e., the levels of education) in a form for easy comparison. A table of values is also presented beneath the display. The mean of each subcategory is depicted by the dot (with lines connecting the subcategories). The median of each subcategory is depicted by the other dot in the body of the bcx. Adjacent values and their associated "whiskers", or the lines drawn from the body of the box to the adjacent values depict the tails of the distribution of each subcategory. Outliers are depicted by heavy dots and are defined as those values greater than 1.5 times the interquartile range of the distribution. The mean of the entire display across all subcategories is depicted by the arrowhead on the y axis.

It is immediately apparent that this subpopulation contains some enlistees with prior service, indicated by the outlier values in the left panel of figure 3.7 that have more than 60 months of service. (If an enlistee entered the Army on 30 September 1978, max length of service without prior service is 60 months through 30 September 1983.) The data requested from DMDC was to be non-prior service (NFS) only; again the important error-indication quality of this



technique is readily apparent. The non-prior service enlistees can be easily extracted from the data set in the interactive mode of this package; by the insertion of a simple truth statement (e.g., length of service <60 months) the data set is reduced to the desired set. (See Appendix G for the depiction of the input screen; selection is entered in the "selection" area.) This feature is also most useful in the comparison of certain other characteristics of the data as will be demonstrated.

The ability to interactively subdivide the data according to other variables of interest is an extremely powerful tool, allowing the analyst to "compose" his areas of comparison and graphically determine associations in a multivariate sense. The actual data is never altered and there is no delay due to timely resubmissions of programs. In addition the graphical displays are rapidly available and intuitively appealing, requiring little explanation to those decision makers with less background in classical data analysis techniques.

The right panel of Figure 3.7 indicates the results of removing the cutlier enlistees with prior service. The scale of the boxplots is now larger so the mean, median, and spread can be readily ascertained. Note that the mean length of service has been only slightly modified by the removal of the 5 outliers (determined by the "ALL" row of the two tables below the plots, 3078-3073), as expected. Also note that the shape of the boxes before and after the removal of the outliers is the same, indicative of the resistance of the boxplot. The right panel of the figure shows that performance in the form of length of service tends to increase as education level increases from the junior high level to high school diploma graduate status. College level enlistees and higher do not demonstrate this trend. Note that enlistees with the graduate equivalency

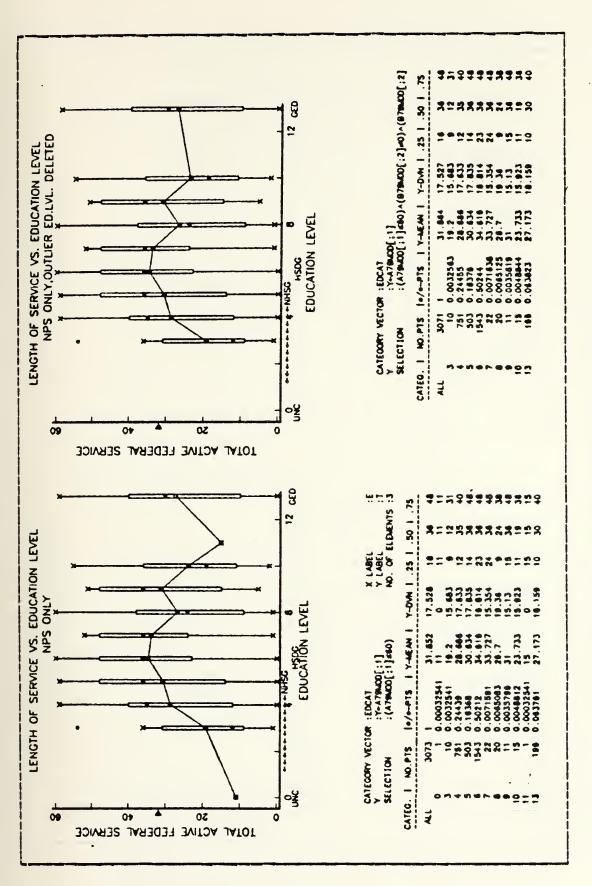


certificate demonstrate poorer performance than non-high-school-diploma graduates (NHSDG). The variance of the distribution of the enlistees with the GED is greater, perhaps due to the manner in which the GED may be awarded: Persons with any level of education can test for and gain the GED, and numerous tests are available for the certificate. Hence the large variance may be explained by the "variance" of the means of awarding the certificate.

In the next figure, (Figure 3.8), the non-priorservice enlistees are again presented in the left panel as a
"comparative other." In the right panel of the figure, all
those soldiers who had an uncoded education level and those
with FhD degrees have been deleted, again utilizing the
selection feature of the GRAFSTAT program. This results in
a "smccther" line through the means, allowing a more discernible view of the association of each level of education and
length of service. Note from the table that only 2 persons
were in these deleted categories, hence they are referred to
as "cutlier" education levels in the title of the plot.
These points will remain deleted throughout the remainder of
this particular analysis.

In Figure 3.9, left panel, the previously discussed boxplct with "outlier" education levels deleted, non-priorservice enlistees is again presented for further comparison. In the right panel, utilizing the selection capability, those enlistees with any years of college have been deleted. Now the increasing trend is clearly evident. As education length cf service increases. increases. Again thcse soldiers with the graduate equivalency certificate demonstrate a lower mean performance than both the non-highschool-graduates and the high school diploma graduates. isolate this trend even further, GED soldiers are deleted in the right panel of Figure 3.10 Now, compared to the left panel of this display, the upward trend is most evident.





Service, II Length of VS. Education Level 3.8 Figure



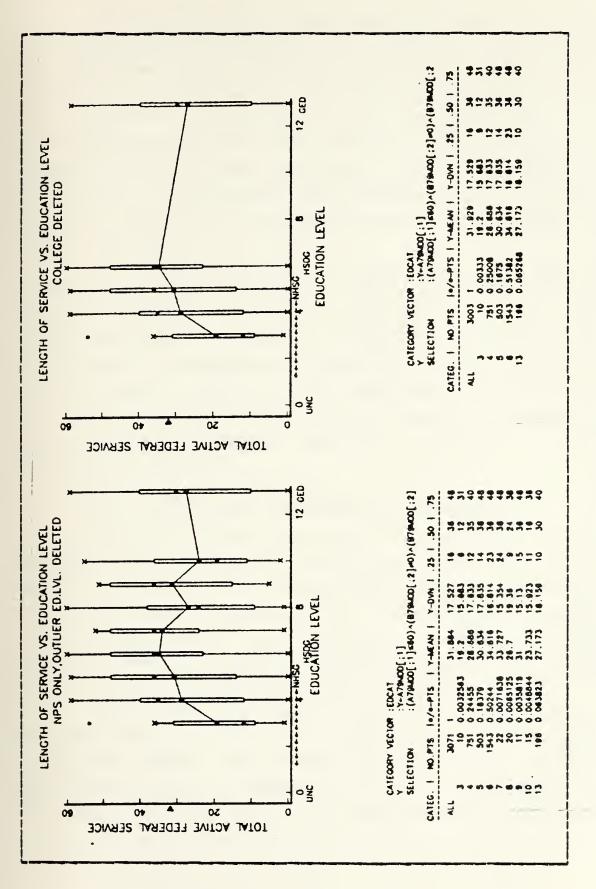


Figure 3.9 Education Level, College Deleted



The distribution of each education level is graphically described in the boxplot. For example, in Figure 3.10, the high-school-diploma-graduate distribution appears to be symmetric as indicated by the position of the mean and median relative to the ends of the body of the box. The distribution appears to have a "thicker" tail in the lower length of service side, depicted by the longer whisker on the bottom of the boxplot. Rapid comparisons of the distributions of each of the subcategories can be done through the hoxplot analysis.

Thus the use of boxplots has indicated that level of education does have an effect on performance in the form of length of service. It should be reiterated that this phase of the analysis is exploratory in nature; the comparison of means could be strengthened through such confirmatory analysis as a one-way ANCVA or in a non-parametric test such as the Kruskal-Wallis test of equality of means. An example of this confirmatory analysis will be provided in a later section of this thesis.

2. The Multivariate Capability of the Boxplot

Military occupational skill of the enlistee will be examined for any indication of an association with performance, and then further analyzed with regards to education level within the occupational skill. Seven military occupational skills (MOS) were considered in this analysis. (Refer to Table I, previous chapter). Again a ten percent sample of the data was utilized for analysis.

Figure 3.11, left panel, provides the first lock at this subcategory of the data. Military occupational skill is pletted against total active service. Each military occupational skill is presented on the x-axis, beginning with combat arms (11B, 11X, 13B), combat support (31M, 64C),

>.



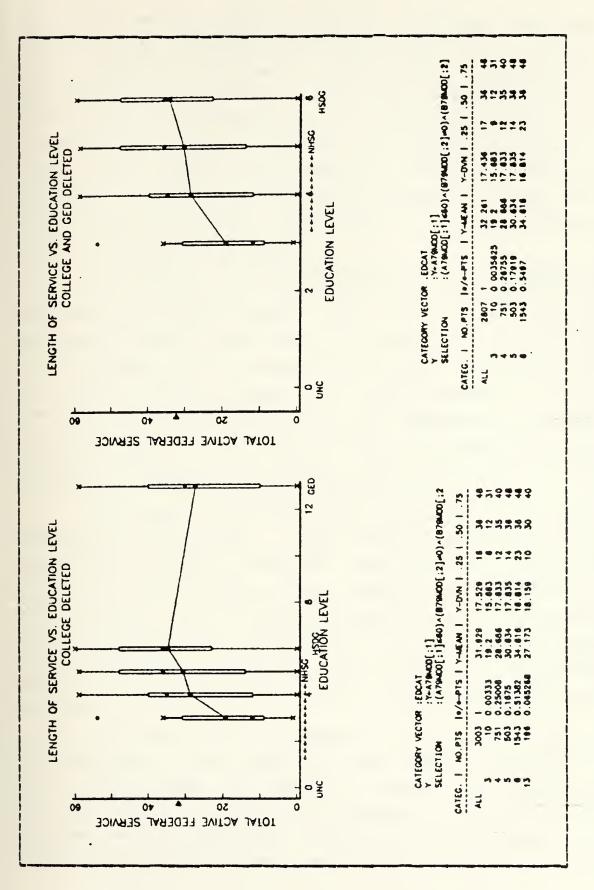


Figure 3.10 Education Level, GED Deleted



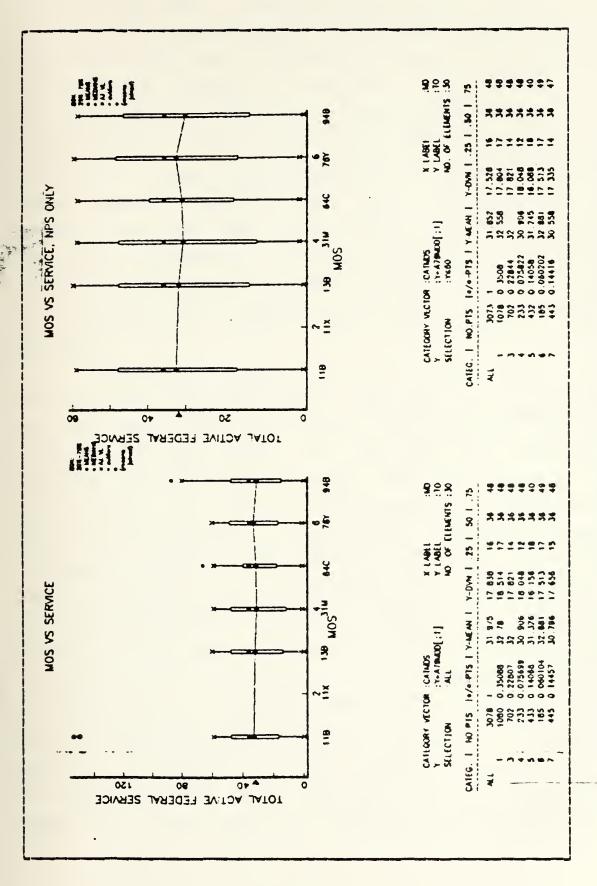
and combat service support (76Y,94B). As before, the distribution of each military occupational skill with respect to total service is presented by the boxplot. Again note the outliers in total service; these same 5 soldiers have been deleted in the right ranel so as to expand the scale of the boxplots for analysis. Through the graphical depiction of these distributions, the occupational skill most successful in terms of service can be readily determined. Here, skill 76Y, supply specialist, demonstrates the greatest success followed by 11B, Infantryman.

The spread of the distribution can be observed in the body of the box; note that the deviation is also provided in the table below. The 11% occupational skill is noticeably vacant. This MOS was created as an entry level of infantryman in FY80, hence this data set contains none of this general skill. Comparing the three branches of skills described above, combat arms was most successful in performance as determined by viewing 11B and 13B boxplots collectively. Combat service support was next in order of months successful service followed by combat support.

The shape of each of the distributions is readily apparent in the boxplcts. Each military occupational skill appears to be skewed toward the lower range of service as indicated by the postion of the median inside the bcdy of each boxplct. The variances appear relatively constant except for skill 64C. The utility of the boxplot in determining homogeneity of variance, for example, for subsequent regression analysis or for ANOVA assumptions is readily obvious.

In Figure 3.12, left panel, the previous figure of non-prior-service-only enlistees has been reproduced to allow comparisons. In order to isolate the effects of education level, all high-school-diploma graduates (and 60 enlistees with at least some college) have been selected cut of the subpopulation, using the selection capability. Thus





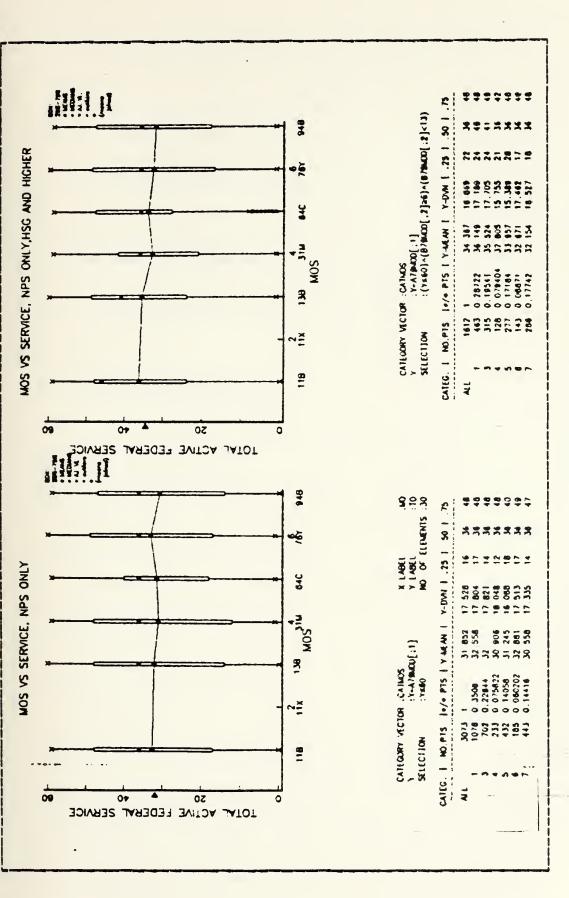
vs. Length of Service Military Occupational Skill Figure 3.11



in the right panel, non-prior-service, high school diploma graduates have been plotted against total active service. Immediately note that a higher mean service is observed by tetter educated enlistees. The variance cccupational skills has been reduced indicating that this subporulation is not as great a risk when considering how These soldiers in skill 11F demenlong each will serve. strate the highest success (mean 36.15 months). Based on these graphical results high school diploma graduates perform letter than the average non-prior-service enlistee, more specifically, combat arms skills rank followed by combat support, and then combat service support. This may seem counterintuitive as technical skills required are thought to be higher in the combat service support branches.

Figure 3.13 repeats the same sort of analysis, this time comparing non-prior service enlistees total service in the left panel to non- prior-service enlistees that have not received a diploma (NHSG) and those that have received a graduate equivalency diploma (GED). Note that "success" has fallen from 31.85 months to 29.08 months. Occupational skill 76Y has the highest mean success, and combat service support now leads in total mean service. Also note that occupational skill 31M demonstrates a much higher variance when only these non-high- school graduates are compared to the total population. This could perhaps be explained by the lack of any real standards in how the GED is awarded. This certificate can be awarded at any level of education, provided that one of numerous tests has been passed. the ncn-high-school graduate with ,say, only a 10th grade level of education could account for extremely poor performance in this somewhat technical microwave operator skill. Cn the other hand, those enlistees with an equivalency degree or 11-plus years of education from a "technically





Occupational Skill, High School Graduates Figure 3.12



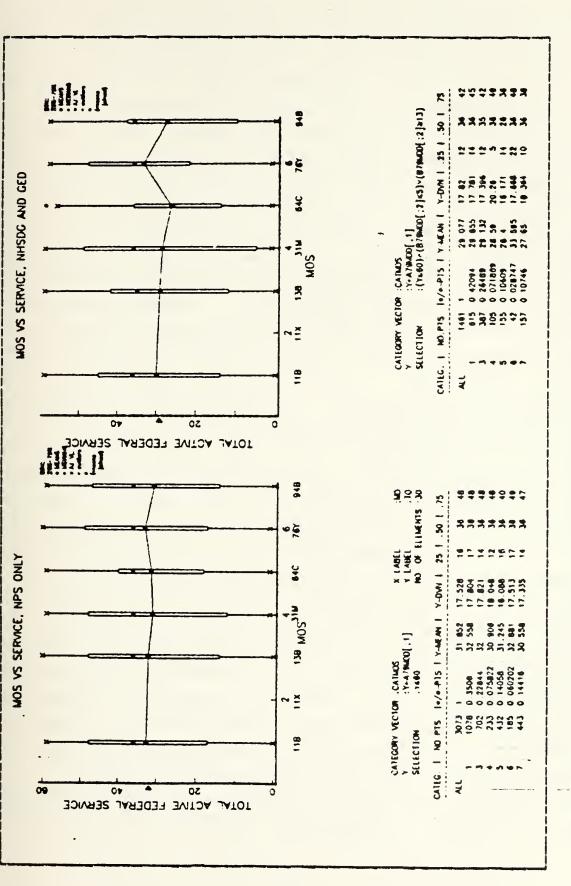


Figure 3.13 Occupational Skill, NHSG and GED



criented" school system could account for the high performance. More research could be performed in the area of "levels" of equivalency status and in a demographic analysis of those non high school graduates.

A comparison of high school diploma graduates to non-high-school-diploma graduates is presented in Figure Those soldiers with equivalency certificates (GFD) have been included in the non high school graduate category. In the left panel of this figure, the high school graduate category is presented for comparison. Again, this plot is non prior service only graduates. The right panel is nonprior-service, non-high-school-graduates and equivalency certificate holders. The "tetter educated" enlistees ,on the average, have outperformed those with less than a school degree (as shown by the mean values both in the boxplots and the tabled values below the plot). Skill 76Y, specialist, in the right panel, indicates a letter performance, (mean of 33.6) than the same occupational skill with a high school diploma (mean 32.7). The variance of the two distributions is roughly the same. Again personal characteristics and the technicality of the skill involved along with the effects of mental group distributions, enlistment tonus differences may explain this anomaly.

Since a difference has been established in performance based on the certificate status at entry, the toxplot can be utilized to go even into further detail. In Figure 3.15, non-high-school-graduates only are compared to high-school-diploma graduates and in Figure 3.16 those with equivalency degrees are compared to the diploma-carrying soldiers. In each figure, the batch remains limited to non-prior-service enlistees, varying only education levels.

Figure 3.15 demonstrates that the non-high-school-graduate performance, depicted in the right panel, was below diploma graduate performance. This is seen



graphically by comparing the relative position of the mean lines and in the tabled value below each plot. Going further, a comparison of each individual occupational skill in the left panel to its counterpart in the right panel indicates that the varied educational level produces and entirely different distribution. This is observed through the location of the respective means and medians, the size of the body of the box, and the length of the whiskers or tails of the distribution.

In Figure 3.16, this same difference in the distribution of military occupational skills with respect to education level is again obvious. In every case, the high school diploma graduates outperform the soldiers with equivalency status. Again, GED holders exhibit a larger variance as indicated by the body of the box, indicating a higher risk in attrition.

The entire analysis presented on the effects of education level within military occupational skill is summarized in Figure 3.17, where the baseline of ncn-prior service enlistees, categorized by occupational skill versus length of service is displayed simultaneously. Education level has been selected in each plot. Education military occupational skill, and length of service have been integrated into a single display. Any other combination of variables such as marital status, age, race, could be further selected to provide more of a multivariate display. The ELA techniques combined with the IBM GRAFSTAT package allows for any combination of covariates in an analysis, limited only by the imagination of the analyst. display allows a rapid comparison of the effects of education level on performance (in the form of length of service), perhaps providing a strong argument in these graphical methods for at least initial decisions regarding what level of education to recruit. Again,



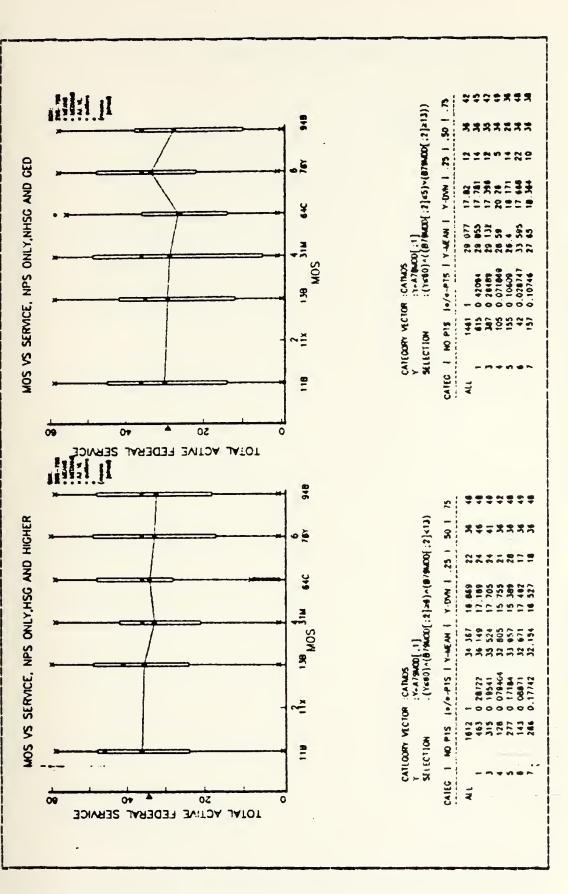
confirmatory analysis is necessary for a more refined analysis of relative merits of alternative educational policies.

3. Summary of Boxplot Analysis of Remaining Variables

The remaining possible explanatory variables and the two "general performance indicators" were analyzed in the same manner as presented above. In each case the effects of education level were observed in a multivariate sense by the use of selection combined with the pairwise comparison of length of service and the other candidate explanatory variables. The actual boxplots are found in Appendix H. Again, confirmatory analysis should be performed to verify the statistical significance of any conclusions drawn from this exploratory analysis. A summary of this analysis is presented below:

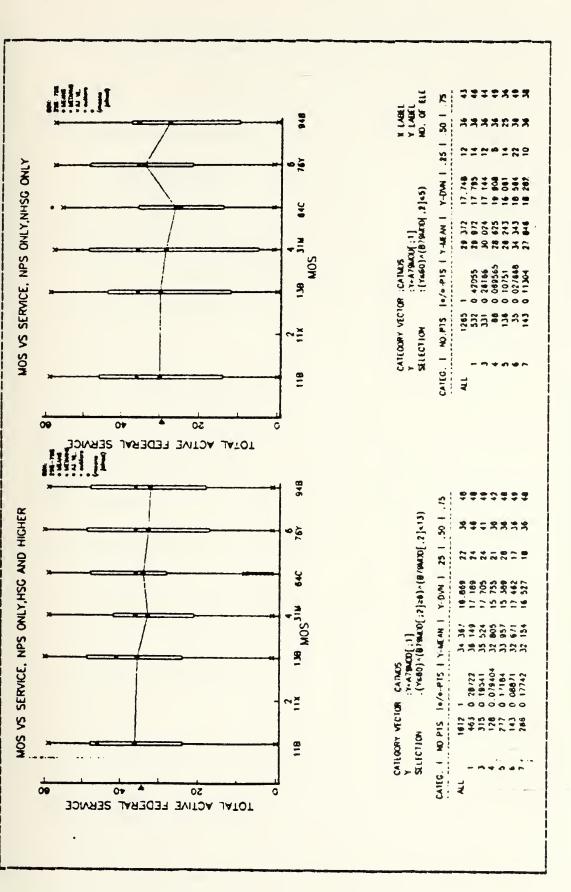
- 1. <u>Mental Category Versus Length of Service</u>: (See Figures H.1 through H.9, Appendix H)
 - As mental category increases, length of service increases. Category 4c outperform Categories 4b,4a,3b.
 - High school diploma graduates outperform the ncn-high-school-graduates and equivalency certificate holders (GED) in all categories.
 - Nc category 1 soldiers were observed in the nonhigh-school-graduate or GED categories.
 - Non-high-schcol-graduates outperformed the equivalency certificate (GED) holders in every category.
 - Variance in the non-high-school graduate and GED performance is higher than that of the diploma graduates, indicating higher risk in attrition. Equivalency certificate (GED) holders' variance was observed to be higher than non-high-school-graduates, again indicating a higher risk.





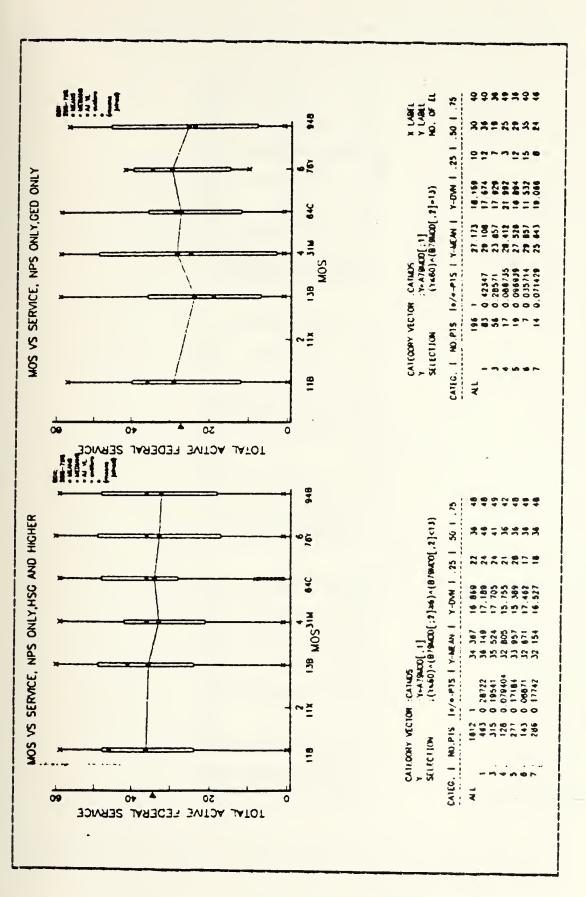
by Occupational Skill GED and NHSG HSDG, Figure 3.14





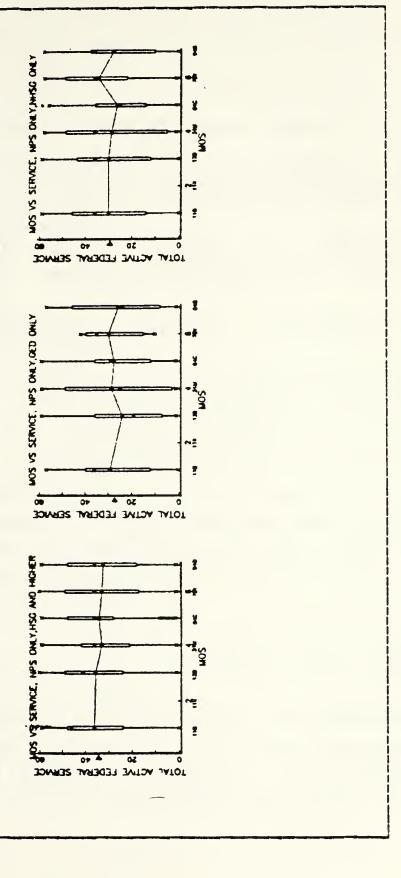
Diploma Grads VS. High School Grads Non 3.15 Figure





Liploma Grads VS. Equivalency Status 3.16 Figure





Recap of Effects of Education on Performance Figure



- 2. <u>Marital Status and Number of Dependents vs. Length of Service</u>: (See Figures H. 10 H. 15, Appendix H)
 - Most enlistees were single with no dependents at time of entry (92%)
 - Single enlistees with 1 dependent had highest mean performance.
 - In general, married enlistees outperformed single enlistees.
 - As number of dependents in married soldiers at time of entry increased, sc did performance. (note: true up to 3 dependents.)
 - High-school-diploma graduates led in performance, fcllowed by non-high-school-graduates, then GED hclders.
- 3. Age <u>Versus Length</u> of <u>Service</u>: (See Figures H.16 through H.24, Appendix H)
 - As age increases (at time of entry) from 17 to 19 years, total service (performance) increases, followed by a leveling off in the 19 to 24 year range. Performance decreases as age increases from 24 to 29 years old.
 - High-school-diploma graduates outperformed cther less educated entrants, non-high-school graduates followed, then equivalency certificate holders.
- 4. <u>Sex Versus Length of Service</u>: (See Figures H.25 through H.30, Appendix H)
 - Males outperformed females.
 - Dirloma graduates (HSDG) outperformed all other education levels; Non-high-school grads outperformed the GFD holders.
 - Non-high-school-graduate females outperformed male non-high-school-graduates and female high-school diploma graduates. However, non-high-school-graduate females displayed the greatest variance in



- length of service, indicating a possible higher risk in attrition.
- Non-high-school-graduate females were followed by GED males and then NHSG males in variance in length of service (risk).
- 5. Race Versus <u>length of Service</u>: (See Figures H.31 through H.36, Appendix H)
 - In general, the "cther" category were the highest performers, followed by blacks, and then whites.
 - High-school-diploma graduates were the highest performers in terms of length of service in all categories.
 - Non-high-schcol-graduates outperformed the graduate equivalency certificate holders (GED).
 - GED blacks displayed the highest variance in length of service, indicating a higher risk in attrition, followed by GED whites.
- 6. Reenlistment Code Versus Education Level: (See Figures H.37 through H.39, Appendix H)
 - At least through the high school diploma graduate level of education, as education increased, reenlistment eligibility increased.
 - GED soldiers received about the same reenlistment codes as these soldiers who entered the army with 2 years of high school.
 - A wide variance in reenlistment eligibility was observed, possibly related to the fact that reenlistment eligibility is mostly up to the local commander's discretion.
- 7. Reenlistment Ccde Versus Length of Service: (See Figures H.39 through H.44, Appendix H)
 - Approximately 30% of the sample was uncoded at the time of the last file update, indicating that the bar to reenlistment may not used as often as it



- could be as a rehabilitative tool for substandard scldiers.
- Generally, as length of service increased, sc did the number of soldiers eligible to reenlist.
- Approximately 50% of the GED holders and of the non-high-school-graduates indicated a reenlistment code of 3,ccrresponding to only 30% in the high-school-diploma graduates. This code corresponds to a Department of the Army initiated bar to reenlistment. This proportion seems a bit unreasonable and more research seems necessary in this multivariate combination.
- High-school-diploma graduates outperformed all others, followed by non-high-school-graduates and the graduate equivalency certificate holders.
- Again, the GED holders demonstrated the largest variance (risk) in length of service, followed by non-high-school graduates.
- 8. <u>Character of Service Versus Education Level</u>: (See Figures' H.45 through H.47, Appendix H)
 - Generally, as education level increased (at time of entry) through high school diploma, so did the character of service awarded.
 - GEC and non-high-school-graduate soldiers received about the same treatment in character of service awarded. Again, high-school-diploma graduates received the largest proportion of the honorable discharges.
 - Ccllege graduates outperformed the high-schooldiploma grads; however those entrants with one and two years of college were outperformed in terms of character of service awarded by the non-high school diploma graduates.



- A wide variance was noted possibly because of the commanders discretion allowed in determining what character of service will be awarded to an individual.
- 9. Character of Service Versus Length of Service: (See Figures H.48 through H.54, Appendix H)
 - As length of service increased so did the number of honorable discharges awarded.
 - Over half cf the cohort received an honorable discharge. A large proportion of early "leavers" also received this honorable discharge, perhaps indicating that some commanders are very lenient in their determination of type discharge to be awarded.
 - High-school-diploma graduates receiving honorable discharges performed the best in terms of length of service, again followed by non-high-school graduates and the GED's.
 - A wider variance in length of service was noted for the non-high-school graduates and the GED's who received honorable discharges, when compared to the high-school-diploma graduates. This perhaps relates again to the discretion that is exercised by the local commanders in awarding discharges. It seems that length of service may not be considered as an indicator of "good" service by a number of commanders in the field.

C. ENAMPLE CONFIRMATORY ANALYSIS

Conclusions drawn from the above explanatory data analysis must be analyzed in a formal manner to determine if differences, say, in the mean performance among the varying levels of education at entry is statistically significant.



An example is presented below; this type of analysis should be performed on all conclusions reached before any policy implementation.

The cne-way-analysis of variance provides a well-structured approach in testing the equality of means among k sample populations. In this approach, the k populations are assumed

- 1. to be i.i.d normal populations, and
- tc have equal variances.

As has been pointed out, some of the boxplot analyses above has indicated that the equal variance assumption is obviously not true; contrarily, this difference in variance was was used as an indicator of the "risk" involved in recruiting that entrant with his particular qualifications. In those cases, nonparametric tests are available for confirmatory analysis. An example of that type will also be presented below. See [Ref. 15: pp. 492-503] for a discussion on 1-way ANOVA.

The actual calculations of the ANOVA table were completed using an AFI program contained in public domain of the Naval Postgraduate School computer system (Library 5,0A3660). A copy of the program is at Appendix I. Results of the analysis are summarized in Table V Thus the null hypothesis can be rejected at the .05 level of significance.

In instances where the homogeneity of variance and normality of population assumptions are infeasible, nonparametric tests can be utilized for confirmation of statistical significance. The Kruskal-Wallis test was utilized to test the following hypothesis:

HO: mean services across all education levels are equal.

H1: for at least one pair of the population represented by the levels of education, the means are different. See [Ref. 16: pp.229-237] for a discussion of the K-W test.



TABLE V Ancva Table for Testing Equality of Means

ZEANOVA MATE ANOVA WAS UPDATED 1/3/79, SEE ANOVAHOW FOR CHANGES. ANOVA TABLE 55 MS DF SOURCE 6483.35 25933.42 21.67 TREATMENT 4 299,14 ERROR 2998 896813.33 922746.75 TOTAL 3002 R = SQUARE = 0.028OVERALL MEAN = 31.93 T4.76 2.69 T1.29 T3.24T12.73

TREATMENT EFFECTS

The actual calculations were performed utilizing the EMDP statistical scftware program P3S on the Naval Postgraduate School Computer System. See [Ref. 17: pp.442-443] for a description cf this package. Results are summarized in Table VI.

TABLE VI Results of K-W Test of Equality of Means

Variable Group	1 LOS Frequency	Rank Sum
No. Name 1 SOPH 2 JR	10 752	9064-0 1017353-5
GED KHSG BSDG	196 504 1546	250661.0 730567.5 2517723.0

Kruskal-Wallis Test Statistic = 75.13
Level of Significance = 0.0000
Using Chi-Square Distribution with 4 Degrees of Freedom



Thus the null hypothesis can be rejected at the .05 level of significance. Multiple comparisons may be calculated in accordance with [Ref. 16: p.231] to determine which pairs of means are different if desired.

E. SUMMARY OF EXPLORATORY DATA ANALYSIS EFFORTS

1. General

Exploratory Lata Analysis techniques have been utilized in the forms of draftsman's displays and toxplots to "preprocess" a large data set. This analysis was presented as a demonstration of the power of EDA techniques and to provide initial insights into the attrition of U.S. Army enlistees prior to further analysis. These techniques have provided the following:

- 1. Familiarity with data set.
- 2. Reduction in the dimensionality of the data set; numerous variables were determined as having no appreciable effects on the dependent variable under consideration.
- 3. Identification of erroneous data.
- 4. Structure of the data set and variable coding.
- 5. Information on multivariate and pairwise associations among the variables. This information will be summarized below.
- 6. An intuitively pleasing form of analysis to assist analysts and decision makers in understanding the problem at hand.
- 7. A means of allowing the analyst to "compose" his method of attack on a large problem in an interactive fashion.



2. FLA and U.S. Army Enlisted Attrition

More specifically, in the investigation of attrition of U.S. Army FY79 erlistees, the following information has been revealed:

1. The variables listed in Table VII below were chserved to have some effect on a soldiers performance which

TABLE VII Possible Explanatory Variables from EDA

Age
Sex
Race
Mental Category
Marital Status/Number of Dependents (at entry)
Education Ievel
Military Occupational Skill

has been defined as his total length of service.

- 2. Level of education at entry has an effect on the performance of enlistees. Education level seems to interact with the other variables listed in Table VII above, producing different levels of performance. Other insights provided by the analysis are
 - High school diploma graduates demonstrated better performance than did non-high-school-diploma graduates and those enlistees who had obtained a graduate equivalency certificate prior to entry.
 - Non-high school diploma graduates demonstrated letter performance than did GED holders.
 - GED holders demonstrated a larger variance in total service obtained, indicating a higher risk in attrition than did non-high school diploma graduates.



- 3. Character of Service and Reenlistment Code are two indicators of performance that may also be affected by education level at entry; however, the discretion exercised by local commanders in awarding these may have confounded them as suitable explanatory variables.
- 4. Confirmatory analysis needs to be performed after exploratory data analysis prior to forming final conclusion for policy implementation. An example was provided.

3. <u>limitations</u>

The EIA techniques are not to be used in lieu of more classical statistical analysis; they are to be used in conjunction with them. Some limitations are

- 1. Acceptance of their use by other statisticians.
- 2. Package utilized in this thesis is in the experimental stage; others may not be readily available to the analyst. Since this package is experimental, certain capabilities are still being developed. For example, in the the ANCVA presented, the means used in the analysis were not stored in a global sense for further analysis and had to be entered "by hand" into an ANOVA program.
- 3. Cost of graphics capabilities for computer systems.
- 4. Storage necessary for EDA packages is currently not available for most personal or desk top computers.

Thus Exploratory Data Analysis has been shown to be a useful technique in the initial analysis of data. In the next charters, a more formal analysis will be presented.



IV. SURVIVOR PUNCTION ANALYSIS

A. BACKGROUND

The Exploratory Data Analysis techniques presented (along with the necessary confirmatory analysis) have shown that level of education, sex, race, age, mental category, and marital status/number of dependents are candidate explanatory variables in determining the total length of service for an enlistee.

A survivor function approach is utilized to gain further insight into these explanatory and their relationship to length of service.

Surpose that the length of service of an enlistee is a random variable X. The cumulative distribution function or c.d.f., then, can be viewed as giving the probability that an enlistee will "die" or "fail" or leave the army before x units of time, a realization of the random variable X, have elapsed. Then the quantity

$$S(x) = 1-F(x) = P(X>x)$$
 (eqn 4.1)

called the survivor function, provides the probability that an enlistee "survives" more than x units of time. The survivor function, for discrete data, is a step function, where the height of the jump between any two values of x is equal to P(X=x). The survivor function is estimated by using the following relative frequency definition of probability:

$$S(x) = 1-F(x) = (number of observations > x)/n (eqn 4.2)$$



where n is the number in the sample being considered [Ref. 18: pp. 92-93, 263-264].

B. AFFLICATION

The survivor function is therefore a logical means of analyzing enlistee behavior with regards to length of service. For this portion of the analysis, attrition will be defined as failure to complete the first term of service. The FY79 COHORT consists of three-year obligated enlistees (3YO) and four-year chligated enlistees (4YO). Each subset will be analyzed separately. The reenlistment decision will be defined as completing greater than one term of service. Hence, based on the survival function model, the following equations indicate the "life" cycle of the enlistee:

TABLE VIII Enlistee Life Cycle Models

3 Year Enlistees

F(enlistee will attrite) =
$$P(X \le 36 \text{ mos.})$$

= 1- $P(X > 36 \text{ mos.})$ = 1- $S(X)$

F(enlistee will complete 1 term) = P(X=36 mos.) = Ht. of jump at x=36

F(enlistee will reenlist) = P(X>36 mos.) = 1-S(x)

4 Year Enlistees

F(enlistee will attrite) =
$$P(X \le 48 \text{ mos.})$$

= 1- $P(X > 48 \text{ mos.})$ = 1- $S(X)$

F(enlistee will complete 1 term) = P(X=48 mos.) = Ht. of jump at x=48

F(enlistee will reenlist) = P(X>48 mos.) = 1-S(x)



These realization times for the random variable X are chosen just to demonstrate the survivor function method-clogy. Considerable research has been done in defining the exact time cutoff for the definition of attrition, since the first "term" of service may actually be thirty-four months as opposed to thirty-six because of the various "early out" programs offered by different commands. This analysis does allow for at least this concept in its definition of attrition as strictly less than thirty-six and forty-eight months (i.e. thirty-five and forty-seven months) length of service for the three year and four year obligations respectively. The methodology suffices no matter where the attrition definition is made in the length of service parameter.

Survivor functions for each of the previously defined candidate explanatory variables are estimated utilizing the Cumulative Distribution input screen in the IBM GRAFSTAT data analysis package. (See Appendix J for a depiction of this screen.) These functions are analyzed for the above mentioned statistics.

The survivor function of the entire sample across all variables is presented to demonstrate the characteristics of the analysis in Figure 4.1 . Using this type of analysis, statistics for the most prevalent enlistee are presented in Figure 4.2 and in Figure 4.3 for 3 year enlistees and 4 year enlistees respectively. The "most prevalent enlistee" was determined by observing the total number in each of the seven variables being considered. Note that the four year obligated enlistees demonstrated higher probability of attrition (0.33 to 0.24), and a lower probability of reenlistment (0.12 to 0.37) than the three year obligated enlistee, ceteris paribus. This may indicate that the utilization of the three year term of service is more cost than the four year term, considering "assess, dress, train" cost described earlier. Results for the mcst prevalent enlistee are summarized in Table IX .



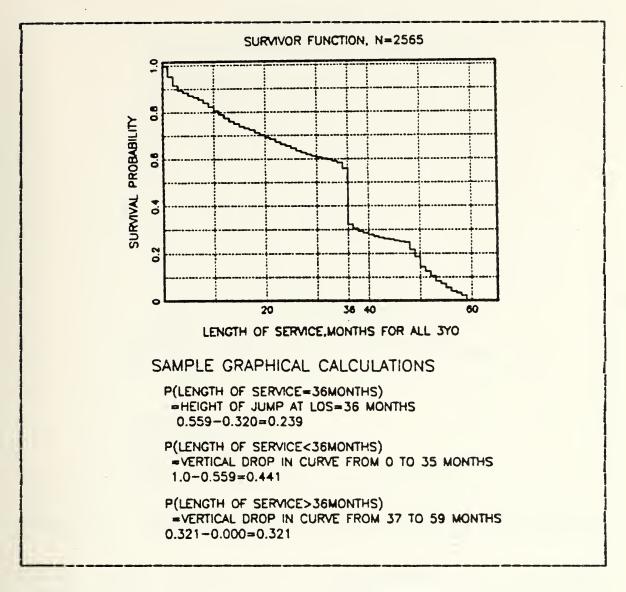


Figure 4.1 Survivor Function For All 3 YO Enlistees

The effects of education level on attrition of three-year-chligated enlistees are presented in Figure 4.4.

Those erlistees with a graduate equivalency certificate indicate a higher probability of attrition (0.54) than both those with two years of high school and those with non-high-school-diploma graduate (NHSDG) status, having three to four years of high school. These findings reinforce the earlier toxplot analysis of length of service. The trend is also



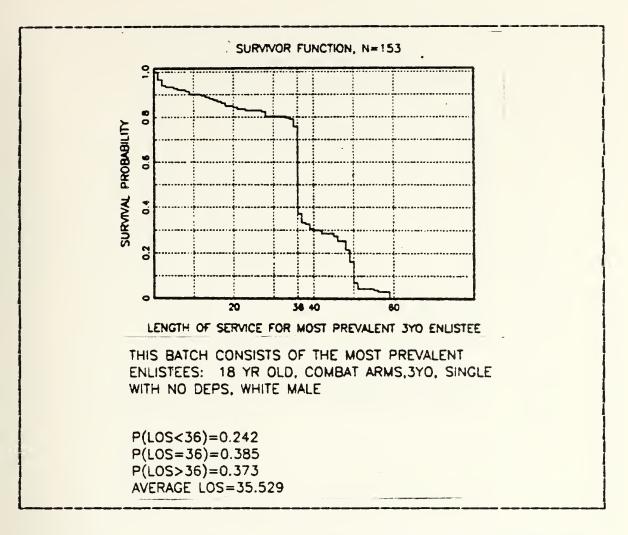


Figure 4.2 Survivor Function, Most Prevalent 3YO Enlistee

evident in the probability of reenlistment with the high-school-diploma graduates having the highest, followed by the NHSDG, then those with 2 years high school and then those enlistees with equivalency certificates. Again the GED enlistee is seen to be inferior to the non high school diploma graduate (NHSIG). Results of this survivor function analysis are in Table X in the following section.



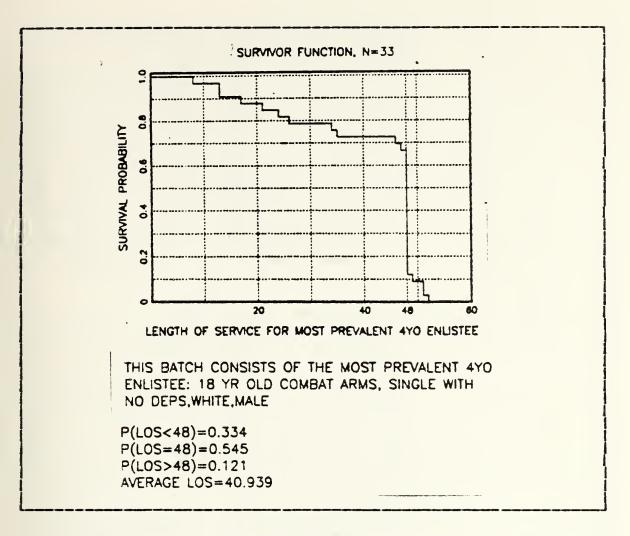


Figure 4.3 Survivor Function, Most Prevalent 4YO Enlistee

Resu	lts of Survi	TABLE IX vor Analysis on Enlistee	Most Prevale	nt
Term	P(attrite)	P(full term)	P(Reenlist)	Ave LOS
3 Years 4 Years	0.242 0.334	0.385 0.545	0.373 0.121	35.53 40.94



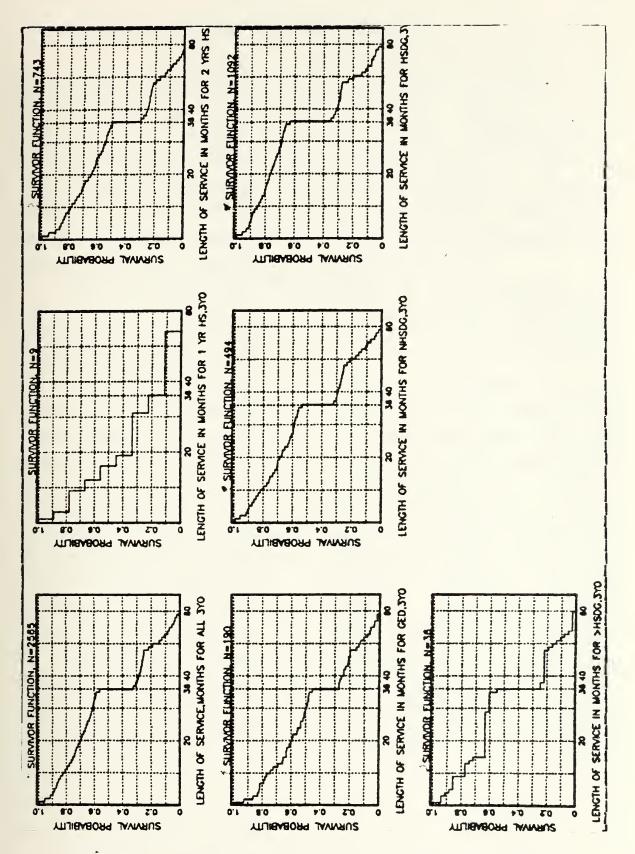


Figure 4.4 Survivor Functions of Education Levels



C. RESULTS OF SURVIVER FUNCTION ANALYSIS

Similar analyses were performed on the remaining six candidate explanatory variables for both the three year enlistees and for the four year enlistees. Actual survivor functions are found in Appendix K and L respectively. Tabular summaries are provided in Table X and XI. Based on these summary tables, the lowest risk attributes in terms of lowest probability of attrition are provided in Table XII. Those attributes that result in the highest probability of reenlistment are shown in Table XIV and Table XV.

The usefulness and simplicity of this approach is appealing for "quick and dirty" analyses in determining short term policy decisions concerning the characteristics desired for prospective soldiers.

Modeling of the survivor curves can provide further prediction capabilities and significance of each of covariates. However, the survivor functions presented all demonstrate the large "jump" at thirty-six and forty-eight for the three year and four year This large "discontinuity" tees, respectively. modelling of the survivor function to be somewhat difficult. Modelling of the survivor is discussed in great detail in [Ref. 19] and [Ref. 20]. The noted similarity in the survivor curves for all the variables under investigation suggest that the use cf a Cox proportional-hazards model may be appropriate: however more research is needed in modeling of the discrete jump in the survivor curve. [Ref. 20]. This analysis has been presented as an initial methodology to demonstrate its usefulness; no modelling will be rerformed.



TABLE X
Results of Survivor Function Analysis for 3YO

Variable F	(LCS<36)	P (LOS=36)	P (LOS>36)	Ave. LCS
All variables Education lvl	0.441	0.239	0.321	30.87
All variables Education 1v1 1 yr High Sch 2 yrs HS GED NHSDG	0.778 0.503 0.542 0.461 0.366 0.400	0.111 0.201 0.184 0.217 0.283 0.400	0.111 0.296 0.274 0.322 0.351 0.200	20.11 28.72 27.09 30.69 33.23 32.80
ESDG Ccllege Sex	0.366 0.400	0.283 0.400	0.351 0.200	33.23 32.80
Male Female Race	0.431 0.515	0.246 0.175	0.322 0.310	31.17 28.39
White Elack Cther Mental Cat	0.467 0.405 0.374	0.258 0.204 0.238	0.275 0.391 0.388	29.21 33.18 34.02
Cati Cat2 Cat3a Cat3b Cat4b Cat4b	0.357 0.401 0.356 0.457 0.449 0.468 0.443	0.214 0.294 0.320 0.225 0.230 0.222 0.193	0.429 0.305 0.324 0.318 0.321 0.310 0.364	33.57 31.85 32.40 30.42 29.86 30.80 32.57
Mar.Stat/No.Deps Single/0 Married/0 Married/1 Married/2 Married/3 Military Skill	0.441 C.448 0.563 0.381 0.333	0.252 0.083 0.000 0.095 0.083	0.307 0.469 0.437 0.524 0.583	30.62 32.92 30.19 36.76 42.00
13B 31M 64C 76Y	0.461 0.464 0.408 0.419 0.402 0.428	0.225 0.195 0.241 0.302 0.217 C.260	0.314 0.341 0.351 0.279 0.381 0.312	30.28 30.73 31.07 31.18 32.82 30.85
9 17 189 178 190 1223 1223 1223 1223 1223 1223 1223 123	912625560 939825560 94398625560 9449450 9445760 94554561 94554561 945560 94560	0.215 0.2566 0.22630 0.22566 0.1495 0.1218 0.075 0.150 0.150 0.150 0.238	0.294 0.3138 0.3386 0.2995 0.4210 0.4421 0.44586 0.44586 0.7138	291.0921 0.0921



TABLE XI
Results of Survivor Function Analysis for 440

Variable	P (ICS<48)	P (LOS=48)	P (LOS>48)	Ave. LCS
All variables Education lvl	0.441	0.239	0.321	30.87
Education lvl 1 yr High So 2 yrs HS 6ED NHSLG HSDG Ccllege	0.670 0.666 0.500 0.367 0.600	0.110 0.167 0.125 0.409 0.240	0.230 0.167 0.375 0.223 0.160	31.78 31.78 39.67 35.88 39.18 28.96
Male Female	0.391 0.667	0.389 0.000	0.220 0.333	38.29 37.00
Race White Elack Cther	0.387 0.424 0.307	0.389 0.288 0.500	0.220 0.288 0.193	37.74 39.36 39.42
Milte Elack Cther Mental Cat Cat1 Cat2 Cat3a Cat3b Cat4a Cat4b Cat4c	0.333 0.376 0.324 0.427 0.495	0.429 0.368 0.485 0.427 0.346 0.296	0.238 0.256 0.191 0.146 0.260 0.239	41.14 38.68 37.29 378.10 36.66
Mar.Stat/No.Description Single/0 Married/0 Married/1 Married/2 Military Skil	0.393 0.550	0.402 0.150	0.205 0.300	37.88 38.85
118 13B 31 M 64 C 76 Y	0.359	0.412 0.352	0.229 0.214 	39.43 36.73
94Ē Ag€				
A 9 17 189 2212 222 222 222 222 222 222 222 222 2	0.418 0.3357 0.7456 0.7456 0.6677 0.6677 0.50	0.436 0.429 0.431 0.018 0.394 0.238 0.040 0.050 0.125	0.145 0.222 0.216 0.185 0.151 0.286 0.298 0.275 0.353 0.375	866 • 522 • 99 • 170 • 170
> 30		••		



TABLE XII

Attribute Values Providing Lowest Risk of Attrition, 310

Variable Lowe	st F(attrition)	Next lowest P(attrition)
Education Level	HSIG	College
Sex	Mal€	Female
Race	Other	Black
Mental Cat.	3 A	1
Marital Stat/ No. of Deps	M/2	S/0
Ag€	28	19
MCS	76 Y	31.M

TABLE XIII

Attribute Values Providing Lowest Risk of Attrition, 410

Variable Lowe	st F(attrition)	Next lowest P(attrition)
Education Level	HSCG	NHSDG
Sex	Male	Female
Race	Other	White
Mental Cat.	31	1
Marital Stat/ No. of Deps	s/0	M/0
Ag€	18	19
MCS	11E	31M



TABLE XIV

Attribute Values Providing Highest Reenlistment, 3 YO

Variable	Lowest P (reenlist)	Next lowest P (reenlist)
Education Level	HSDG	NHSDG
Sex	Male	Female
Race	Black	Other
Mental Cat.	1	4C
Marital Stat	/ _{M/3}	M/2
Ag€	30	28
MCS	761	31M

TABLE XV
Attribute Values Froviding Highest Reenlistment, 4YO

Variable	Lowest P(reenlist)	Next lowest P (reenlist)
Education Level	NHSEG	2 yrs HS
Sex	Female	Male
Race	Black	White
Mental Cat.	4 A	2
Marital Stat	m/0	s/0
Ag€	26	25
MCS	11E	13B



V. RESULTS AND CONCLUSIONS

A. GENERAL

An intuitively pleasing, simple methodology was presented for the study of rerformance in the form of length of service of U.S Army enlistees. Some Exploratory Data Analysis techniques were demonstrated through the use of the IBM GRAFSTAT data analysis package. The interactive carabilities of the rackage and the APL language were exploited to provide a means of rapidly manipulating and observing the selected data. The tools proposed, the draftsman's displays, boxplots and survivor functions, were used on actual cohort data from the Defense Manpower Data Center.

Several possible explanatory variables and their association with performance were presented based on the Exploratory Data Analysis. Confirmatory analysis was performed to support the Exploratory Data Analysis. Probabilities of enlistee attrition and reenlistment were provided using a survivor function analysis for each of the candidate explanatory variables. Attributes that presented the highest risk of attrition and the highest probability were presented.

B. SUMMARY

The increasing cost of "assessing, dressing and training" today's Army enlistee coupled with the diminishing supply of 17-21 year old prospective enlistees have prompted research effort toward gaining insight into those personal attributes that produce the most successful soldier in terms of first term completion. The basis for understanding the relationships of these personal attributes and for using this



understanding in recruiting policy lies in the ability to rapidly analyze the available data on current enlistees and to present the analysis in a form that is understandable and useful for the decision maker.

This thesis has presented a broadly applicable and simple methodology, using Exploratory Data Analysis through the interactive capability of the IBM GRAFSTAT package and the AFL language, for defining the area of analysis, identifying errors in the data, reducing the dimensionality of the problem, and determining relevant association of personal characteristics of enlistees to performance. The honds tetween Exploratory Lata Analysis and more classical statistical analysis were demonstrated. Use of survivor function analysis provided statistics on chosen explanatory variables, indicating the importance of these characteristics.

The further application of the methods in this thesis and cf Exploratory Data Analysis in general should increase the practitioner's ability to make sound decisions regarding future manpower planning issues. With the increased availability cf graphics-capable personal computers, Exploratory Lata Analysis is relevant at all levels of decision making.

C. RECOMMENDED FURTEER RESEARCH

The following items deem further research:

1. A comparison of Exploratory Analysis techniques in this theses to other data analysis packages such as those available in BMDF and SAS (see [Ref. 17] and [Ref. 21]) would be useful in determining advantages and disadvantages of the different approaches in variable selection and error identification. In particular, the Cox proportional hazards model in the BMDP program r2l [Ref. 17: pp. 576-594] uses a stepwise approach to identify important explanatory



variables and estimates the survivor as well as the hazard function for further analysis. Note however that models such as this Cox proportional hazards model for estimating the effect of concomitants on survival curves are not applicable because of jumps in the survival functions at known times. More research is needed to determine how to apply the model to such a function with this large discrete jump.

- 2. The Graduate Equivalency Degree programs offered throughout the United States need to be analyzed in detail for standards used in awarding the certificates. The wide variance and the poorer performance of the GED holders indicate that non-high-school-diploma graduates should be treated separately in any analysis, contrary to the popular grouping of the two categories. Perhaps different GED levels would provide insight into future performance at least as well as the different levels of high school status have.
- 3. The trends and probabilities have been presented as a methodology on only a 10 percent sample of the data: comparisons of these cutcomes to other data sets would be useful in the determination of prediction possibilities.
- 4. Modeling of the survivor curves would provide a detailed account of the actual contribution of each explanatory variables using multivariate regression techniques. Again further research is needed in the applications of modeling techniques to survivor curves with the noticeable jumps at known times.



APPENDIX A EXPLORATORY DATA ANALYSIS TECHNIQUES

Exploratory Data Analysis techniques are usually first attributed to John W. Tukey in his book by that title [Ref. 22]. Exploratory Data Analysis for the purposes of this thesis will be defined as "the activity of examining data, both graphically and through numerical summaries, for the purpose of revealing properties of the data itself, and with luck, of the processes giving rise to that data." [Ref. 23: p. 2]. Thus EDA techniques can be thought cf as "informal " techniques to examine the data pricr "formal", more classical analysis techniques, in crder to prevent needless calculations irrelevant to the investigation at hand. Quite often more can be learned about the data in this initial, informal look at the data. Chambers et. al. prints cut, graphical EDA methods are perhaps most effective in the initial glance at the data to limit the scope of the investigation to only those variables that are pertinent [Ref. 12]. These graphical methods allow the investigator to rapidly synthesize information, more efficient and intuitive manner perhaps than through methods available in commercial statistical packages that produce tabular data.

Cne particular method of multivariate analysis is the multidimensional array of scatter plots called a "generalized draftsman's display" of the data [Ref. 12: pp. 136,145]. An example display is seen in Figure A.1 This figure demonstrates how the pairwise scatter plots are arranged so that "any adjacent pair of plots have an axis in common" [Ref. 12: p. 145]. All variables of interest, then, for the entire data set can be displayed as the first phase of



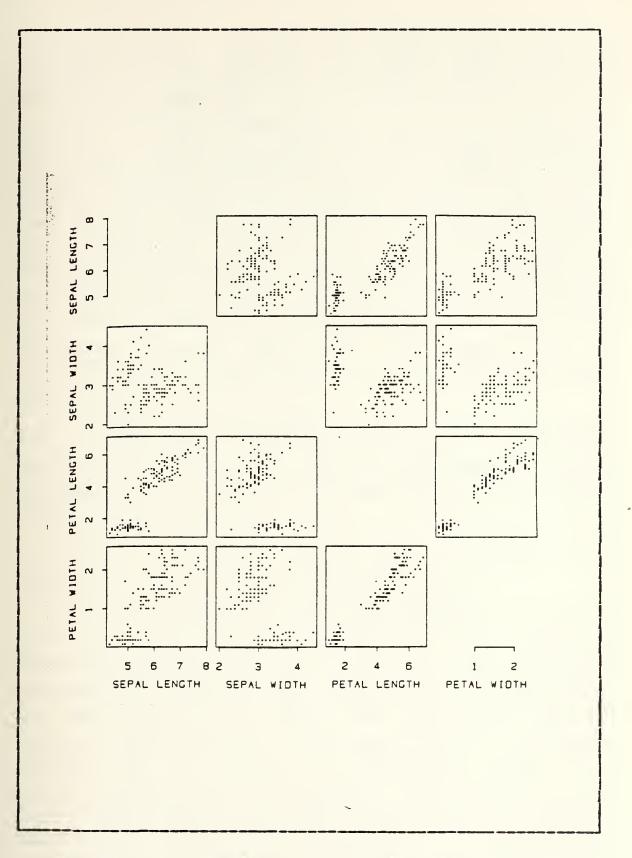


Figure A.1 Draftsman Display from Chambers et. al.



the investigation. Then one can rapidly and effectively determine if trends exist and for which specific pairwise association of variables.

Captain Malcolm Johnson, a student of Operations Research at the Naval Postgraduate School, has developed an APL program called "draftsman" that is imbedded in IBM's GRAFSTAT package on the school's computer system (See [Ref. 24: pp. 13-17]. for information on use of GRAFSTAT) that organizes any data set into a draftsman's display. This program also allows for transformations of the data and for jittering of the data. His efforts have been published as a Master's thesis that includes a tutorial for use of the "draftsman" program. [Ref. 13]. This program will be utilized in the initial phase of the data analysis efforts of this thesis.

Cf course, the draftsman's display is only the first step cf the analysis. If trends are evident, then further analysis should be performed utilizing more formal confirmatory analysis to verify any graphically-determined associations among the variables.

The use of boxplcts is another EDA technique that is very useful in "taking an initial look" at the data. The boxplct is a "simple method of summarization".

The upper and lower quartiles are depicted by the "hody" of the box, the median is portrayed by a line, circle or other distinguishing mark as is the mean. Upper and lower adjacents are depicted at the end of lines extending from the body of the box. These terms are defined as the "largest observation that is less than or equal to the upper quartile plus 1.5 times the interquartile range, and smallest observation that is greater than or equal to the lower quartile minus 1.5 times the interquartile range," respectively. Values that fall outside the range of adjacent values are called outside values. These are plotted as



individual roints. See Figure A.2 for a depiction of the components of the boxplot.

The hoxplot provides a rapid "impression" of the distritution of the data. The median, mean, and spread are all obvious. The length of the lines to the adjacent values demonstrate the "stretch" of the tails of the distribution. The individual points for the cutside values allows the user of the plot to consider "outliers" although not every outside value is an outlier.

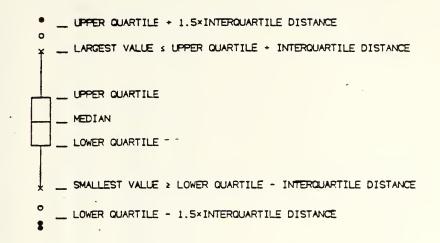
The figure also allows for some determination of the symmetry of the distribution of the data, simply by viewing the symmetry of the bcdy of the box about the median line or dot.

These plots are useful when it is not feasible or necessary to capture all the details of a distribution, or when many distributions need be compared. The width of the box has no significance.

An excellent discussion of these and other EDA techniques is found in [Ref. 12], from which this description of boxplots was taken.



SAMPLE BOX PLOT PLOT OF 50 POINTS



, INTERQUARTILE DISTANCE = UPPER QUARTILE - LOWER QUARTILE

Example box plot for fifty data points from a regenerative simulation. The interquartile distance equals the estimated upper quartile minus the estimated lower quartile. The light circles are data points which fall between the largest value less than or equal to the upper quartile plus the interquartile distance and the upper quartile plus 1.5 times the interquartile distance. The dark circles are data with values above this latter point. Similarly for the lower part of the box plot.

Figure A.2 Example Boxplot



APPENDIX B
HISTOGRAM OF FY79 NHSG ASSESSIONS

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	227	3.5	5334	42.0						
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	1 2	3.0 3.0	5435	42.						
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APPENDIX C FORTRAN PROGRAMS TO READ DATA



```
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C MENT.

//DTHOMAS JCE (1972,037E), 'O.THOMAS', CLASS=B

//#MAIN ORG=NPVMI.1972F

// EXEC FCRIXCD

INTEGER*4 SSAN1, SSAN2, SSAN3,

** TAFMC, HYECO, PGO, MSO, CEPT, ETSYO, ETSMO, CHSVO,

** REG, TAFMS, HYECS, POS, MSS, TEPS, ETSYS, ETSMS, CHSVS,

** RES, TAFML, HYECL, PGL, MSS, TEPS, ETSYS, ETSMS, CHSVS,

** ETSYL, ETSML, CHSVL, KEL

INTEGER*4 DANK/' '/, NINE/' -y'/

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DEPULETSMU,ETSMC,CASVC,REU,
TAFMS,HYECS,PGS,MSS,LEPS,ETSYS,ETSMS,CASVS,RES,
TAFML,HYECL,PGL,MSL,LEPL,ETSYL,ETSML,LASVL,REL
                                       С
              300
              100
    /#
//GC.FT O1F O01 DE JAIT=3230V, VUL=SER=MS0282, DISP=(ULU),
// DCB=(RECFM=FB, LKECL=326, BLKSIZE=12714),
// DSNAME=MS3.S1972.CFT79
//GO.FT O2F O01 DD JAIT=3350, VCL=SER=MVS0U4, DISP=(SAR),
                                                SPACE = (CYL, (+,4)), DCB= (RECFM=FB,LK &CL=90,0LKS)ZE=19000),
DSNAME=S1972.079A
```





```
C
//DTHOMAS JGE (1972,039E), "D.THOMAS", CLASS=6
//#MAIN ORG=NPGVM1.1972F
// EXEC FCRIXCG
//FORT.SYSIN DD #

INTEGER*4 SSAN1, SSAN2, SSAN3,
# CENK, CEND, ZIP1, ZIP2, HOK, FECIL, TF, AF CTP, APTA, APTB, APTG, AP
                                                                                                                                                                                                                                              APIG
APIH
APIJ
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                  c
                                                                                                                                                 REAC(1,100) SSAN1,SSAN2,SSAN3,
CENR,CEND,ZIP1,ZIP2,HOR,
RECIL,TF,AFQTP,APTA,APTE,
APTC,APTJ,APTE,APTE,
APTG,APTH,APTI,APTJ,APTK,
APTL,APTK,APTN,APTJ,APTF
                       C #RITE(2,200) SSAN1, SSAN2, SSAN3,

# CENR, CENO, ZIP1, ZIP2, HUR,

# RECIC, TF, AFCTP, APTH, APTH,

# APTC, APTO, APTH, APTH,

# APTC, APTH, APTH, APTH,

# APTC, APTH, APTH, APTH,

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# A
                  C
                    /*
//GC.FT 01F 001 DE UNIT=3330V, VUL=SER=M3U 282, U15P=(DLD),
// DCB=(RECFM=FB,LKECL=320,BLKS1ZE=1271+),
// JSNAM6=MSS.S1472.CF179
//GO.FT 02F001 DD UNIT=3330V, VLL=SEK=MV3004,DISP=(SHR),
// SPACE=(CYL,(4,4)),CCB=(RECFM=FB.LK.CCL=85,BLKS1ZE=190+0),
                                                                                                          DSNAME=$1972.279C
```

97



APPENDIX D APL PROGFAMS FOR DATA MANIPULATION

```
VSTRIP2[0]V
       ♥ STRIP2
       TAFMO+DPAFT1[;1]
[1]
       HYECO+DRAFT1[;2]
523
[3]
        FGO+DRAFT1[;3]
       MSO+DRAFT1[;4]
[4]
       DEFO+DRAFT1[;5]
[5]
       CHSVO+DRAFT1[;6]
[6]
[7]
       REO+DRAFT1[;7]
       AGEE+DRAFT1[;8]
[8]
[9]
       HYEC+DRAFT1[;9]
[9] HYEC+DRAFT1[;9]
[10] SEX+DRAFT1[;10]
[11] FACE+DRAFT1[;11]
[12] ETH+DRAFT1[;12]
[13] MS+DRAFT1[;13]
[14] AFOTTG+DRAFT1[;14]
[15] MOS+DRAFT1[;15]
[16] A+DRAFT2[;2]
[17] F+DRAFT2[;3]
[18] C+DEAFT3[;4]
[19] D+DEAFT3[
       vRECODE[0]v
v RECODE DATA;C;D;NCODE;TSTOF;RIATA
       Derinsert the COLUMN TO BE RECORD!
[1]
[3]
       0+0
       De'INSERT THE DIGITS TO BE RECODED!
[4]
       D ← D
[5]
       DE'INSERT THE NUMBER TO BE RECODED TO
       HCODE+0
[5]
       TSTOR + DATA
[7]
[3]
       DATA[;C]+DATA[;C]=D
      DATA[;C]+DATA[;C]xNCODE
F 9 7
[10] FDATA+DATA
      RDATA[;C]+PDATA[;C]+TSTOR[;C]x(RDATA[;C];MCODE)
[11]
[12]
      REDATA+RDATA
[13] OF THE RECODED DATA IS NOW A SLOBAL VARIABLE CALLED REDATA!
```



```
VAVESCAN[ [] V
     ▼ REAVESCAN ARRAT; C1; C2; A; VAL; V
[1]
    ATHIS FUNCTION CHOOSES A SUBSET OF AN ARRAY AND
    ACALCULATES THE MEAN OF THAT SUBSET
[2]
     DE'INSERT THE COLUMN NUMBER OF THE SELECTION VECTOR!
[3]
     C1+0
[4]
     VEARRAY[;C1]
[5]
     DE'INSERT THE COLUMN NUMBER OF OF THE VAR YOU WANT AVERAGED!
[63
[7]
     92+□
     ACARRAY[;C2]
[8]
     OF THE PESIFED SELECTION VALUE FOR THE SEL VECTOR
[9]
[10]
     VAL+D
     SEL+(V=VAL)/A
[11]
[12] Detthe Subset that you have selected is stored as global variable
      SEL'
[13] De'THE AVERAGE OF YOUR SELECTED PERSONNEL IS:
[14]
    R+(+/5EL)+(F5EL)
      OCOLAT[0]
      O COLAT
[1]
      PRAFT1+A79[;2],A79[;3],A79[;4],A79[;5],A79[;6],A79[;9],A79[;10]
E33
      DRAFT1+DRAFT1, 279[;2], 279[;3], 279[;4], 279[;5], 279[;6], 279[;8]
      DRAFT1+DRAFT1,879[;9],879[;19]
[4]
      PRAFT2+A79[;2],979[;9],979[;10],979[;11],979[;12],979[;13],979[;14
[5]
      DRAFT2+DRAFT2,C79C;151,C79C;161,C79C;171,C79C;181,C79C;191,C79C;20
      DRAFT2+DRAFT2, C79[;21], C79[;22], C79[;23], C79[;24]
[63
      DRAFT1+4(15 3078 fDRAFT1)
[7]
      DRAFT2+0(17 3078 FDRAFT2)
[8]
        THATPLD[0]T
       WATRLD
      ABUILDS MATRIX FOR USE IN ANOVA TESTING IN CHAPTER 3
 [1]
       [2]
 [3]
       MATR← 1543 5 FROW
 [4]
       MATE[;1]+GED,(196+MATE[;1])
       MATRE;23+HSDG
 [5]
 [6]
       MATR[;3]+NHSG,(503+MATR[;3])
 [7]
       MATR[;4]+JR,(751+MATR[;4])
 [8]
       MATR[;5]+SOPH,(10+MATR[;5])
```

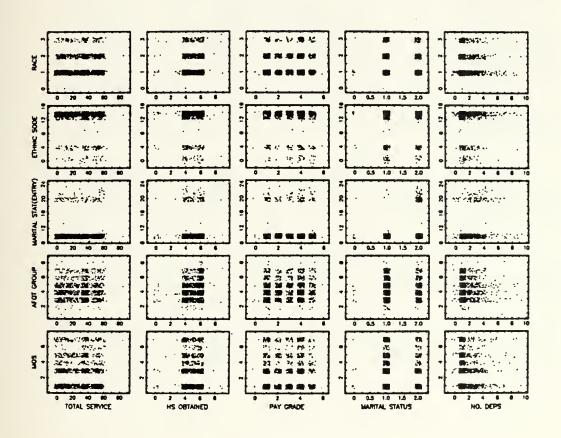
99



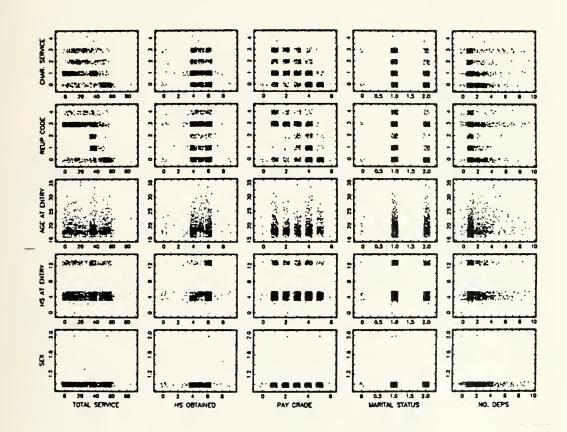
```
PREC[[]]
      ♥ P+PRC DATA; DATA1; 5EL; MEQ36; MLT36; MGT36; EQ36; LT36; GT36; FEQ36; FLT3
        5; PGT36
[1] ACALCULATES REL, FRER (PROBABILITY) FOR SURVIVAL ANALYSIS.
     DETCHECK TO SEE IF THIS FN IS SET UP FOR 36 OF 48 TO
021
      AVESCAN DATA
[3]
[4]
     DATA1+SEL
     HER48+FER48+(DATA1=48)/DATA1
[5]
     NLT48+9LT48+(DATA1 (48) / DATA1
[6]
[7]
     MGT48+FGT36+(DATA1,48)/DATA1
[8]
      P2+FER48+NER48+FSEL
      F1+FLT48+NLT48+F5EL
F97
     F3+PGT48+NGT48+F5EL
[10]
     DETVECTOR OF PROBABILITIES:P(LOS(48),F(LOS=48),F(LOS)48)
[11]
[12]
     P+F1,P2,F3
        ♥TO4MKE[[]]♥
       C TOAMER DATA
     ABUILDS MATRIX OF 4YO ONLY DATA, DATA IS ORIGINAL
 [1]
 [2]
     ADATA SET.
       Y04+DATA[;11]=4
 [3]
      NDATA4+ 479 10 F(1 1 1 1 1 1 1 1 1 1)
 [4]
      MDATA4[;13+Y04/DATA[;1]
 [5]
      HDATA4[;2]+Y04/DATA[;2]
 [6]
 [7]
      NDATA4[;3]+Y04/DATA[;3]
      NDATA4[;4]+YO4/DATA[;4]
 [8]
      MDATA4[;5]+Y04/DATA[;5]
 [97
 [10] NDATA4[;6]+Y04/DATA[;6]
 [11] NDATA4[;7]+Y04/DATA[;7]
[12] MDATA4[;8]+Y04/DATA[;8]
[13] MDATA4[;9]+Y04/DATA[;9]
[14] .HDATA4[;10]+Y04/DATA[;10]
        △YOZMKE[[]]√
      D TOJMKE DATA
 [1] ABUILDS MATRIX OF 3YO ONLY DATA, 'DATA' IS ORIGINAL
 [2]
     RIATA SET
 [3]
       Y03+DATA[;11]=3
      HDATA+ 2565 10 f(1 1 1 1 1 1 1 1 1 1)
 [4]
      NDATA[;1]+Y03/DATA[;1]
 [5]
      NDATA[;2]+TO3/DATA[;2]
 [6]
      [E;]ATAG\EOT+[E;]ATAGH
 [7]
      HDATA[;4]+103/DATA[;4]
 [8]
 [9]
      HDATA[;5]+TO3/DATA[;5]
 [10] NDATA[;6]+103/DATA[;6]
 [11] NDATA[;7]+Y03/DATA[;7]
 E12] MDATA[;8]+r03/DATA[;8]
E13] MDATA[;9]+r03/DATA[;9]
[14] HDATAC;10]+T03/DATAC;10]
```



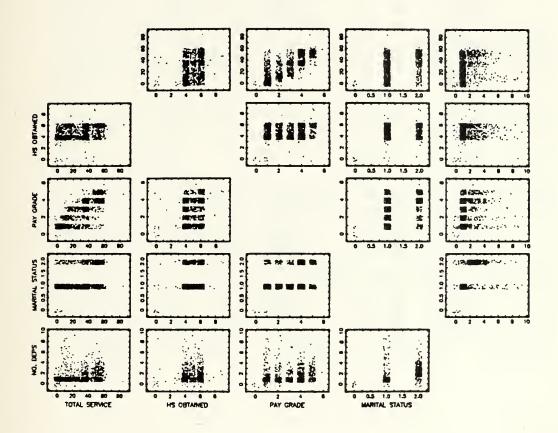
APPENDIX E OVERALL VIEW OF FIRST DRAFTSMAN'S DISPLAY



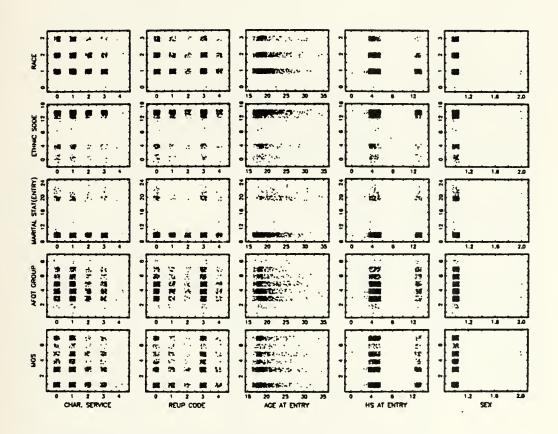




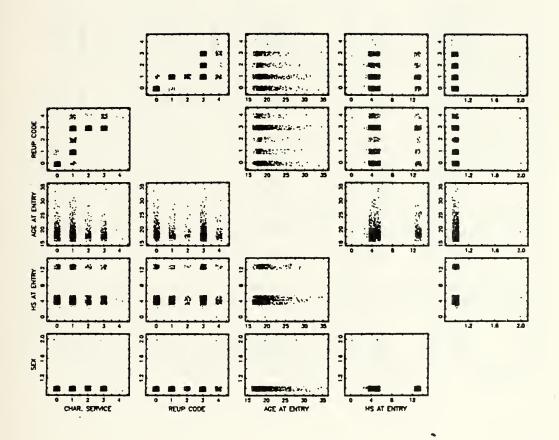




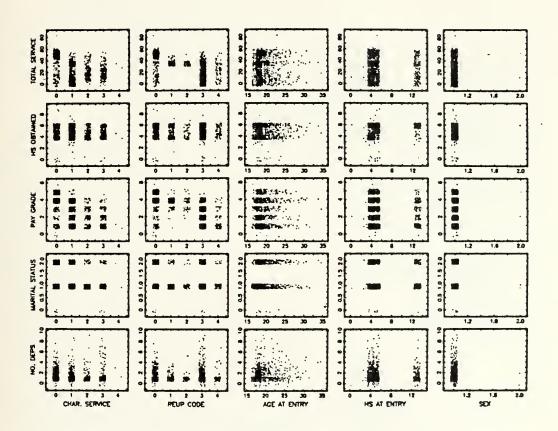




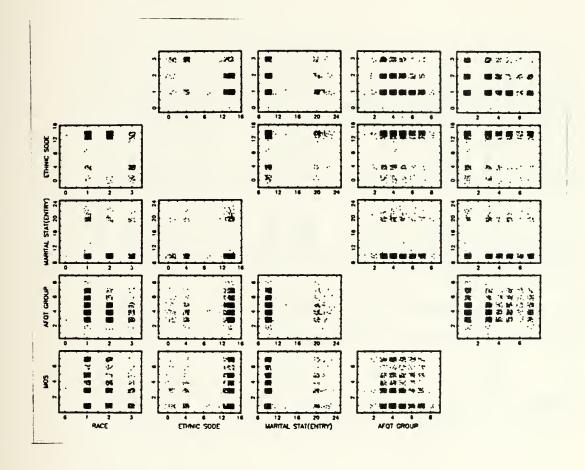




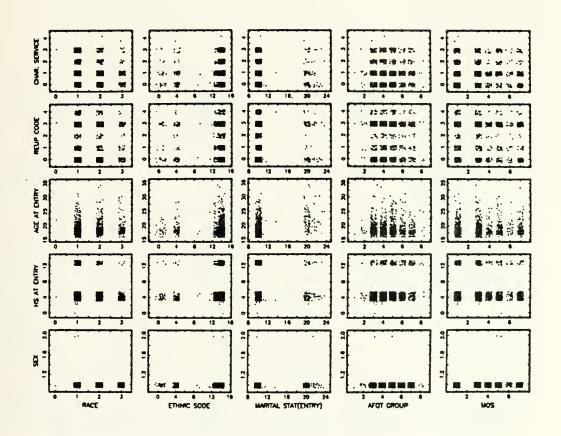




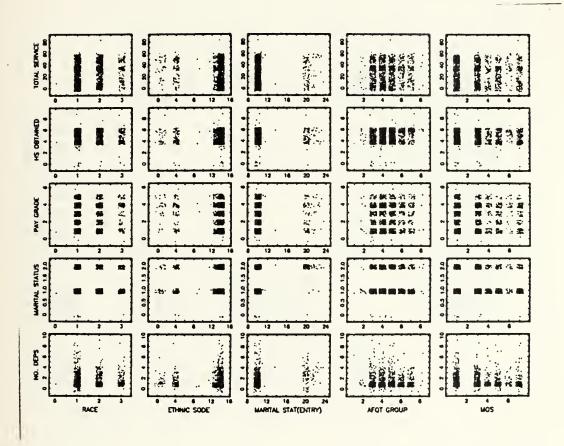






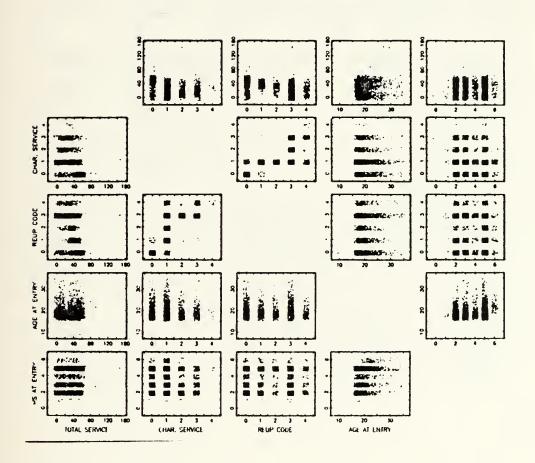




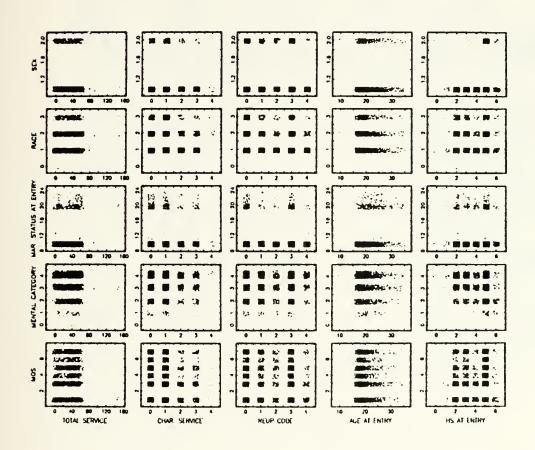




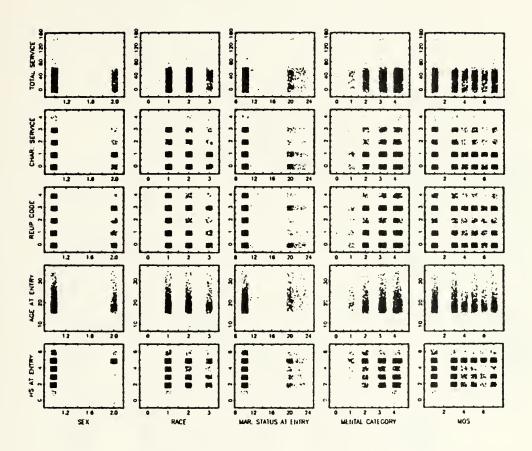
APPENDIX F CVERALL VIEW CF REVISED DRAFSTMAN'S DISPLAY



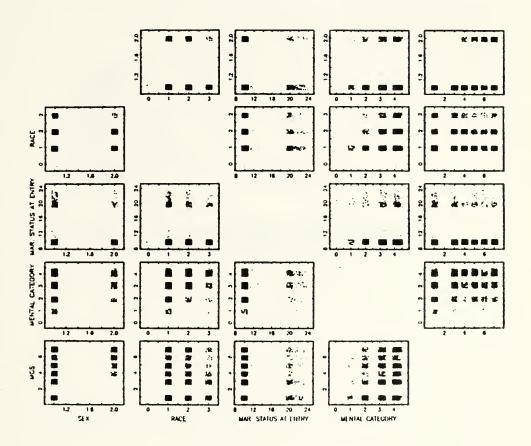














APPENDIX G INPUT SCREEN, IEM GRAFSTAT SUBPOPULATION CATEGORY ANALYSIS

CATEGORY MALLYSIS

CATEGORY VECTOR : C
Y VARIABLE : Y
UNNETCHED (0) OR WEIGHTS : 0

PERCENTILES (OR BOX) : BOX
SYMBOLS DEFINED (Y/N) : N
PLOT HEADER (IN QUOTES) : A

SCREEN HEADER (IN QUOTES) : A

SCREEN HEADER (IN QUOTES) : A
PLOT POSITION ! TABLE POSITION:
SCALE X-AXIS LABEL (IN X-OTES) : A
PLOT POSITION ! SCALE X-AXIS LIN
PARTIAL PLOT 1 1 1 1
AXES AND GRID CONTROL 0 1 0 0

PROGBAM

ENTER-GO PF: LOHELP 2-WIEW GRAPHICS (3279) 3-RETURN A-MPITE ON SCREEN CLEMB-DEFAIL? SHLAST RESPONSES 6-KRASE 7-PROFILE 8-UNDEFINED RESPONSES 9-OUTPUT 10-STORE/RETRIEVE 11-INTO APL 12-SCREEN DISPLAY



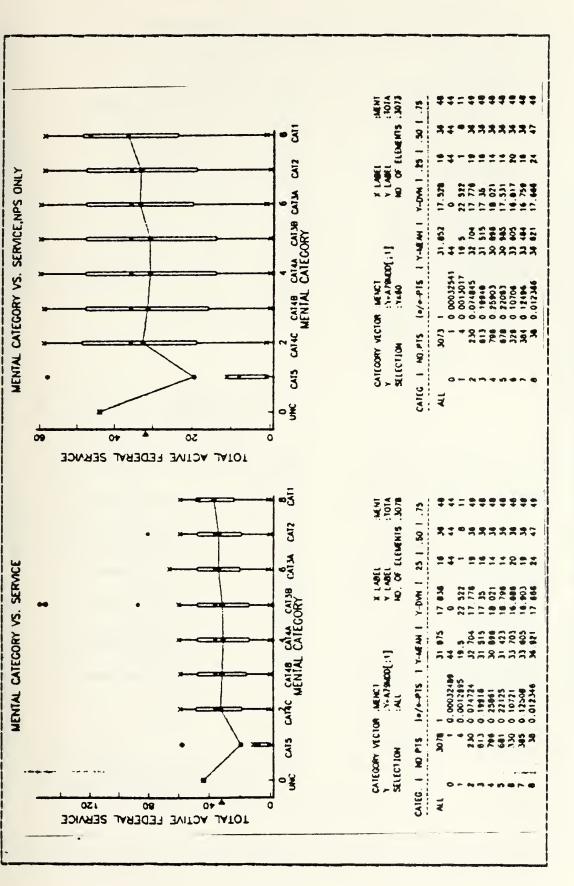
APPENDIX H BOXPLOT ANALYSIS CF REMAINING VARIABLES

Boxplots of the remaining candidate explanatory variables versus length of service are provided in this appendix. Refer to Chapter 3, pages 62 through 66 for discussion on each of these boxplots. Remaining candidate explanatory variables displayed in this appendix are listed in Table XVI

TABLE XVI Candidate Explanatory Variables

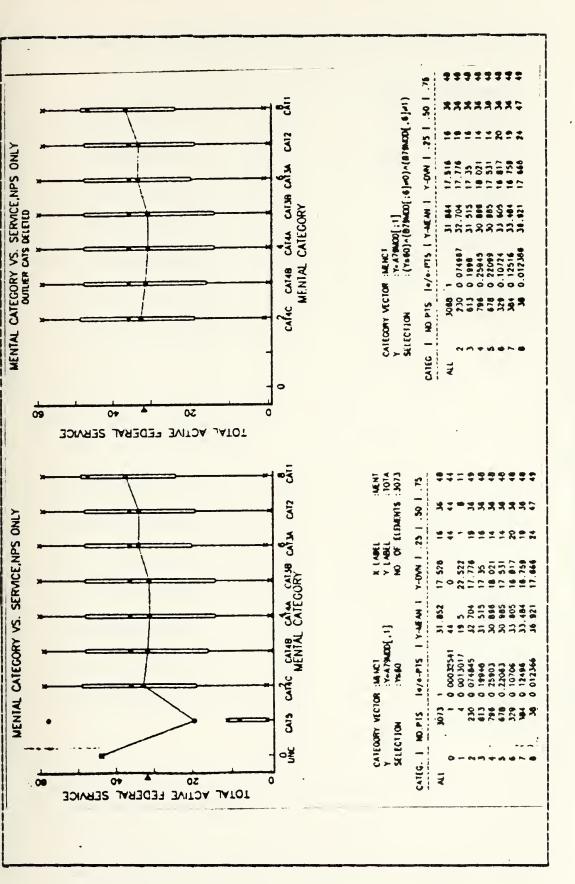
Mental Category
Marital Status
Age
Sex
Race
Reenlistment Code
Character of Service





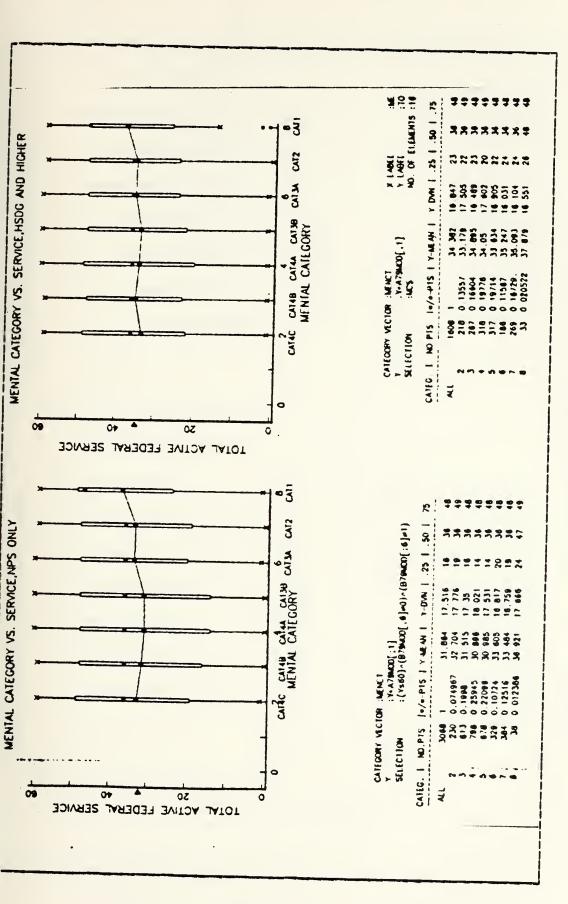
Length of Service, I Mental Category vs. Figure





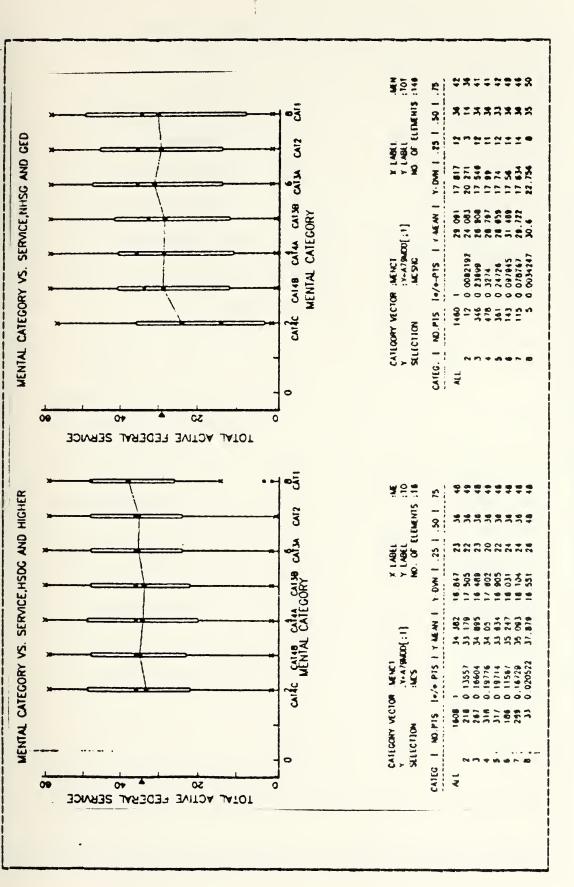
Service, II Length of Category vs. Mental H.2 Figure





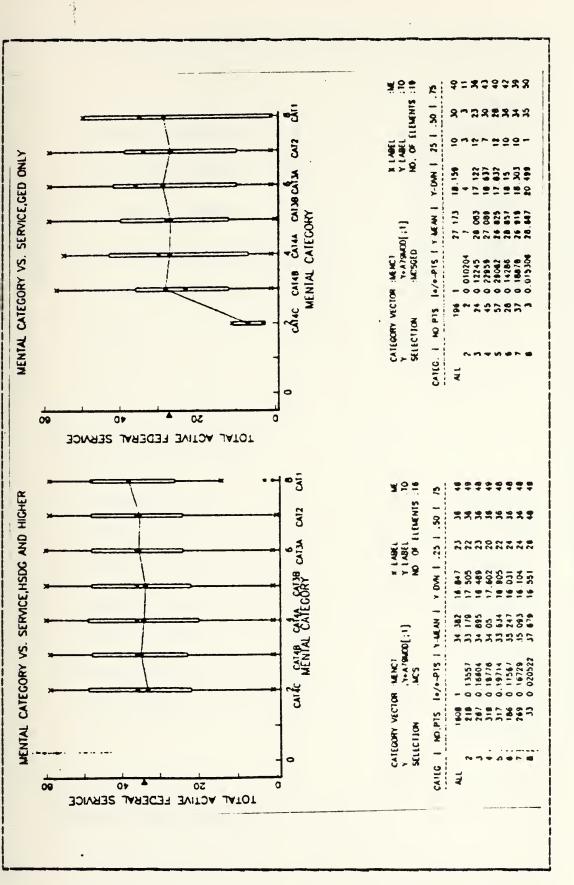
Service, III of Length Mental Category vs. H. 3 Figure





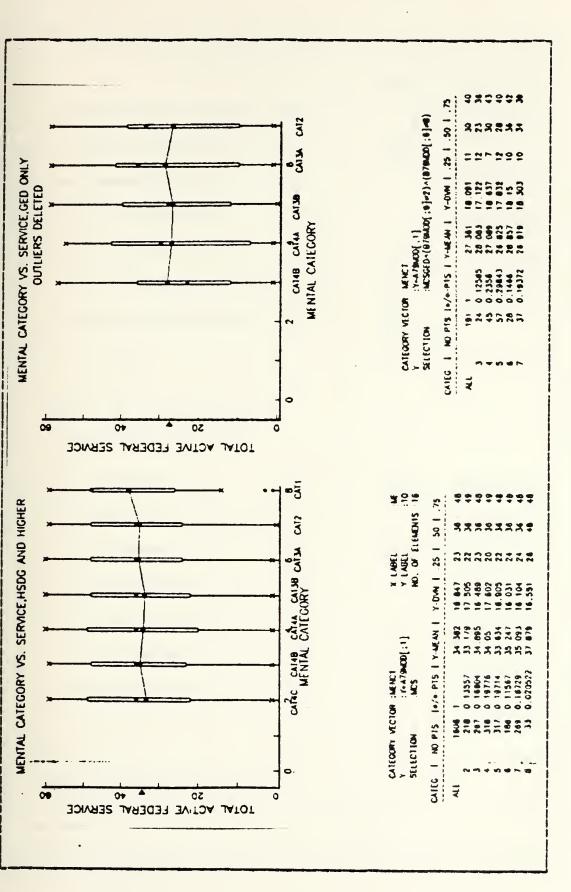
Service, IV of Length VS. Mental Category H. 4 Figure





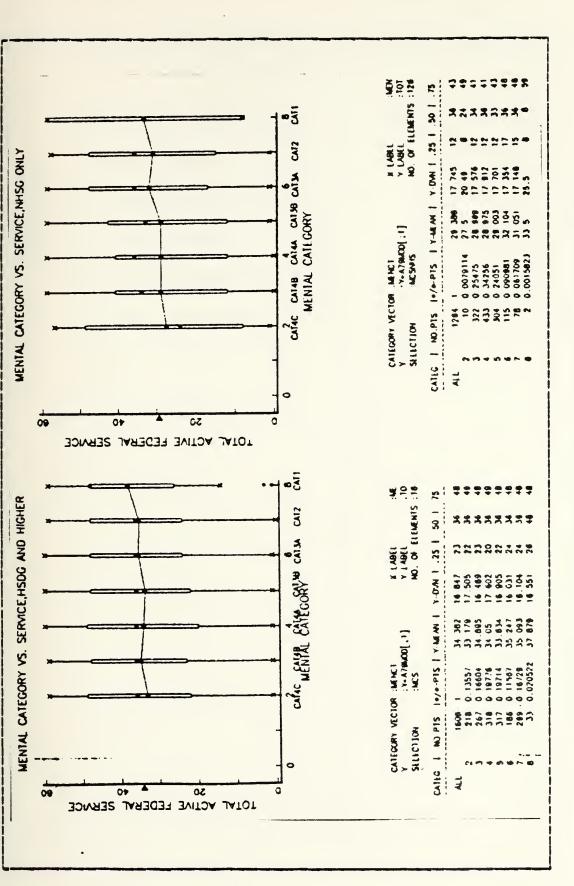
Mental Category vs. Length of Service, V H.5 Figure





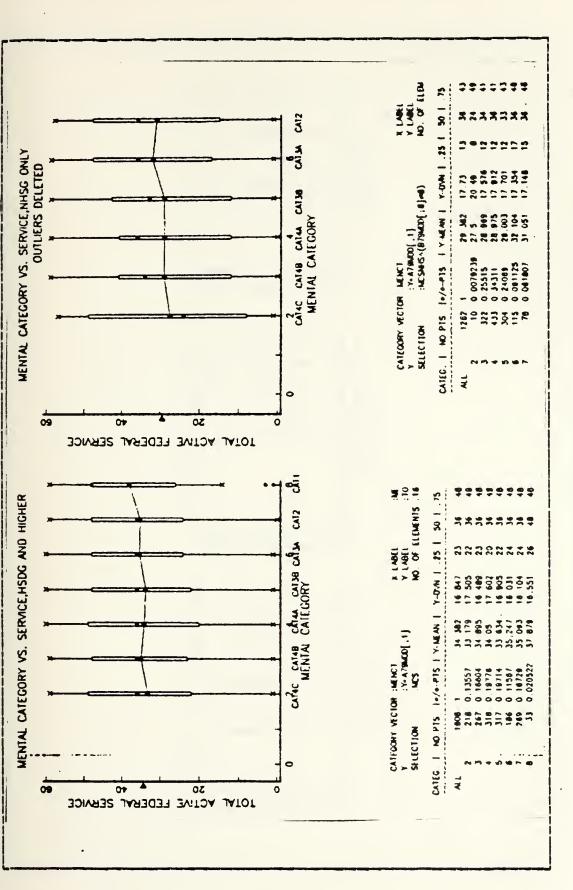
Mental Category vs. Length of Service, VI H.6 Figure





Service, VII of Length Mental Category vs. Figure





Service, VIII cf Length Mental Category vs. H. 8 Figure



Mental Category vs. Length of Service, IX Figure H.9



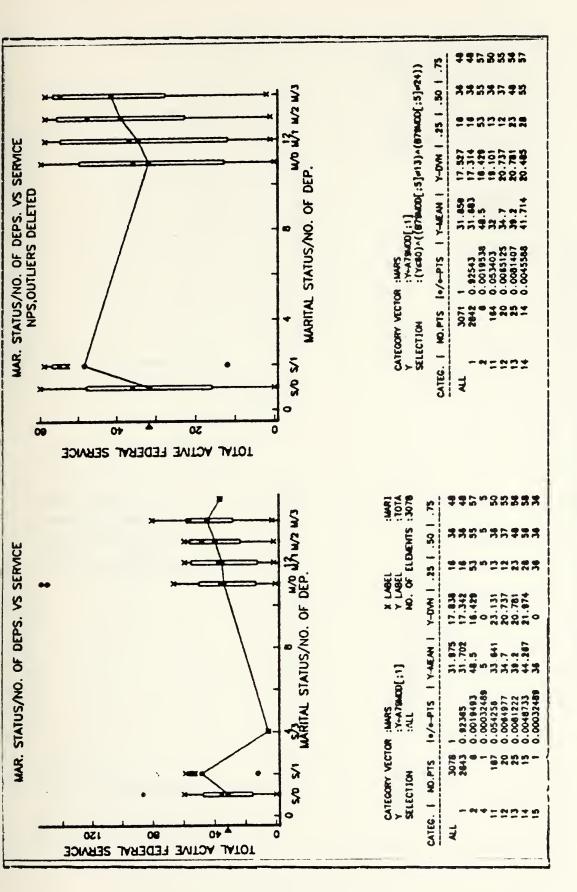


Figure H.10 Marital Status vs. Service,I



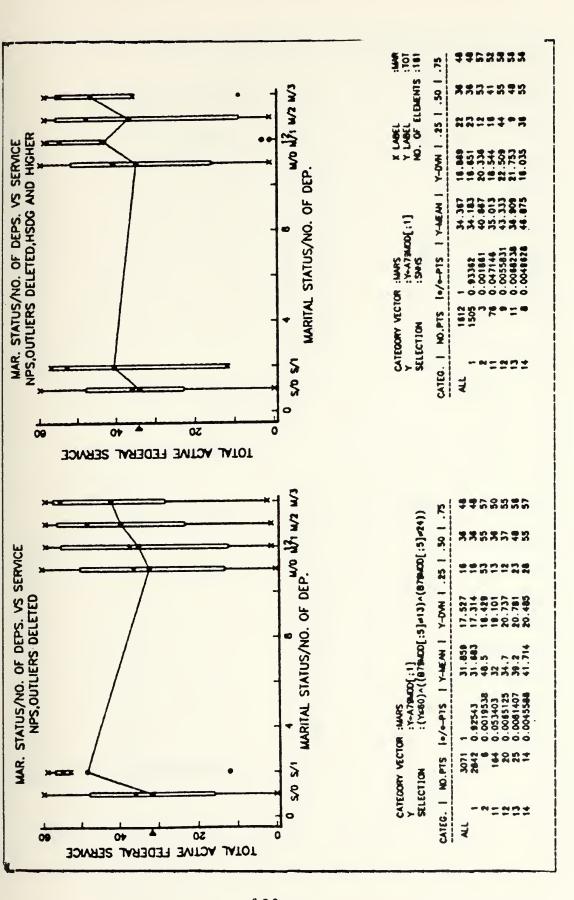


Figure H. 11 Marital Status vs. Service, II



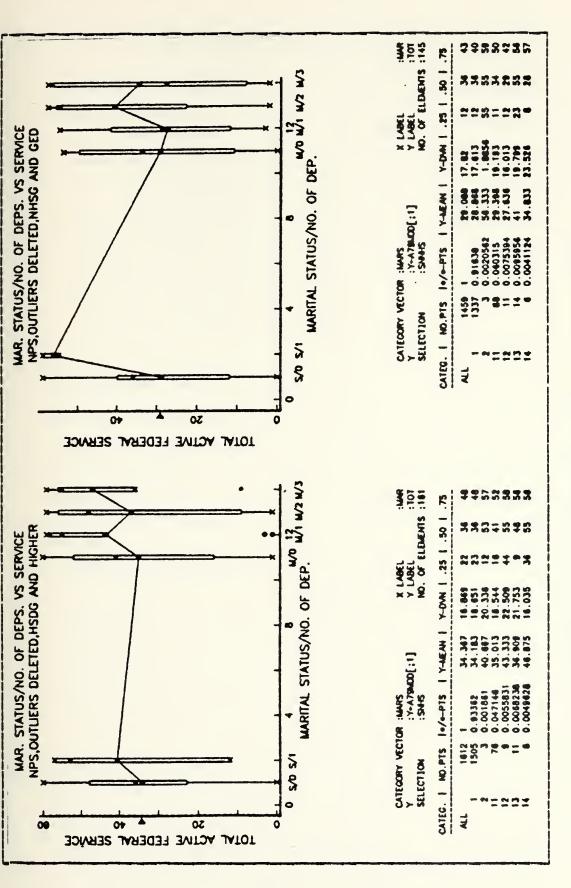


Figure H.12 Marital Status vs. Service, III



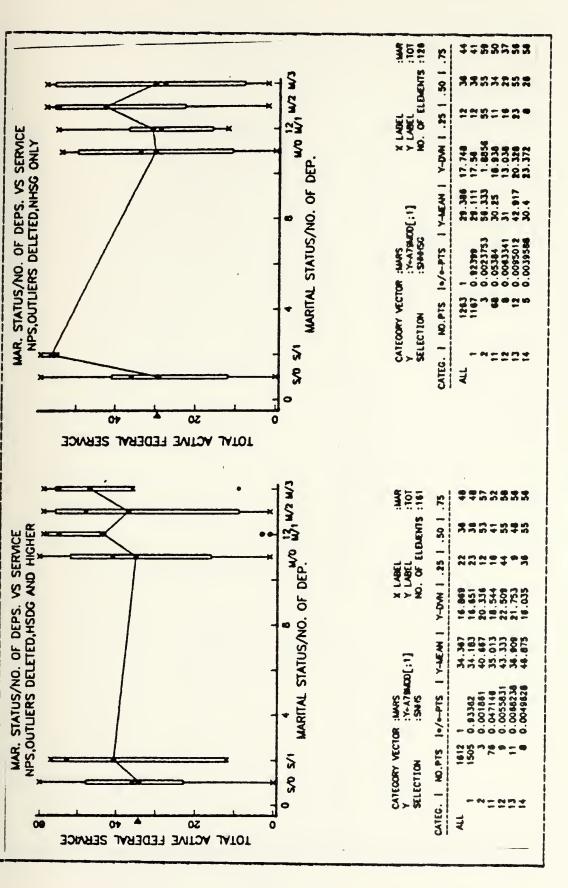


Figure H. 13 Marital Status vs. Service, IV



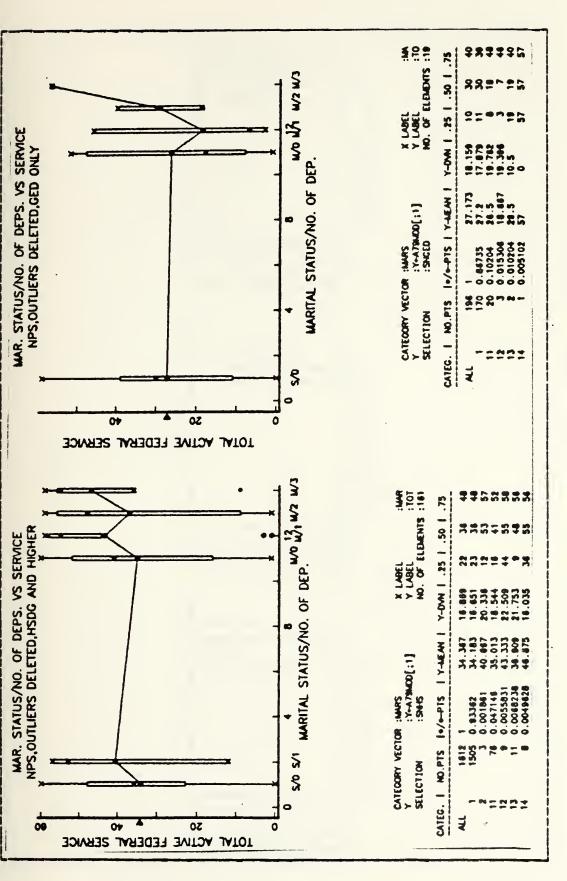


Figure H. 14 Marital Status vs. Service, V



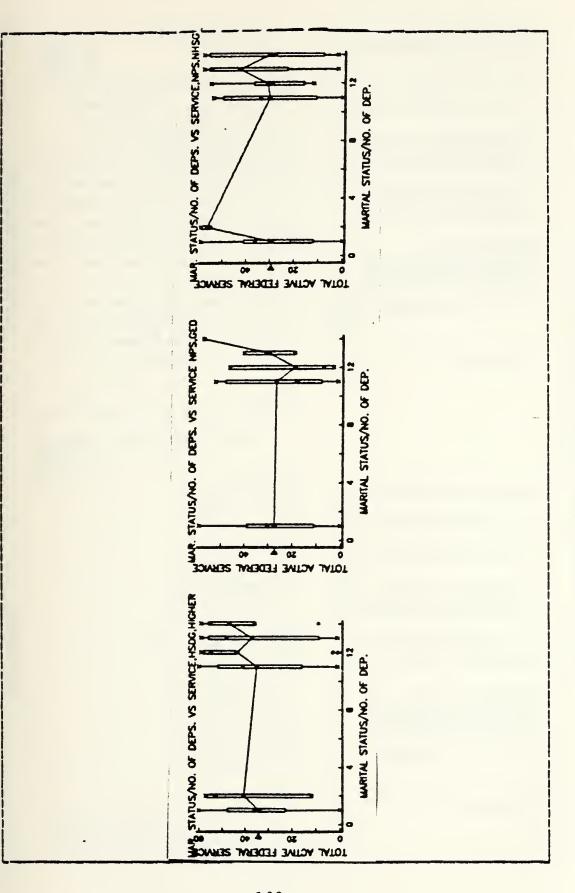


Figure H.15 Marital Status vs. Service, VI

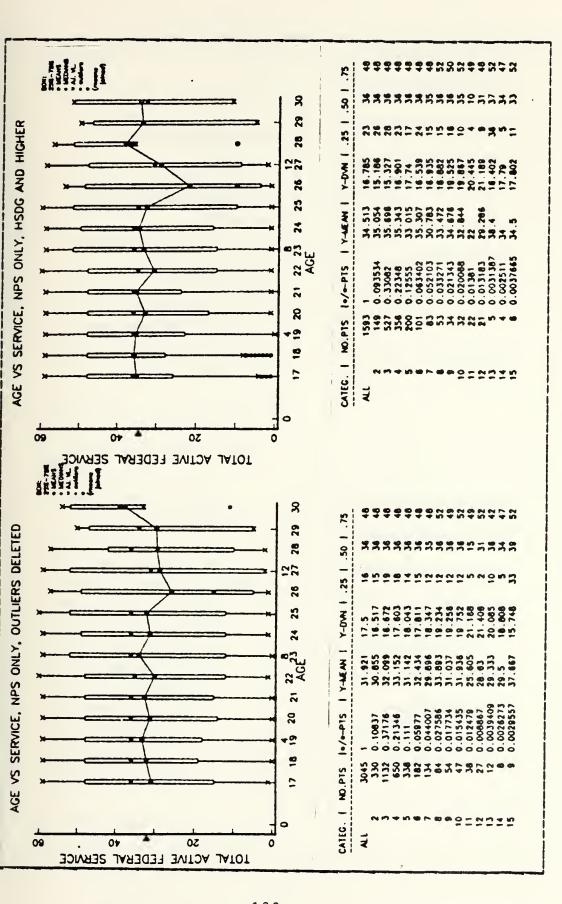


Figure H.16 Age vs, Service, I



Pigure H. 17 Age vs. Service, II





Pigure H. 18 Age vs. Service, III



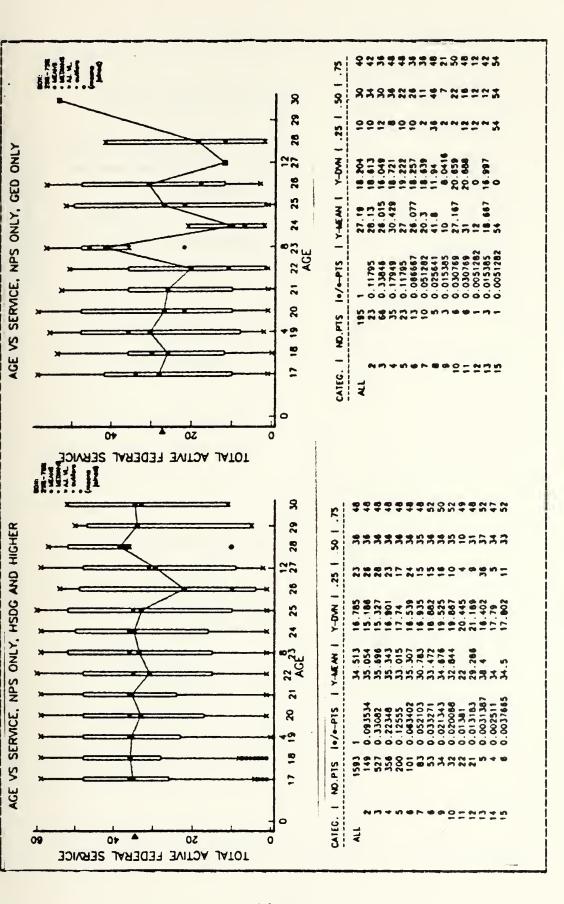


Figure H. 19 Age vs. Service, IV



Figure H.20 Age vs. Service, V



Figure H. 21 Age vs. Service, VI



Figure H.22 Age vs. Service, VII



Figure H.23 Age vs. Service, VIII



Pigure H. 24 Age vs. Service, IX



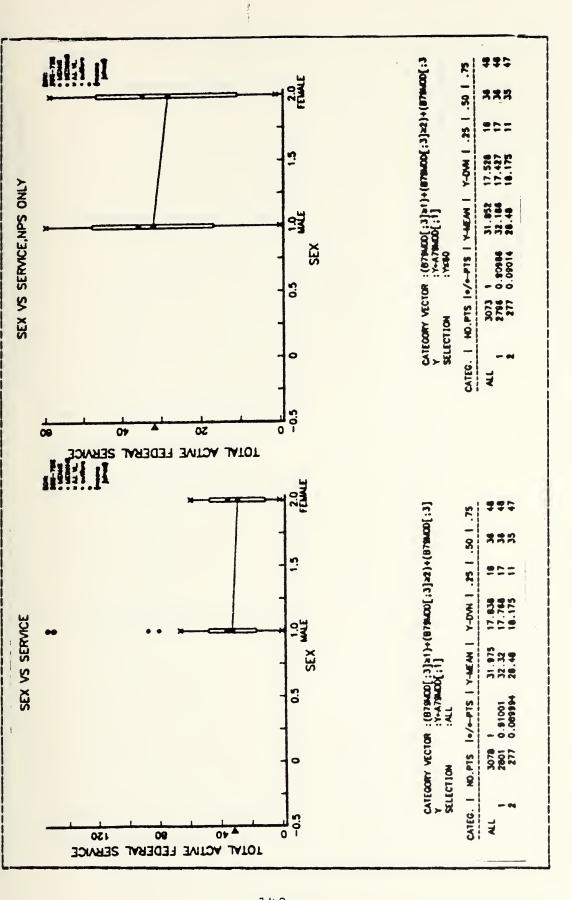


Figure H.25 Sex vs. Service, I



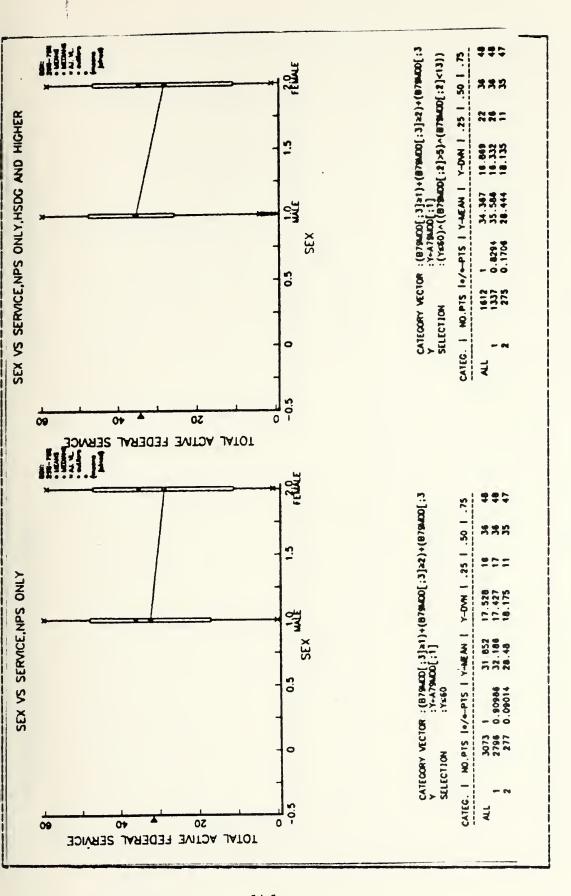


Figure H.26 Sex vs. Service, II



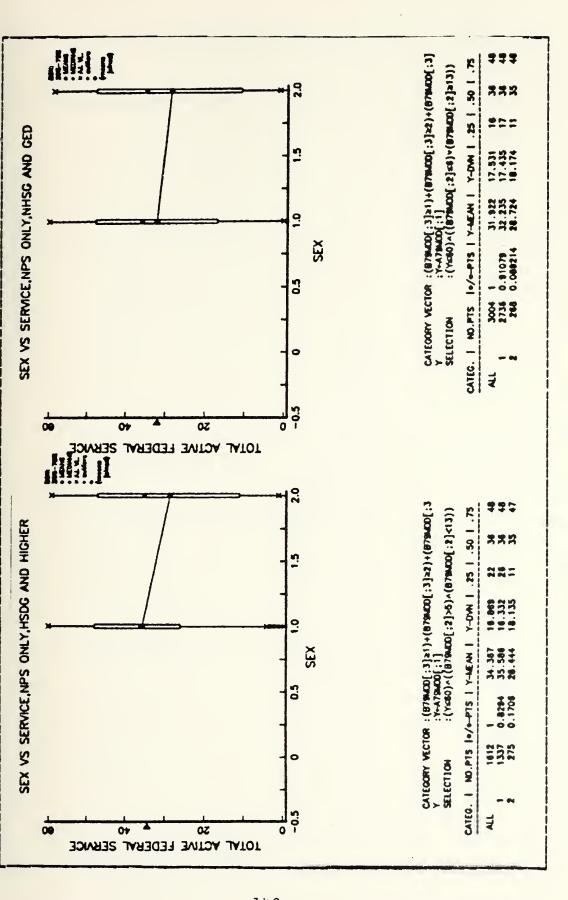


Figure H. 27 Sex vs. Service, III



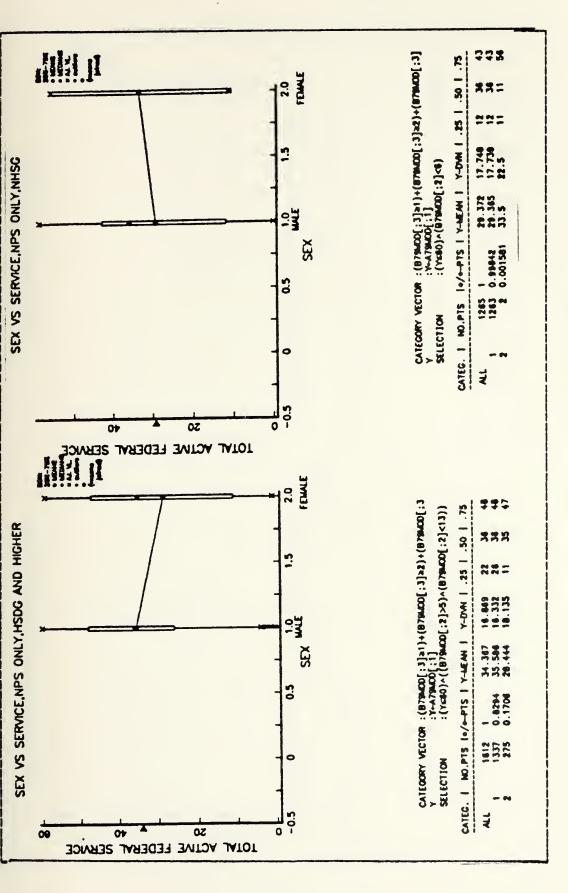


Figure H.28 Sex vs. Service, IV



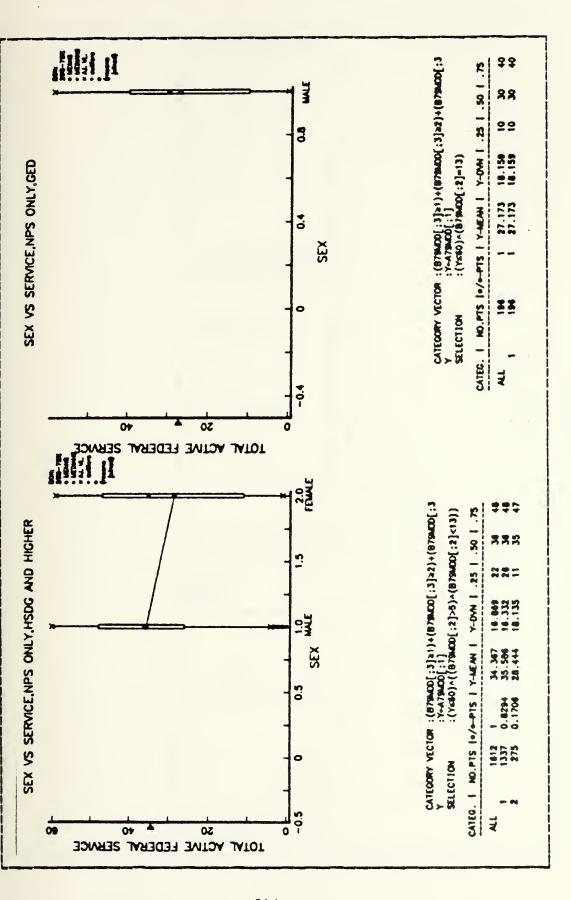


Figure H.29 Sex vs. Service, V



Figure H.30 Sex vs. Service, VI



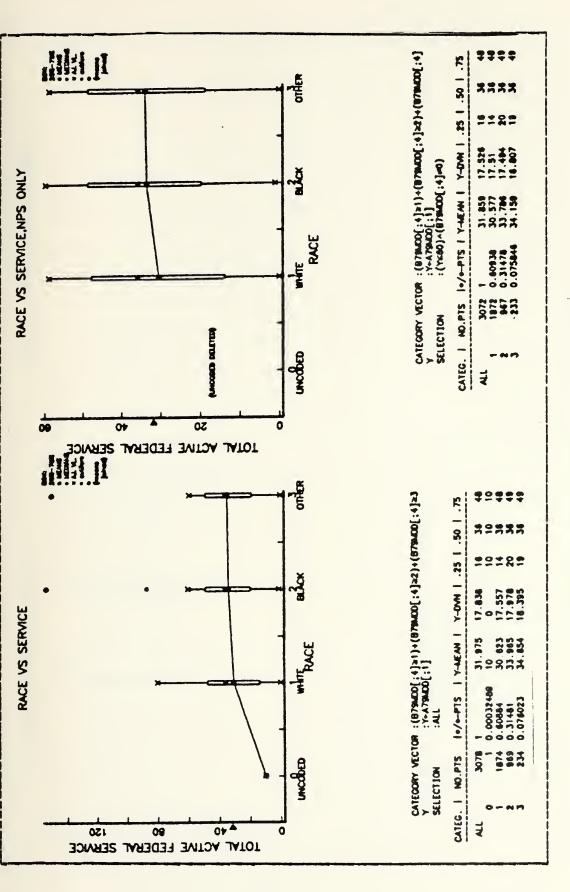


Figure H. 31 Race vs. Service, I



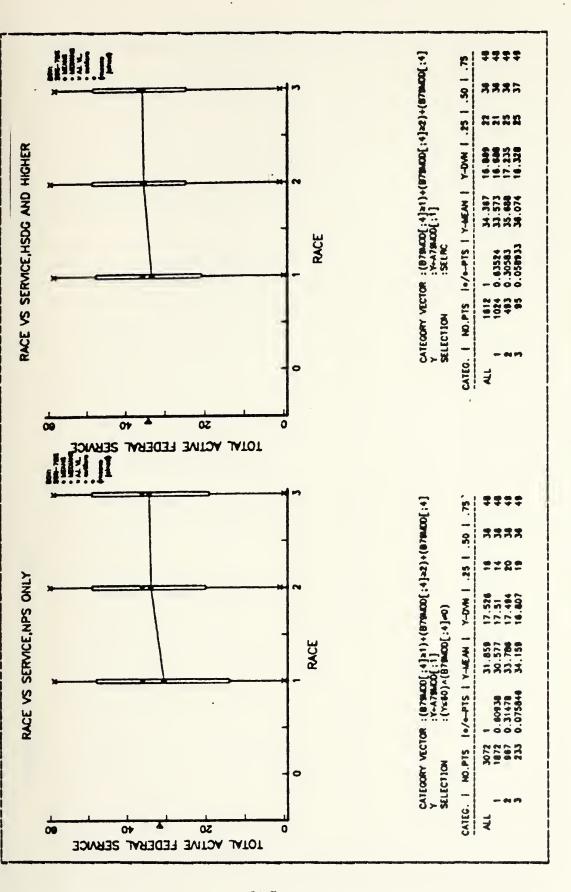


Figure H. 32 Race vs. Service, II



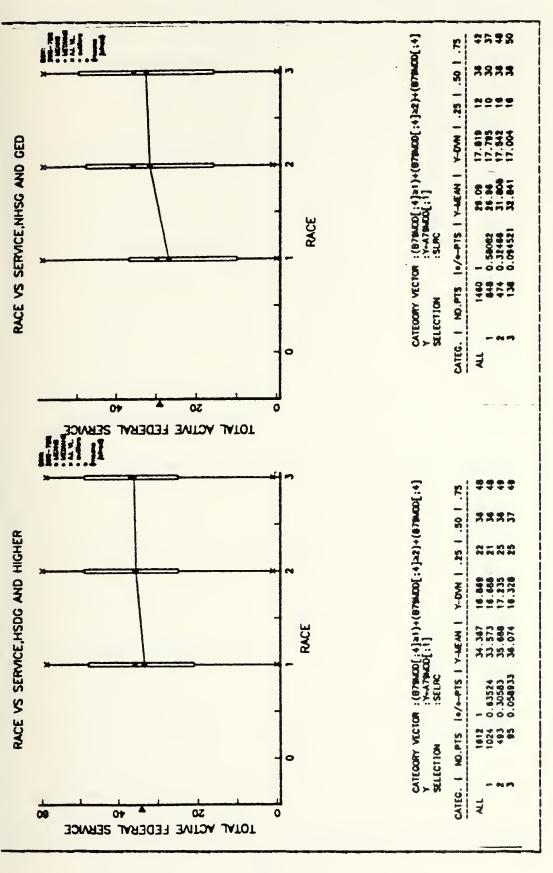
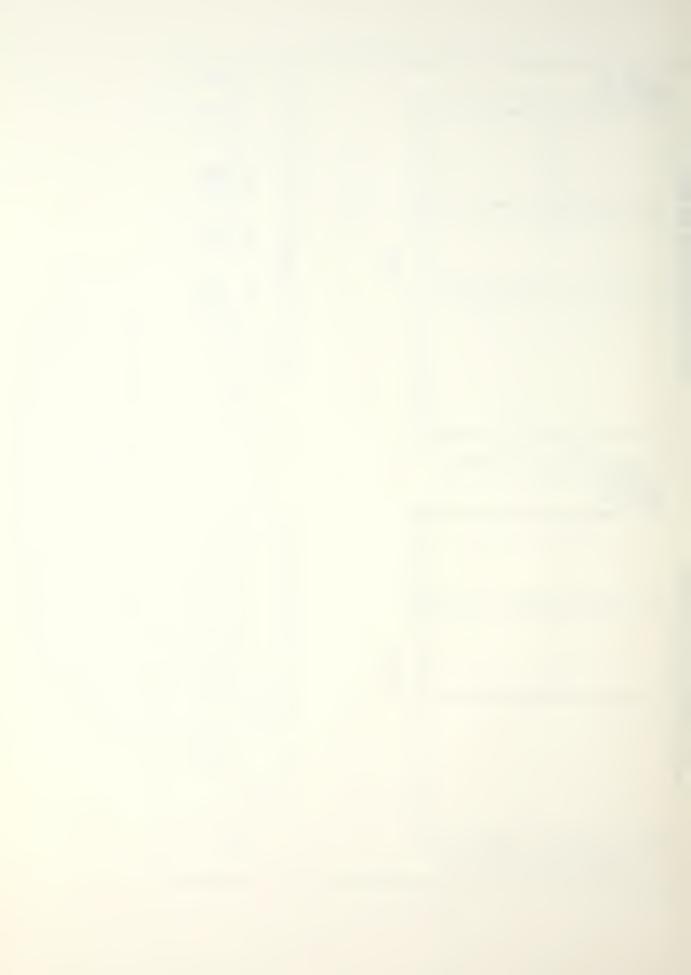


Figure H.33 Race vs. Service, III



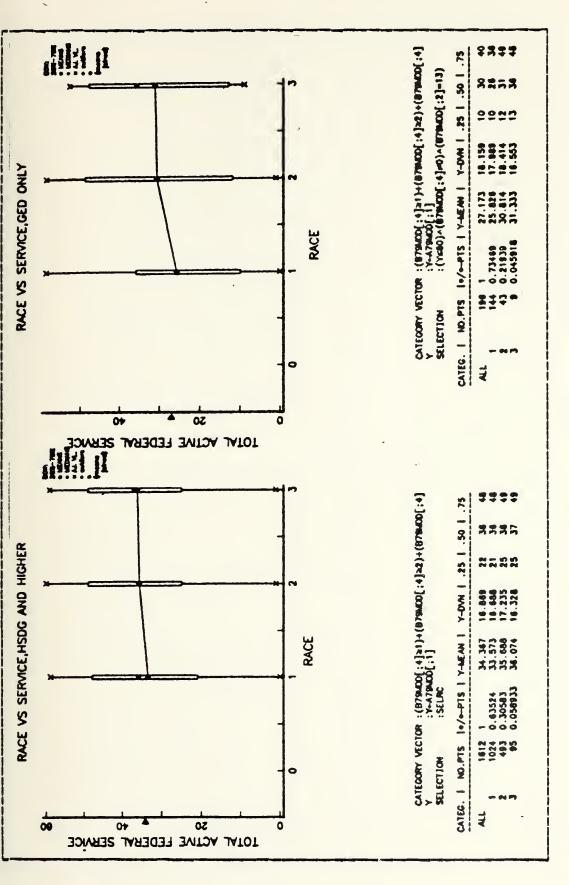
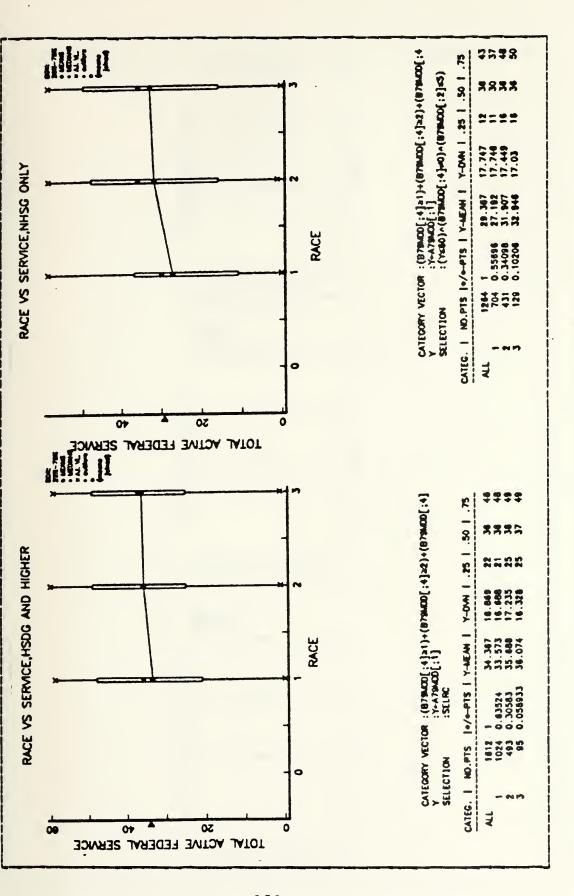


Figure H. 34 Race vs. Service, IV



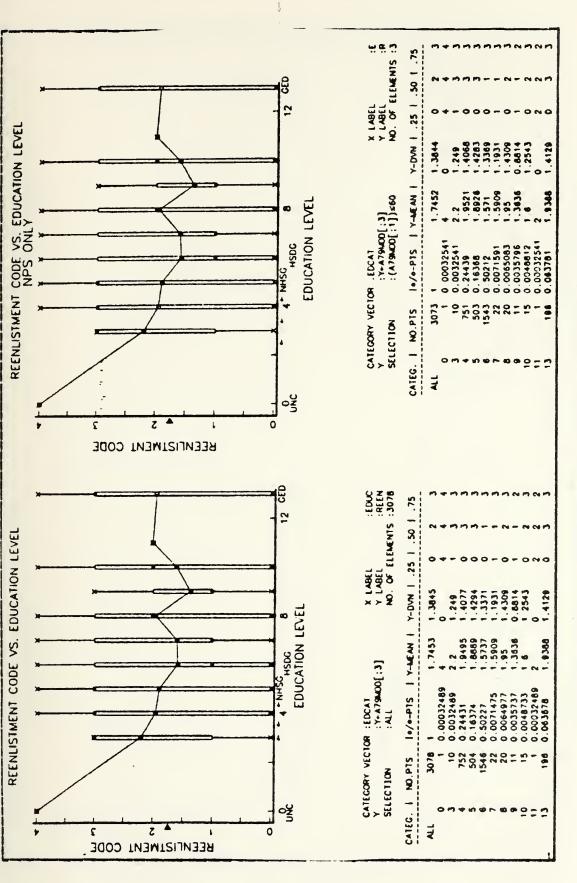


Pigure H. 35 Race vs. Service, V



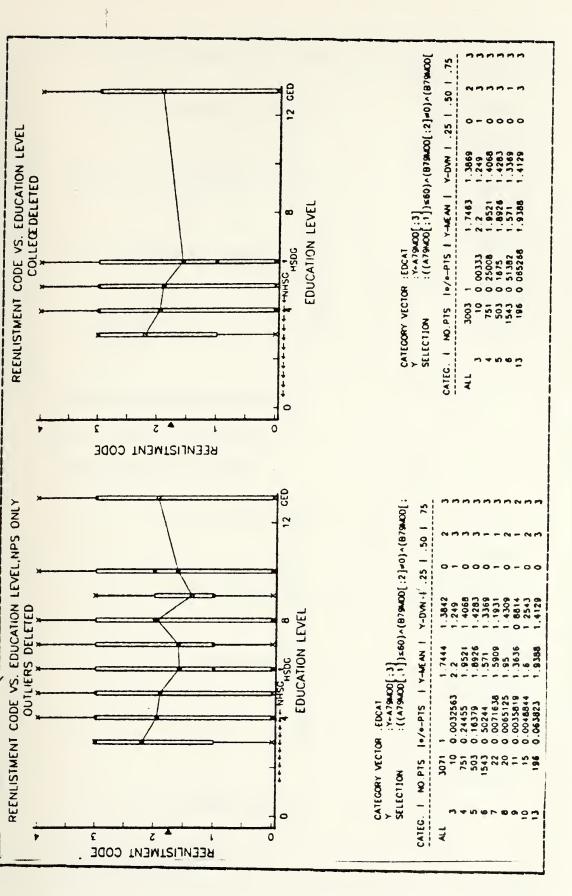
Figure H. 36 Race vs. Service, VI





Education Level, I Reenlistment Code ws. H.37 Pigure





Education Level, II Reenlistment Code vs. Figure H.38



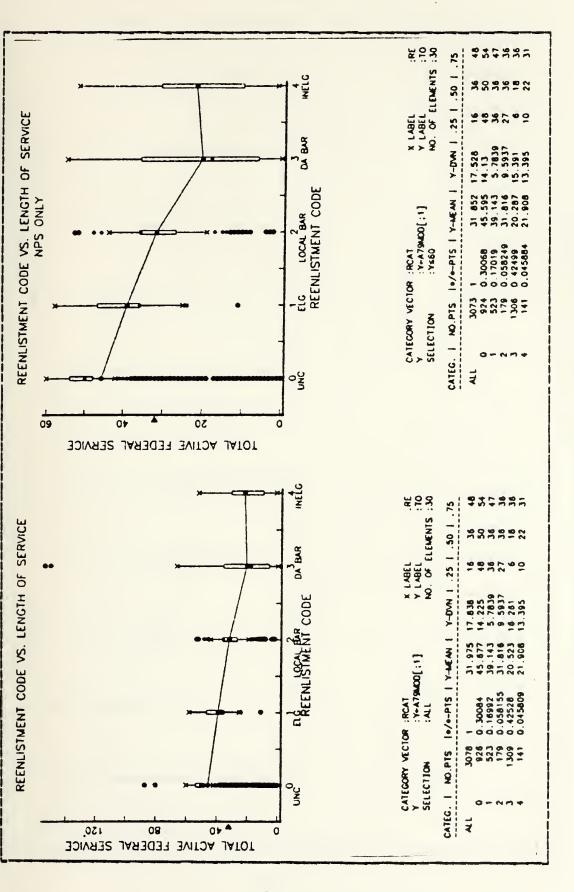


Figure H.39 Reenlistment Code vs. Service, I



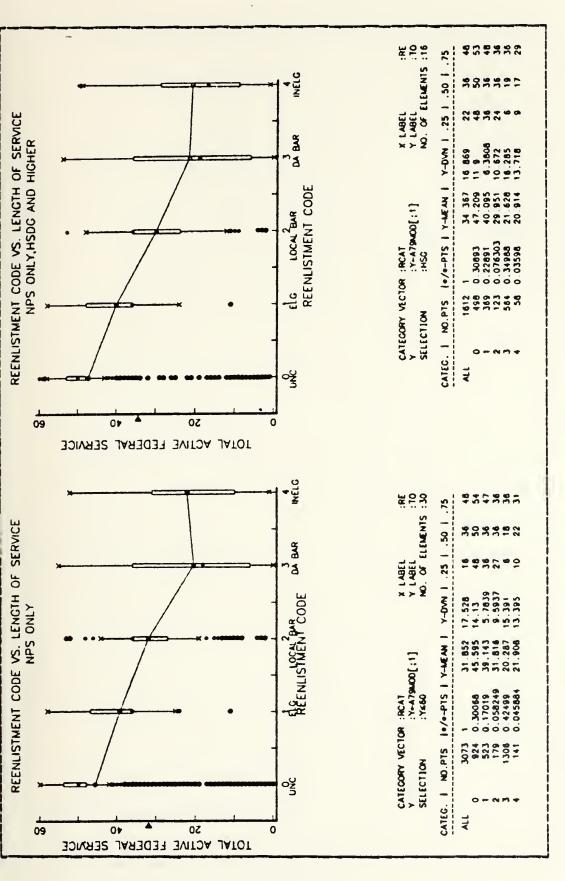


Figure H.40 Reenlistment Code vs. Service, II



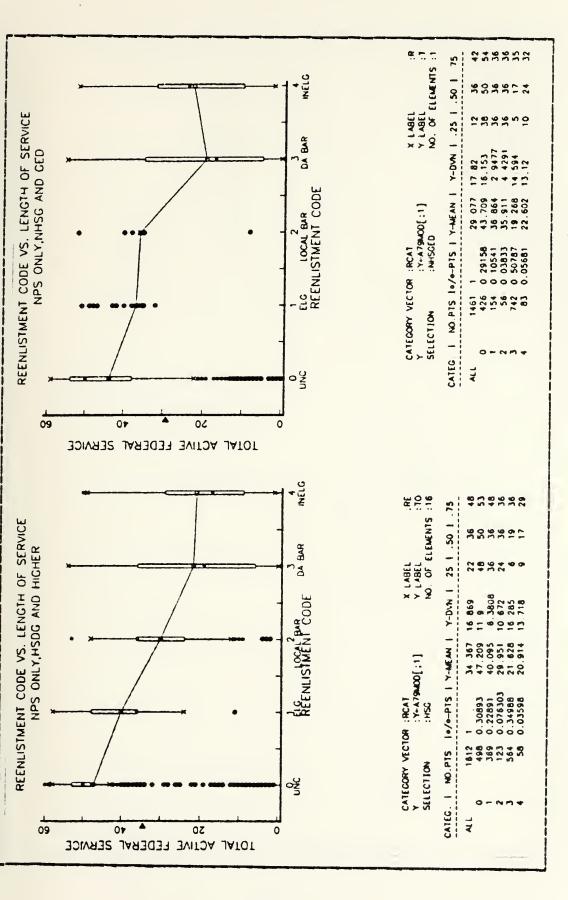


Figure H.41 Reenlistment Code vs. Service, III



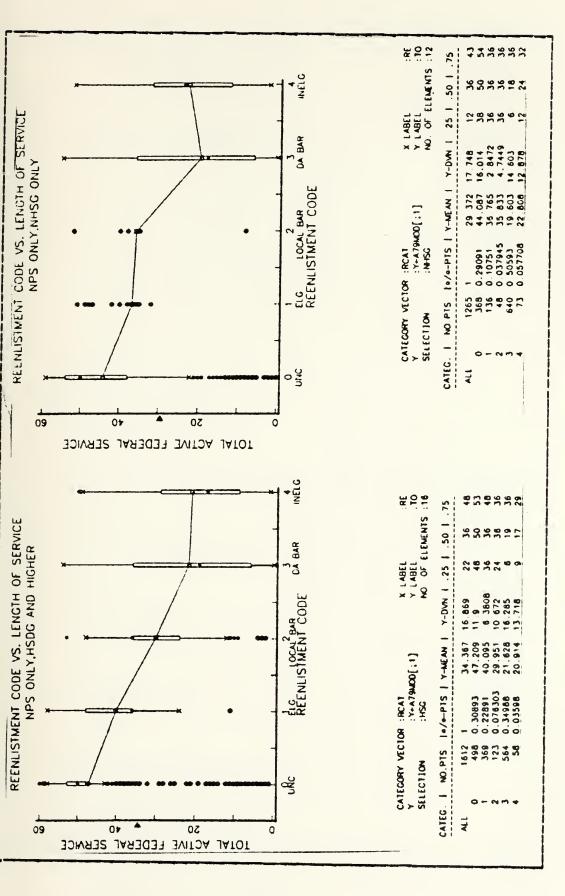


Figure H.42 Reenlistment Code vs. Service, IV



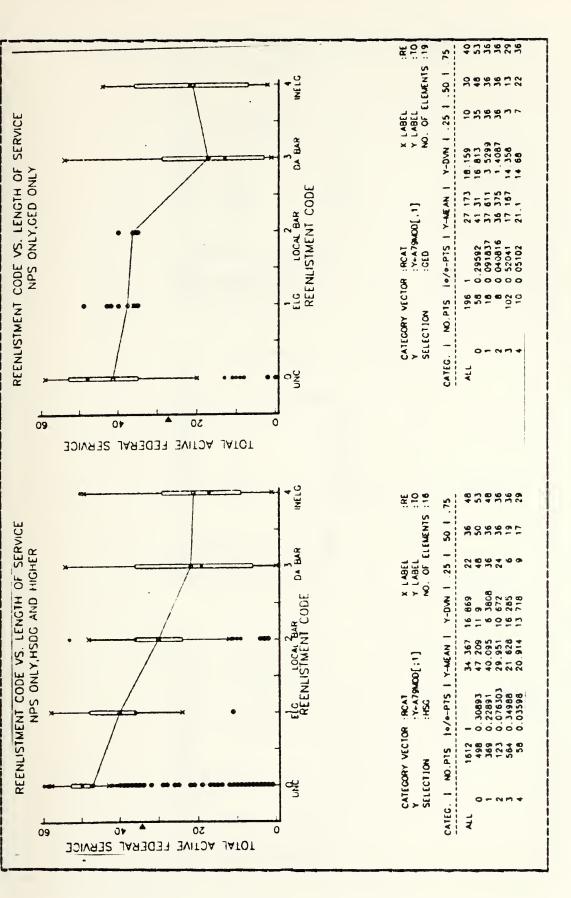


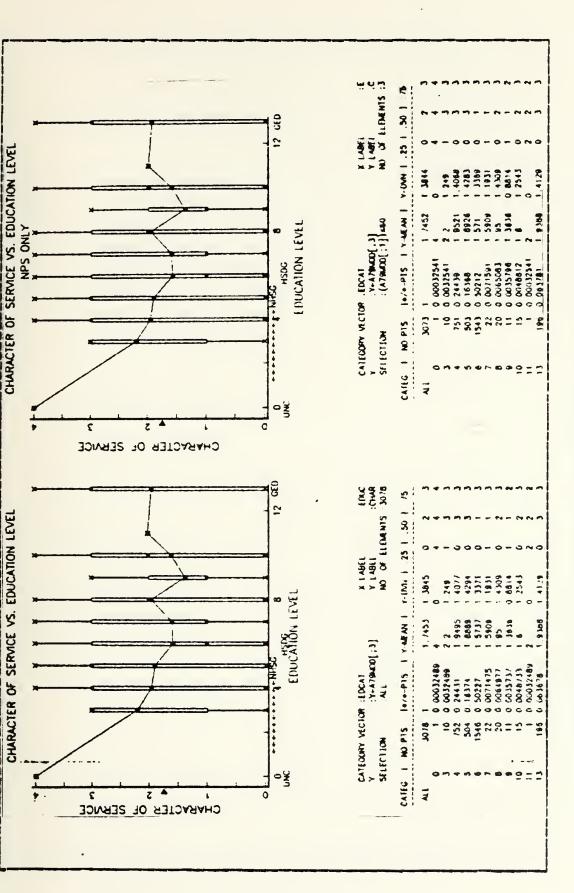
Figure H.43 Reenlistment Code vs. Service, V



Figure H.44 Reenlistment Code vs.

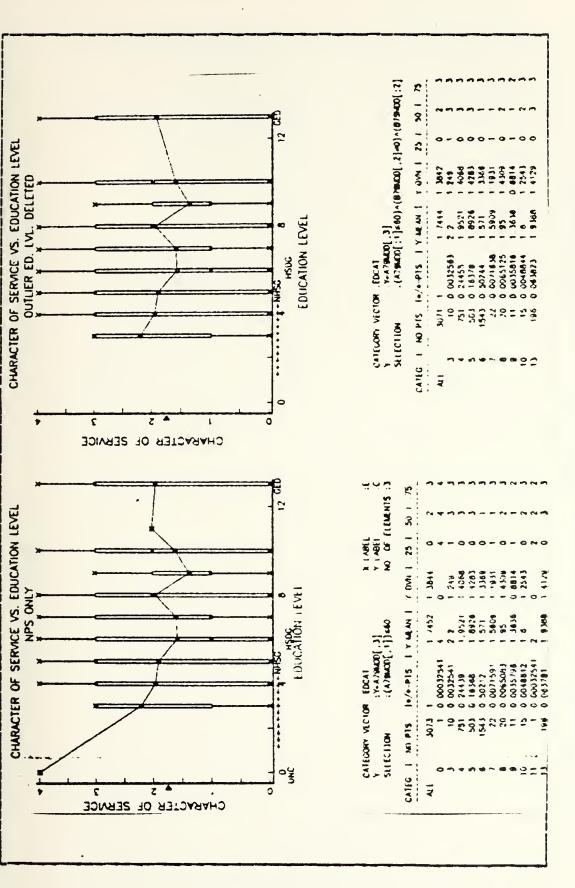
Service, VI





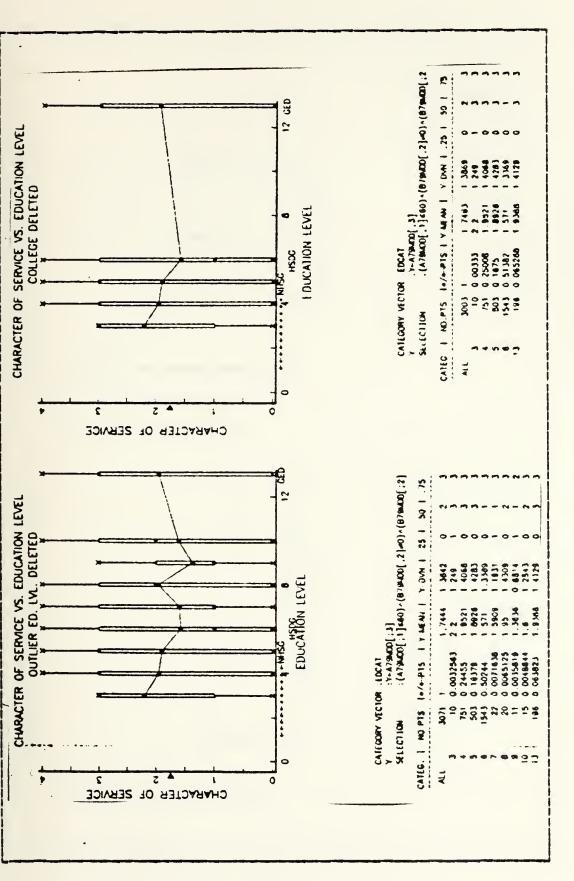
Education Level, I VS. Service of Character Figure H. 45





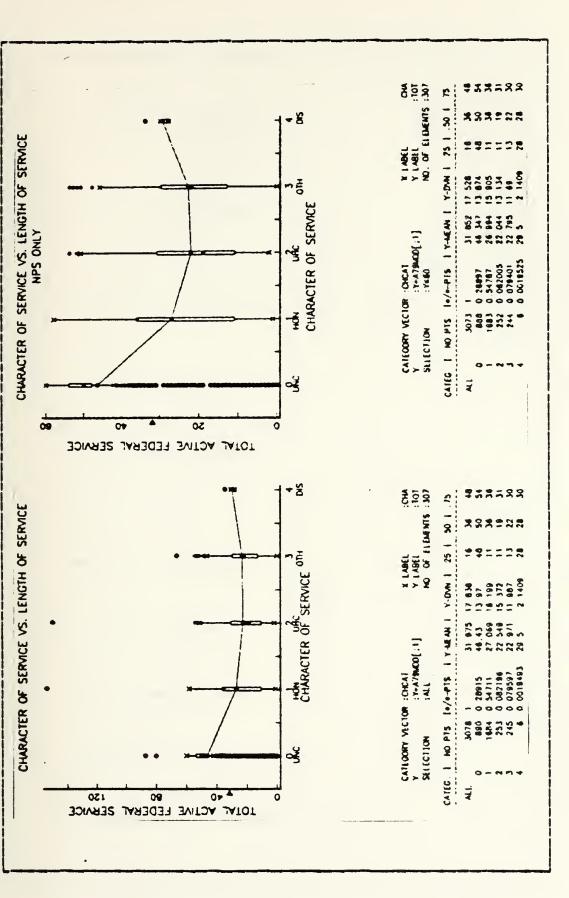
Education Level, II Service vs. of Character Figure B.46





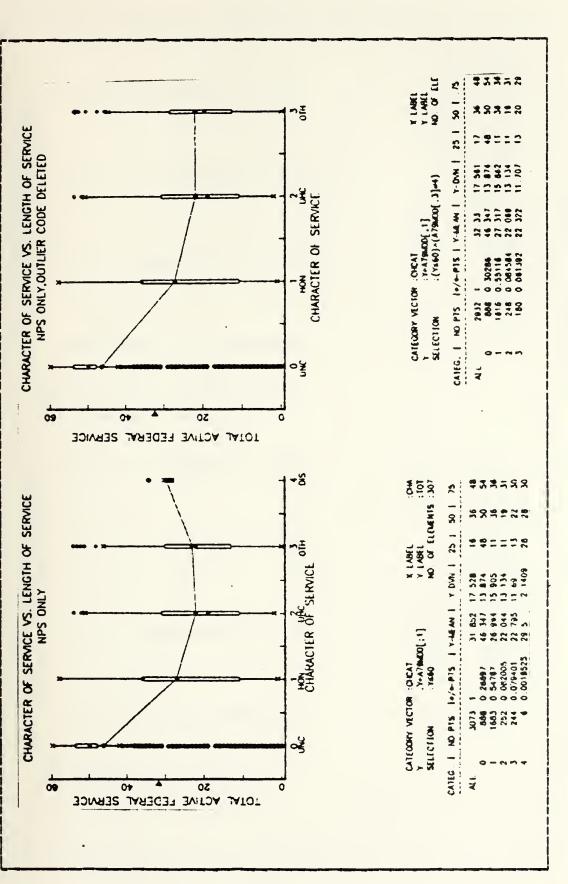
Education Level, III Service vs. Character of H.47 Figure





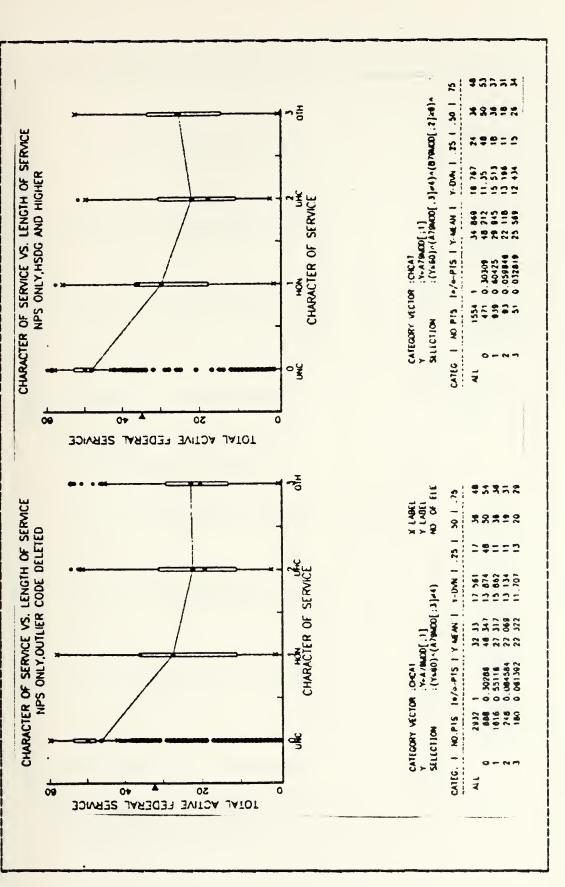
Service vs. Service, I Character of H. 48 Figure





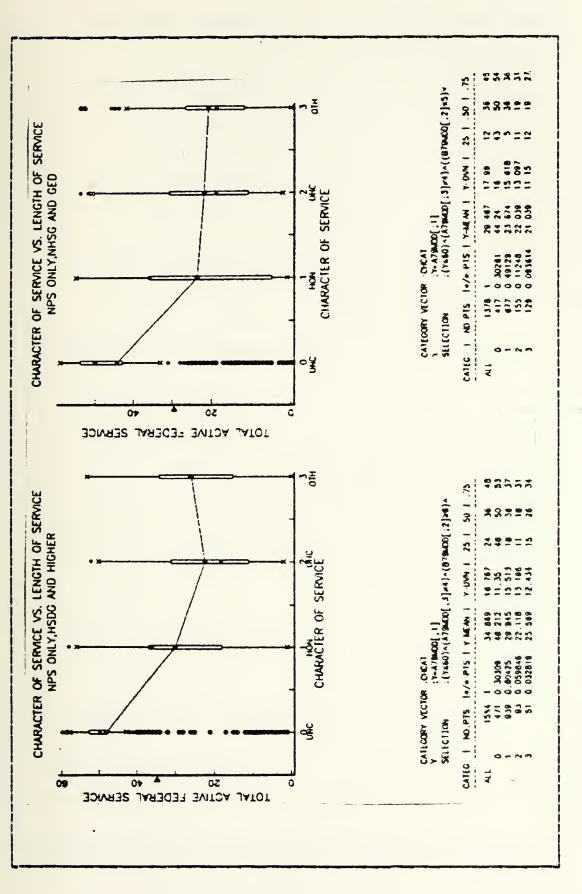
Service, II Service vs. of Character Figure H. 49





Service, III VS. Service of Character H.50 Figure





Character of Service vs. Service, IV Figure H. 51



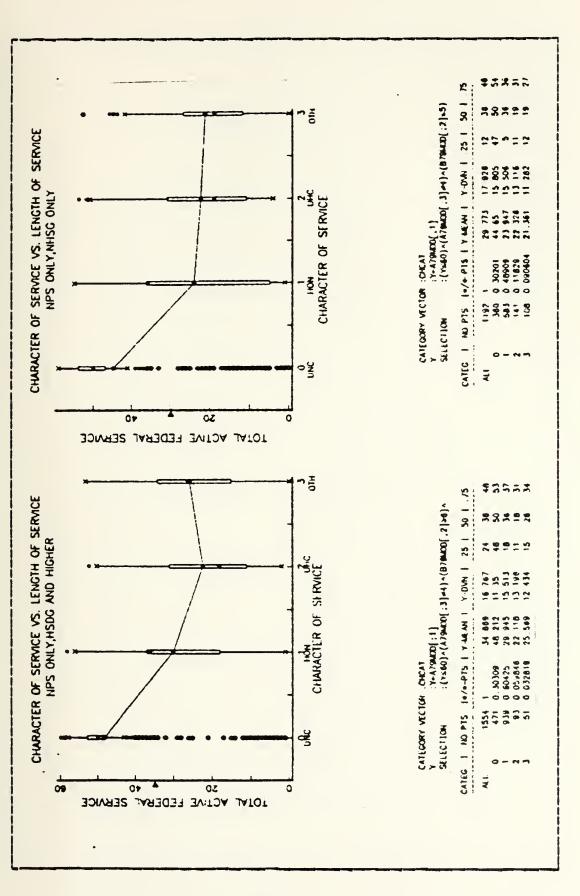


Figure H. 52 Character of Service vs. Service, V



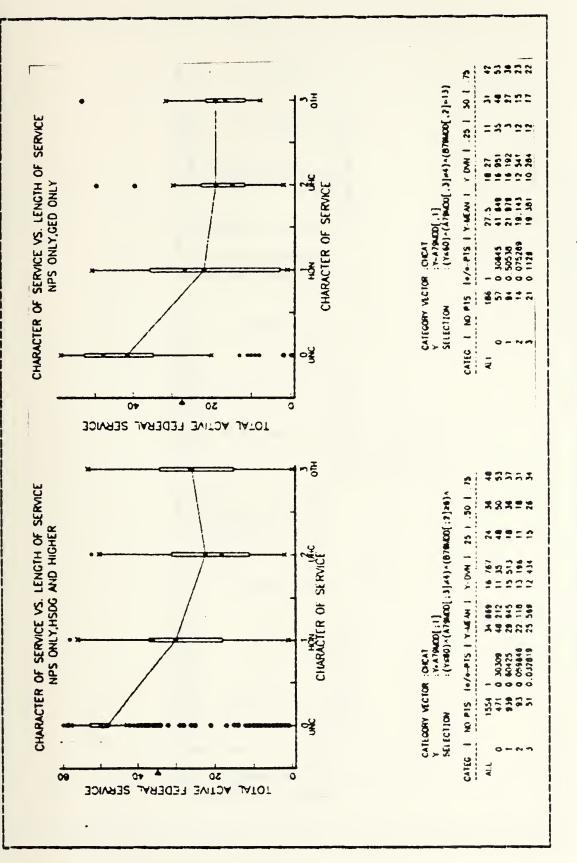
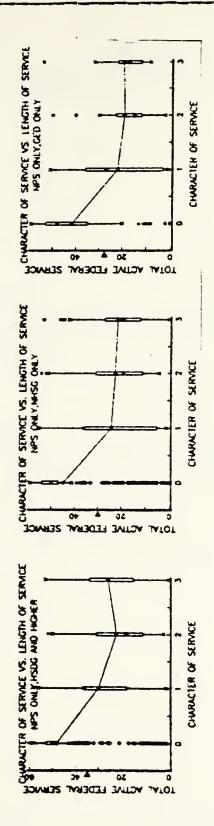


Figure H. 53 Character of Service vs. Service, VI





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APPENDIX I APL PROGRAMS TO PERFORM ONE-WAY ANOVA

```
VEDJAVOHAC
      V ZEANOVA TT;N;K;MAX;BTSS;TSS;TD
     'ANOVA WAS UPDATED 1/3/79, SEE ANOVAHOW FOR CHANGES.'
[1]
[23
     →ENTERX (1=f, TT
[3]
     NEFFMISSETETT
[4]
    MAX4F/N
[5]
    K+1467
     +SUM
[6]
[7] ENTER: INFUT
[8] SUM: +5KIFX ( (OPTION=1) V()=+/+/(Y=MISS)
     →Oxfp[+'RUN ABORTED; NO MISSING VALUES ALLOWED WHEN OPTION=2.
[9]
[10] SKIP: TD+Tx(MISS#T)
[11]
     SUMSQ
```



```
SUMSQ;C;NUMBER;B;BLDF;BLDCK;BLSS;EDF;F;MSBL;MSE;MSR;T;TDF;WTSS;T
         BAR
      T+++YD
[1]
[2]
      TSSE(+/(+/TD*2))-CE((+/T)*2)+RUMBERE+/R
[3]
      BLSS+(+/(((B++/TD)*2)+K))-C
[4]
      MSBL+BLSS+BLDF+MAX-1
[5]
      →7xl(OFTION=2)
[6]
      BLSS+BLDF+0
      WTSS\leftarrowTSS\rightarrowBLSS+BTSS\leftarrow(+/((T\star2)\divN))\rightarrowC
[7]
[8]
      MSR-FBTSS+K-1
[9]
      TDF+NUMBER-1
      F+MSR+MSE+WTSS+EDF+TDF-BLDF+K-1
[10]
      BLOCK+(B+K)-TBAR+(+/T)+NUMBER
[11]
[12]
                              ANOVA TABLE!
[13]
      ' SOURCE
                       DE
                                    55
                                                 MS
                                                           pr t
[14]
      □ 廿 ← ' '
      'B TREATMENTB, 15, F13, 2, F11, 2, F8, 2' FMT(K-1), BTSS, MSR, F
[15]
[16]
      → (OFTION=1)/L5
      'D BLOCKSD, 18, F13.2, F11.2, F8.2' FMT(MAX-1), BLSS, MSBL, (MSBL+MSE
[17]
)
[18] L5: 'U ERFORU, 19, F13.2, F11.2' FMT EDF, WTSS, MSE
      'O TOTALO, 19, F13.2' FMT TDF, TSS
[19]
[20]
      'OR-SQUARE = 0,F5.3' FMT(BTSS+BLSS)+TSS
      'moverall mean = m,F10.2' FMT TBAR
[21]
E223
      "BIREATMENT EFFECTS B,F6.2" FMT BISS+(T+N)-TBAR
E233
      Z+(MISS#T) XZ+T-(MAK, K) pT+N
E243
      → ( DFTION=1 ) / O
[25]
      'DBLOCK EFFECTS D,F6.2' FMT BLOCK
      Z+T-TBAR+BLOCK . +BTSS
[26]
      \nabla
```

VSUMS@[[]]V



```
DEMT[[]]
        □ OL←E FMT R$S$W$&$G$X$T$K$J$M$Q$F$D$N$O$L$B$V$CH$H
        NEGET WERE (15-24PR)PR
[1]
        OL+((1=1↑M) ↓ 1 O xM+M+2↑H+1<FCH+EH,',')FA+'0123456789.'
[2]
[3]
      <u>--→EXI(N+O=N)∨V+1≥₽5+₽E-----</u>
       L(); →~ ( V V ( x F + 4 x G = p K + p X + ' ' ' ) / * / ( ' A ' , O + ' 🗓 ' ) e 5
[4]
[5]
        →(LO+(V←O=F5←J↓5)+\¤=M[2]←1),Ŀ-(\x¤←O+,=K),Fx~'A';K←K,(J←5\'
, 1) 个5
        →E+xpS+'TEXT DELIMITER'
[6]
[7]
        \rightarrowL3-3xx(p\varphi\inK=K\in(KeT1\psi\Delta)/K)[W\inpX\in(pX\in(K)D)\uparrowK)\psi(-(\varphiK))QD)\psiK
       <u>Ŀ:→(¤←~1↑@</u>←KεΔ)/Ŀ3−2x(βK)≠₩←1↑¤←'XA'εK←(~Kε' ッ')/K
[8]
[9]
        →L3x1(B≠+/G)*xM[2]+10±|1+△1(B+|1-G10)*K
        →L3-Φ0,-(L+'EFI'εK)/xW+10±|1-Δ\(|1-G+B\',')/B+(1-(ΦG)\0)/K
[10]
        ⊕←(1↓ρ×←((1Гρ⊕)L(ME13-H),W)→⊕)Φ⊕
[11]
[12] L3:→(HDx\HA~'X'eK),E→FX←→W,D←OFF←((M→H,O)X1,W)FX
        →L4-\w14L,Q←14FR←(O 1 XFF←RE;\ME23←QLME23FQXVAP3)↓R
[13]
[14]
        門去門÷10×4~110@|P+0=門
[15]
        →L3x10=J←+/B←('B'εK)*0=F←(L0.5+Nx,F)÷N←10xD←10xl1-Δ15ψB
       L4:→(F1ΨPL)/F-FFX+(1 0 xFG+JFTX'T')FJ+J,O+√/T+O>F+B/F
[16]
        →(xL+(O[LxJ+'Z'∈K)[,xxT+(T+O+1+L1()@1[]F))>O+L+W-D+O+x2↓L)/L/
[17]
F,F,I
        →E+xpS+'FIELD WIDTH'
[18]
[19]
        →L4+1+1((J[2]←L√.<0)+0+1+10[.≤[L+(β/,L)+T+10=[F)>W-D+0+3
[20]
        TEMULERCT/114034L4818X4'E','+0T'CU82-XL3,AC1+8(0810)+1L3
[21] F:→(□∨2≥Pxw'T'eK)/I, N+FX+□[11, 1+Q(PF10)+FNx1||F], X
[22]
        D \leftarrow y = (-N) \land (Df \cdot x \forall N E \cdot 2 + D \exists \neq 1 \land \Delta) \circ \cdot \langle D \leftarrow \langle D \leftarrow 1 \rangle
[23]
        XENEX,X[D/\SXE,X]E' '
[24] I:→(J←J∨O=+/D←OFL-D)/I+FD←FF←G,∆[1+&(LF10)+L|F3
0250
        F+Df(,O+GΦO)\(,O+O*,<(-G)Φ\L+G+1\fG)/,F
[26]
        →H□-\J∨L+~'L'&K,F[T/\D+1^X+8F+F,X;]+'x`
[27]
        F \leftarrow \times_F (, \phi \circ) \setminus (, \phi \leftarrow \times \times_{A} \wedge \circ) /_{y} F
[28]
        → ( ~ H ) / E - N ← 1 , D ← O ፆ F ← E ← ( D , N ← W × 1 - 2 × L ) ↑ F
[29] HD:CH \leftarrow (FK \leftarrow (T1 \land D \leftarrow O, (ME23 L FD) \land D \leftarrow (', '=CH) / (FCH) \land CH) \land CH
[30]
        \mathtt{D} \leftarrow \bullet \bullet (\mathtt{ME23}, \mathtt{K}) \land \mathtt{O} = 1 = \mathsf{V} (\mathtt{ME23}, \mathtt{E}) \circ (\mathsf{V} \land \mathtt{D} \circ \bullet \bullet \mathsf{V} \land \mathtt{E} \leftarrow \mathsf{E} / \mathtt{D} \leftarrow 1 \lor \mathtt{D} - \mathsf{T} \land \mathtt{D} ) \setminus \mathtt{K}
[31]
        →(LO-VAXQ), FOL+OL, ((1=1↑M) \ MX1, W) FD, F
[32] E:K+'NO VALID E, I, OR F PHRASE'
[33]
        (+'FMT PROBLEM
                                    - ^ y K ) y + ( 1 y f 5 ) f 5
         \nabla
```



APPENDIX J INFUT SCREEN FOR IBM GRAFSTAT CDF PROGRAM

CLAULATIVE DISTRIBUTIONS

TYPE OF PLOT	: SURVIVOR	
DATA	: X	
DISTRIBUTION	. (TO ME FIT)	PARAMETER SPECIFICATION: A
	: 0	ESTIMATION WETHOO : 4
CENSORING	. •	CONFIDENCE LEVEL(S) : .95
		CONTINUE CENECIST
	: A	
FREQUENCIES	. 1	
K-S BOUNDS	: N	K-S CONFIDENCE LEVEL(S): 95
HORMALIZE (Y/N)	; ♥	
PLOT HEADER (IN GLOTES)		
SCREEN HEADER (IN OLDTE		
E ANIS LABEL (IN OLOTES		
Y AXIS LABEL (IN QUOTES	i) : A	
POSITION	: 1	
SCALE X-AXIS	: LIN	SCALE Y-AXIS : LIN Q YMAX
PARTIAL PLOT		LINE TYPES : 1 1
AXES AND ORID CONTROL		
		PHICS(3279) SHRETURN AMPRITE ON SCREET
CLEAR-CEFALAT 5-1	AST RESPONSES	SHERASE PHAYIS CONTROL SHIABLE
SE SPONSES SHO	SUTPUT 10-STORE	METRIEVE 11-INTO APL 12-SCREEN DISPLAT



APPENDIX K SURVIVOR CURVES FOR 3 YEAR ENLISTEES

This Appendix contains survivor curves for FY79 3 year-obligated enlistees for the six candidate explanatory variables listed in Table XVII below. Tabular summaries of the analysis and discussion of the analysis is provided in Chapter 4 of this thesis.

TABLE XVII Candidate Explanatory Variables

Sex Race Mental Category Marital Status/Number of Dependents Age Military Cccupational Skill



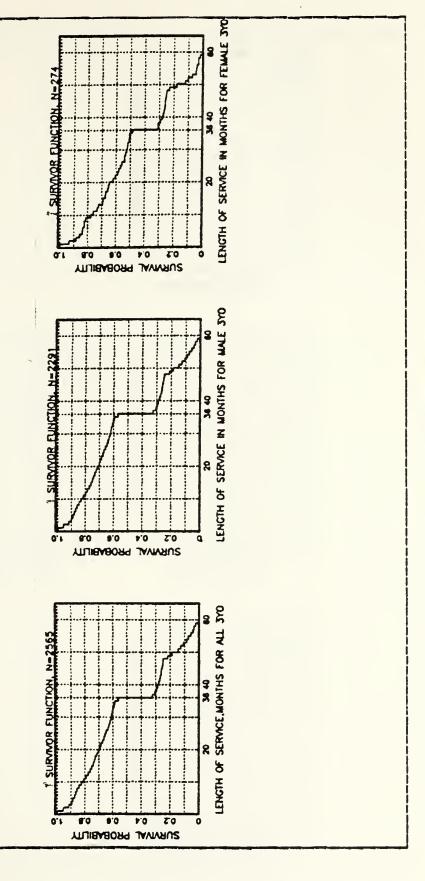
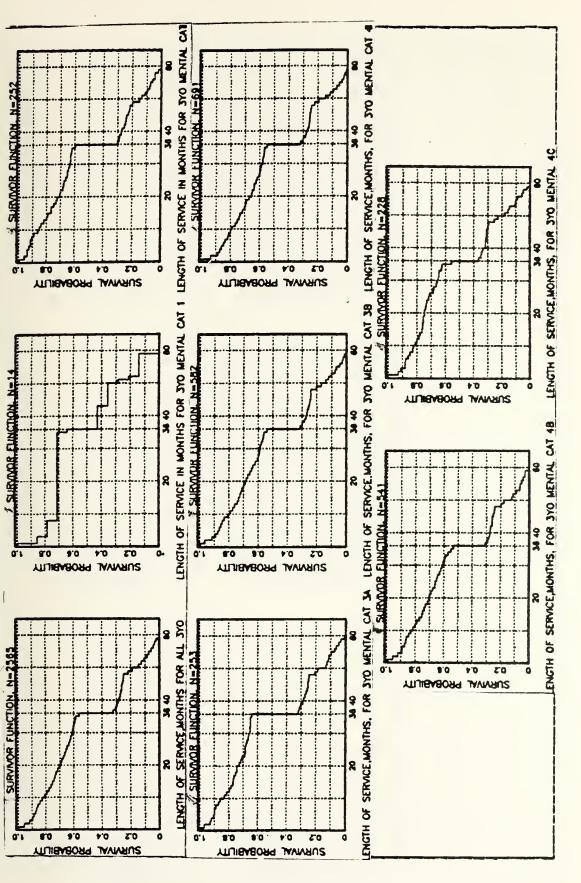




Figure K.2 Race



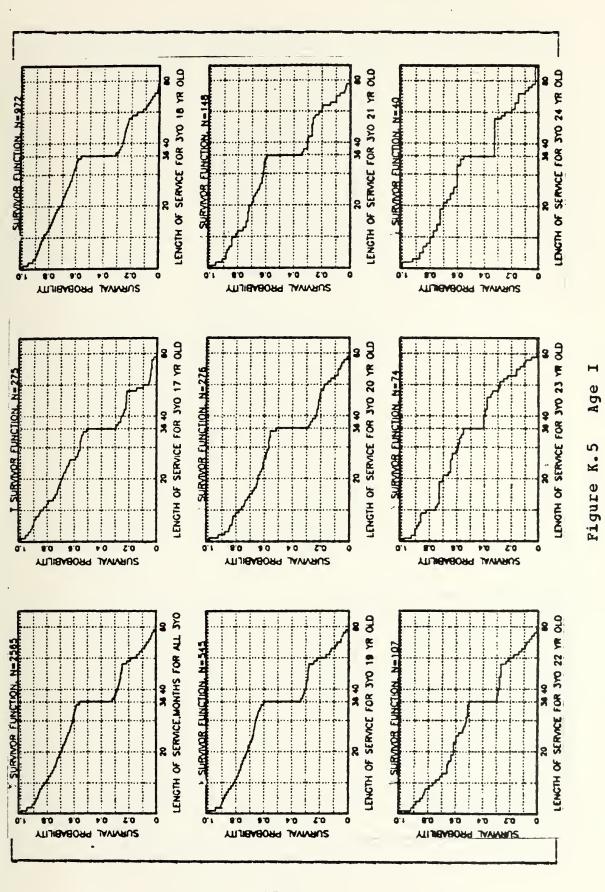


Pigure K.3 Mental Category



Marital Status/ Number of Dependents Figure K.







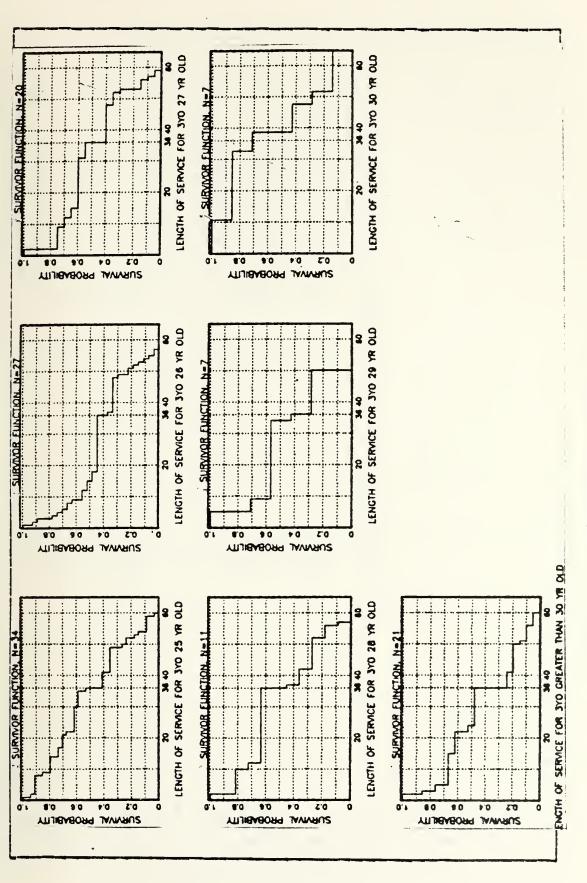


Figure K.6 Age II



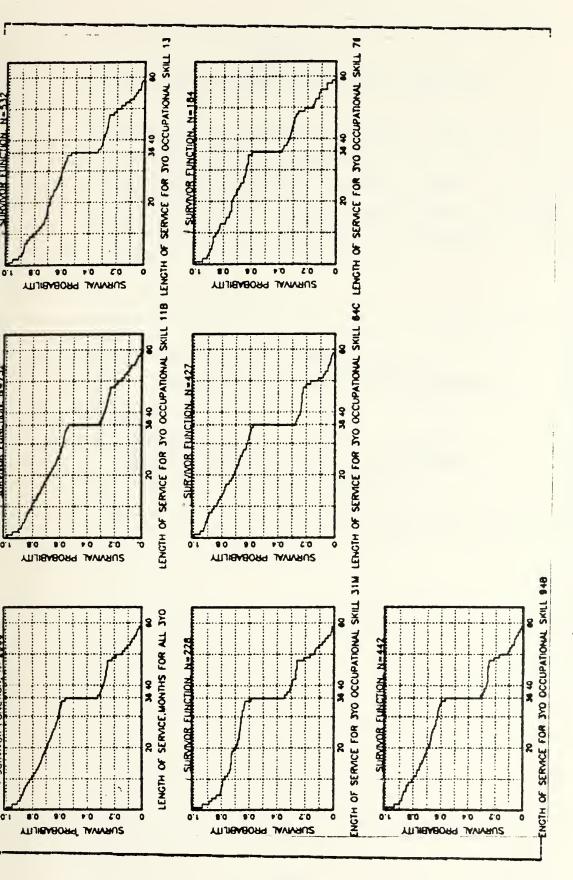


Figure K.7 Military Occupational Skill



APPENDIX L SURVIVOR CURVES FOR 4 YEAR ENLISTEES

This Appendix contains survivor curves for FY79 4 year-obligated enlistees for the six candidate explanatory variables listed in Table XVII below. Tabular summaries of the analysis and discussion of the analysis is provided in Chapter 4 of this thesis.

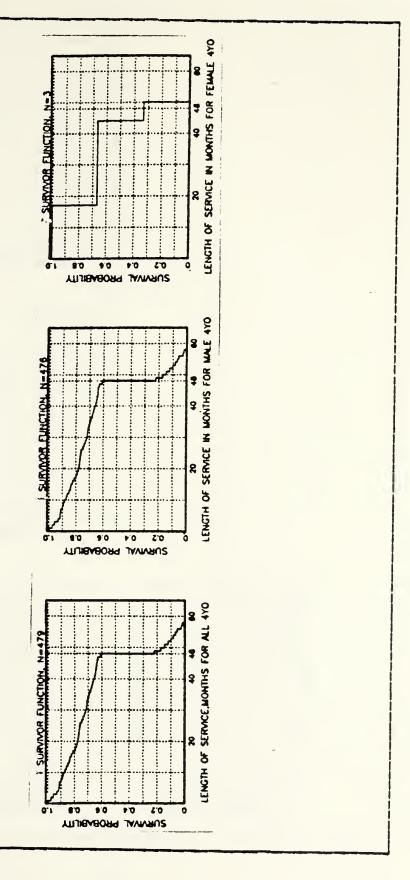
TABLE XVIII Candidate Explanatory Variables

Sex Race Mental Category Marital Status/Number of Dependents Age Military Cccupational Skill



Figure L. 1 Education Level







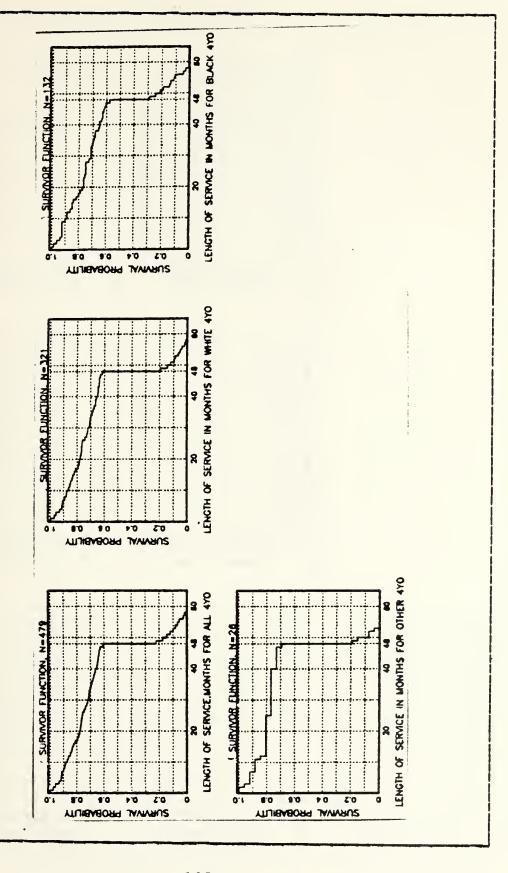
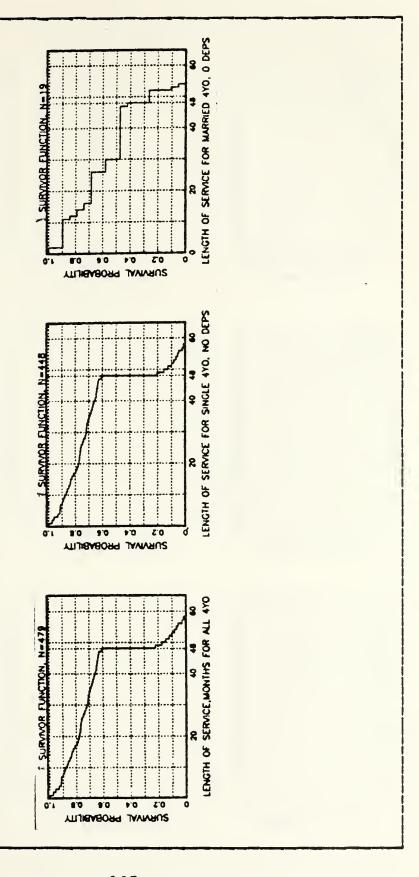


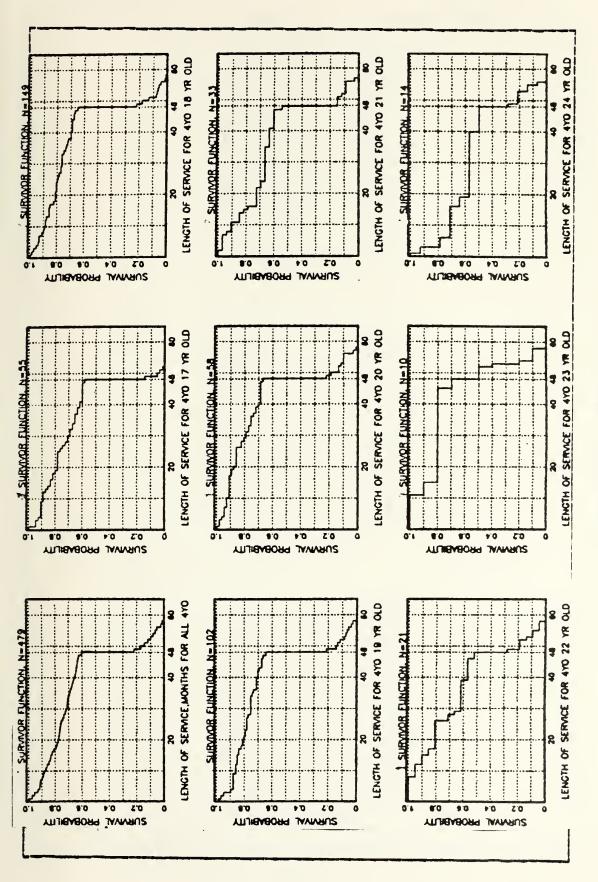


Figure L. 4 Mental Category









Pigure L.6 Age I



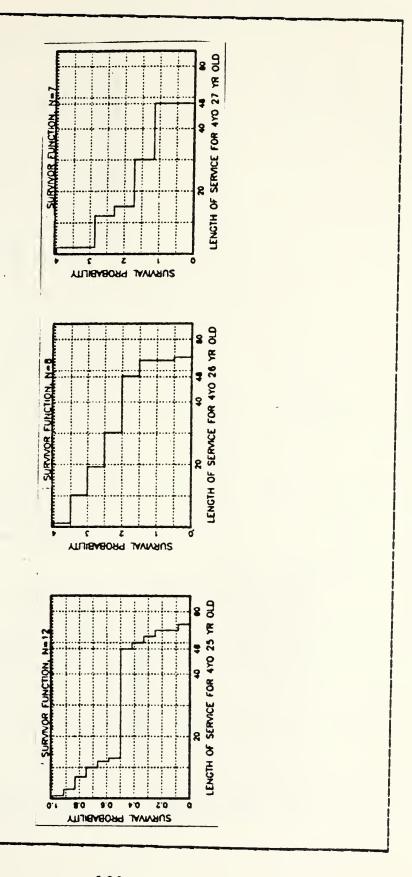




Figure L.8 Military Occupational Skill



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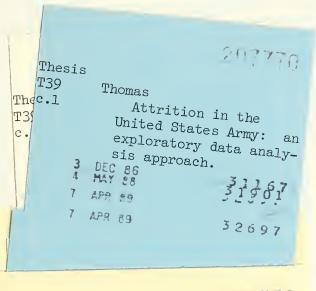
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